TDDD55-Lesson 1 Introduction to formal languages and automata theory and a brief introduction to Lab 1

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Agenda

- Hour I
 - Brief introduction to Automata Theory and Formal languages
 - Some hints for Lab 1
- Hour 2
 - Problem-Solving
 - (See exercises on the course homepage)
 - If time permits, start with Lab-1



A Formal Language

- Consists of words
 - A.k.a Strings, Symbol sequence?
- A word consists of letters
 - A.k.a Symbols, Glyphs
 - Do not need to be what we think about as letters
- Must be well-formed
 - That is, in short, conform to the rules and structures defined for it
 - Natural Language Examples:
 - **I** painted a nonexistent house
 - ✤ Well-formed but does not make sense
 - □ bicycle ride I
 - ✤ Not well-formed but can be understood
- Classes of languages exist
 - More about this later in the course



What is a Letter and an Alphabet?

- Letter (Symbol, Glyph,...)
- Alphabet usually denoted with the Greek letter sigma
- EX:
 - $-\Sigma = \{A, B\}$



Words

- From these definitions we know that AAA, ABA and ABBBBA are words in <u>our</u> language, assuming it is well formed
- A formal language is the set of the possibility infinite words we can construct from our alphabet
- EX:
 - $-\Sigma = \{A, B\}$
- Some possible words
 - W = {A, AA, AAA, AAAA,}



Automata?



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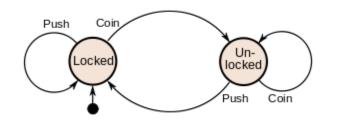
Examples of Automata

- Your Computer
 - It is a Turing machine
- The Coffee Machine
 - Finite State Machine (**FSM**). However, it might as well be a Turing machine $as^1 \otimes$
- Different classes of Automata
 - Read more in Introduction to Automata Theory, Languages, and Computation $\textcircled{\odot}$
 - Chapter 1 & Chapter 2 are **relevant** for this course
 - □ Focus on concepts, not proofs/lemmas².
 - Full Course
 - German Languages and Automata Theory, 6 credits (TDDD14)
- For Lab 1, we deal with FA and regular languages
 - More specifically, regular expressions, which we use to specify our Automata that do tokenizing

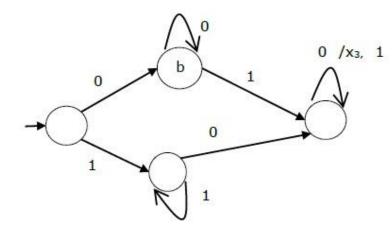


¹Now, in the 2020s, even fridges might be Turing Machines

• What is Automata Theory?



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- In textbooks, Automata are usually depicted using State Diagrams
- Moore and Mealy machines are a variant of automata with output ?
 - Moore
 - The Output is associated with the state
 - Mealy
 - The Output is associated with the transition from one state to the next



Digital Logic

- Digital Logic is a language
- Alphabet
 - $-\Sigma = \{0,1\}$
- Words:
 - {00, 01,10,11...}
- Can be described by a regular expression
 - **-** [O-1]⁺



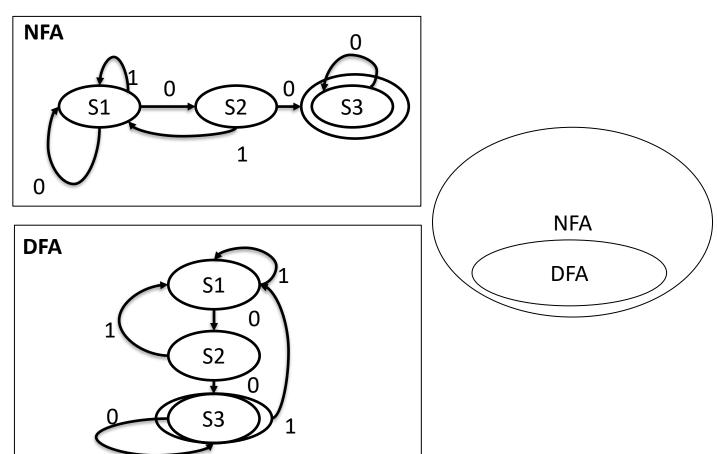
State Diagrams/Finite Automaton (FA)

- Directed graph (Digraph)
 - Set of states:
 - Set of transitions:
- A string is accepted by an **FA (Finite Automaton)** if we go from the start state to some accepted state
- Nondeterministic finite automaton (NFA)
 - Theoretical
 - Can be simulated



State Diagrams/Finite Automaton (FA)

- Nondeterministic finite automaton (NFA)
 - Theoretical
 - Can be simulated
- Deterministic Finite Automaton (DFA)
- Furthermore
 - A DFA is an NFA, but a DFA is not an NFA
 - DFA can be seen as a "restricted" NFA
 - NFA gives you more creative freedom when modeling
 - Ad-hoc Transitions



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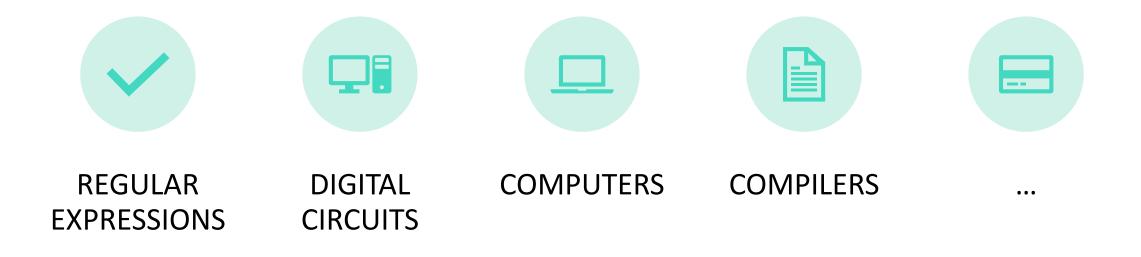


Practical Applications



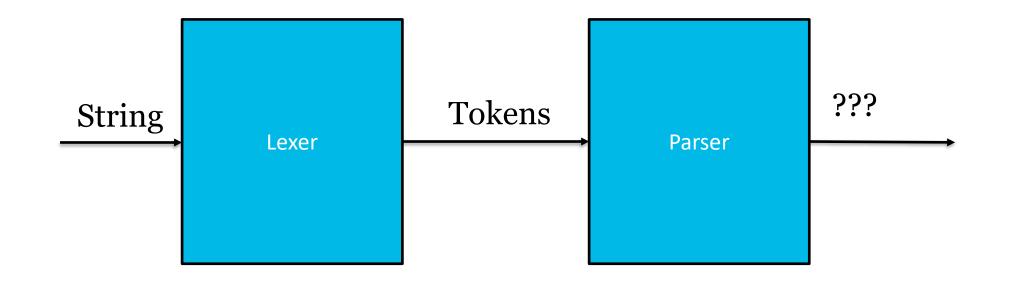
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Applications

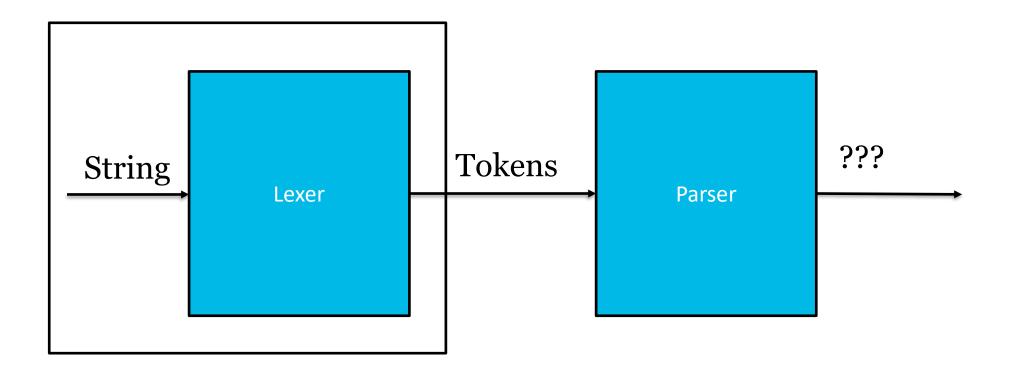




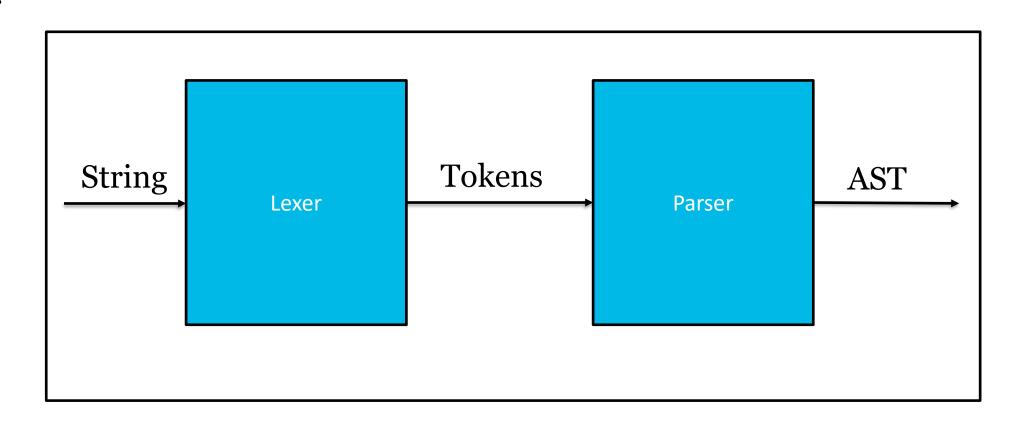
Compiler Pipeline













Regular expressions and Finite Automata (FA)

- What is accepted by FA can also be described by a regular expression!
- Important. The limitations of finite automata also applies to regular expressions
 - Finite automata can only count
 - □Can not solve the problem of balanced parenthesis
 - □Can not process context free-grammars
 - Hence, you can not parse using regular expressions



Dictionary. Some short terms explained

- Σ = Alphabet, sequence of symbols (Sigma)
- \mathbf{Q} = The set of states in our FA
- $\boldsymbol{\delta}$ = State transition function (Small Delta)
- F = Set of final states, or you can say accept states
- q_0 = Initial state
- FA = Finite Automata
- NFA = None deterministic finite automata
- DFA = Deterministic finite automata



Dictionary. Some short terms explained

- ε = Empty string (Small Epsilon)
 - AεBεC ⇔ ABC
- * = The Kleene star
- *AB* = Juxtaposition (Concatenation) between string A and B
- + and |
 - In the tradition of the text (Formal languages): + means "or" (|)
 - It might also mean concatenation/juxtaposition in some recent literature
 - Please state what definition you use



Technique to generate NFA from a regular expression



Converting Regular Expresisons to NFA: Thompsons algorithm

- Converts regular expressions into a corresponding NFA
- Not a part of the course but might be useful to learn anyway
 - Usually, intuitive approaches work as well





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Hints for Lab 1

- Instructions:
 - https://www.ida.liu.se/~TDDD55/laboratories/instructions/lab1.html
- Clone the lab from
 - <u>https://gitlab.liu.se/tddd55/tddd55-lab</u>
- In this course, it is extra important to consult the documentation and not attempt to make progress by trial and error!
- Remember also to handle tabs (\t)
 - New in 2023

□ A test for Lab-1 that checks this



- Lab 1 consists of several files
 - main.cc
 - Makefile
 - Makefile.dependencies
 - scanner.h
 - scanner.l
- scanner.l is the only file that you need to modify
 - You will reuse your results later in Lab 3/4



- To Compile:
 - Type make in the directory where the files are
- Test the lab by executing:
 - ./scanner ./test/<file-you-want-to-run>
- It is recommended that you start with the identifiers



- Scanner specification via regular expressions
- Some definitions that <u>usually</u> mean the same thing
 - Tokenizer, Lexical analyzer, Scanner
- Necessary to escape special tokens (Or rather token that has a meaning in Flex)
- Try the examples from the Flex manual
 - https://www.ida.liu.se/~TDDB44/laboratories/instructions/_static/flex/index.html
- Remember also to handle tabs (!) "\t"



- An Integer with a dot
 - INTDOT $[0-9]^+$ \.
- An Integer
 - INTEGER $[0-9]^+$
- An Integer without a period or an Integer with a period
 - INTEGER_OR_INTDOT (INTEGER)|(INTDOT)
- Nested comments might be hard.
 - Tip: Read up on Flex start conditions.
 - See chapter 10 in the flex manual.



Extended solution proposals

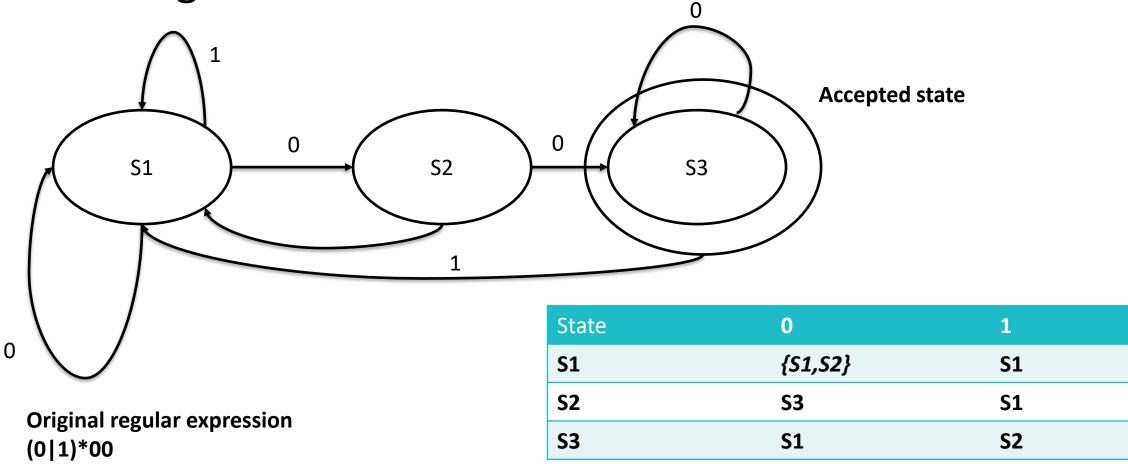


Extended solution proposal to Exercise 2.1 (A)

- a) $L_1 = \{x \in \{0, 1\}^* \mid x \text{ ends in } 00\}$
- We can write L1 as the following regular expression:
 - $-(0|1)^*00$
- From this we define our NFA
 - From our starting state we can select between two paths
 - 0* or 1*
 - For oo. We simply go forward two steps



Resulting NFA





Note not according to Thompson's algorithm. Furthermore, note that this is not a DFA, it is nondeterministic since we can either go to S1 or to S2 in state S1

Extended solution proposal to Exercise 2.1 (A)

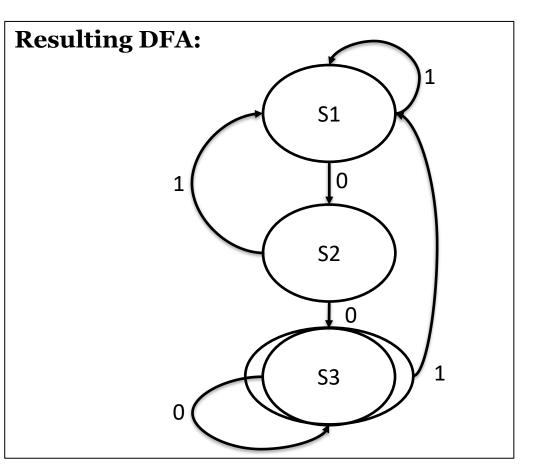
- Deriving a DFA
- (Q , Σ , δ , q_0 , F)
 - Alphabet: $\Sigma = \{0, 1\}$
 - Transition function: δ See next slide
 - States: Q = $\{S_{1}, S_{2}, S_{3}\}$ //*Intuition*: We have to handle atleast 3 tokens
 - Accept states: $F = {S_3}$
 - *S*1 –> *S*2 –> *S*3 for the input 00

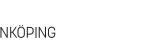


State transition table for our transition function: δ

State Input	0	1
S1	S2	S1
S2	S3	S1
S ₃	S ₃	S 1

- Alphabet: Σ = {0, 1}
- Transition function: $\boldsymbol{\delta}$
- States: Q = {S1,S2,S3}
- Accept States: F = {S3}





Teaser for the next theme: (Context Free Grammars/ Lab 2)

GrammarsDescribing Regular Expressions using Grammar



Regular Expressions to Grammar (Exercise 2.4)

- Given the following regular expressions
 - $-00(1|0)^{*}1$
 - $-101(101)^* 101(010)^*$
 - $-(11|010)^*11(00|11)^*$
- Find Context Free Grammars(CFG) that correspond to the word that is accepted by the regular expression
- If there are any insecurities regarding CFG and production rules, see lecture 3



Regular Expression 2.4 (A)

- $00(1 \mid 0)^* 1$
- For this expression we shall first consider the types of strings we can accept
- We know that our alphabet is:

 $-\Sigma = \{0,1\}$

- Let's derive a set of words that we would accept:
 - {001, 0001, 00101, ...}
- Note the Kleene star * and |
 - Kleene star * allows the empty string



Deriving a CFG for 2.4 A

- $00(1|0)^* 1$
- Intuition
 - From the expression above we notice that we always need oo as a prefix
 - Likewise, the suffix must be 1
- Rule 1
 - $-S \rightarrow 00A1$
 - We do not yet bother with what A should be



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Deriving a CFG for 2.4 A

- $00(1|0)^* 1$
 - We know that 1|0 means a 1 or zero
 - From this we know that (1|0)* gives the set:
 - {ε,0,1,00,01,10,11,001,...}
 - 2^N Different combinations where N is positive infinity
- Zero (ε) times gives us:
 - $-001 \Leftrightarrow 00\epsilon 1$ So we can introduce the rule A $\rightarrow \epsilon$



Deriving Rules for 2.4 (A)

- $S \rightarrow 00A1 \& A \rightarrow \varepsilon$
 - Now we look at $00(1|0)^*$ 1 again
 - $-(1|0)^* //{\epsilon, 10, 110, 1110, ...}$
- For the entire expression we would have 00101 for 10
 - Notice that we need flexibility here. We can't simply state that A is 10. The reason is that A might be 110 or 1110
 - If we say $A \rightarrow 1A$ or $A \rightarrow 0A$ we get this flexibility
- Set of production rules for our CFG are: $\{S \rightarrow 00A1, A \rightarrow \epsilon, A \rightarrow 1A, A \rightarrow 0A\}$



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References

Hopcroft, J. E. (2008). *Introduction to automata theory, languages, and computation*. Pearson Education India.

Aho, A. V., Sethi, R., & Ullman, J. D. (1986). Compilers, principles, techniques. *Addison wesley*, *7*(8), 9.

