



Automated Planning

Relaxed Planning Graphs

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Apply delete relaxation

Create a graph
efficiently representing many ways
of achieving the goal
in the relaxed problem

Extract one possible solution π from the graph
(not necessarily optimal!)

$$h_{FF}(n) = |\pi|$$

or

$$h(n) = \text{cost}(\pi) \geq h^+(s)$$

Running Example

■ Running example due to Dan Weld (modified):

- Prepare and serve a surprise dinner,
take out the garbage,
and make sure the present is wrapped before waking your sweetheart!

$s_0 = \{\text{clean}, \text{garbage}, \text{asleep}\}$

$g = \{\text{clean}, \neg\text{garbage}, \text{served}, \text{wrapped}\}$

<u>Action</u>	<u>Preconds</u>	<u>Effects</u>
cook()	clean	dinner
serve()	dinner	served
wrap()	asleep	wrapped
carry()	garbage	$\neg\text{garbage}, \neg\text{clean}$
roll()	garbage	$\neg\text{garbage}, \neg\text{asleep}$
clean()	$\neg\text{clean}$	clean



Running Example (2)

■ Let's apply delete relaxation

- Prepare and serve a surprise dinner,
take out the garbage,
and make sure the present is wrapped before waking your sweetheart!

$s_0 = \{\text{clean, garbage, asleep}\}$

$g = \{\text{clean, served, wrapped}\}$

<u>Action</u>	<u>Preconds</u>	<u>Effects</u>
cook()	clean	dinner
serve()	dinner	served
wrap()	asleep	wrapped
carry()	garbage	–
roll()	garbage	–
clean()	–	clean

**Pointless actions:
No effects!**



- Now we want to find a relaxed plan
 - What is **true** initially?
 - ➔ first proposition level in a relaxed planning graph

Proposition
level 0

garbage

clean

asleep

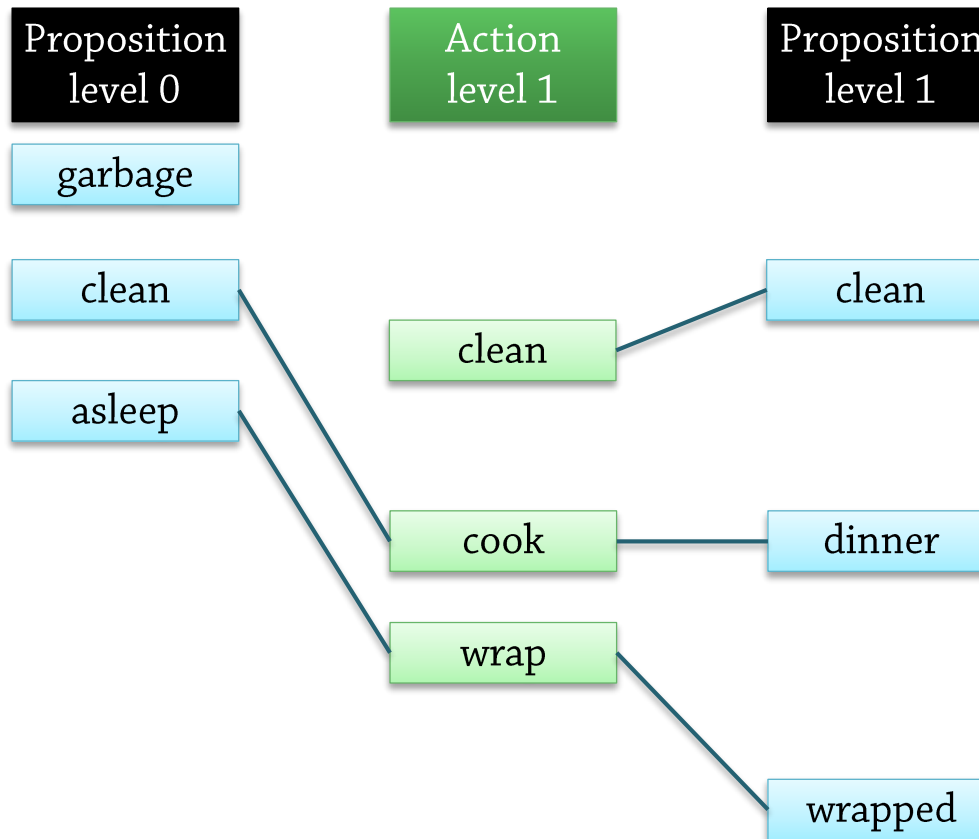
Planning Graph introduced by GraphPlan

Heuristics based on Relaxed Planning Graph
pioneered by FF (FastForward)

RPG 2: Actions and Effects

■ Next step:

- Which actions could be executed first?
- Which effects would we get?



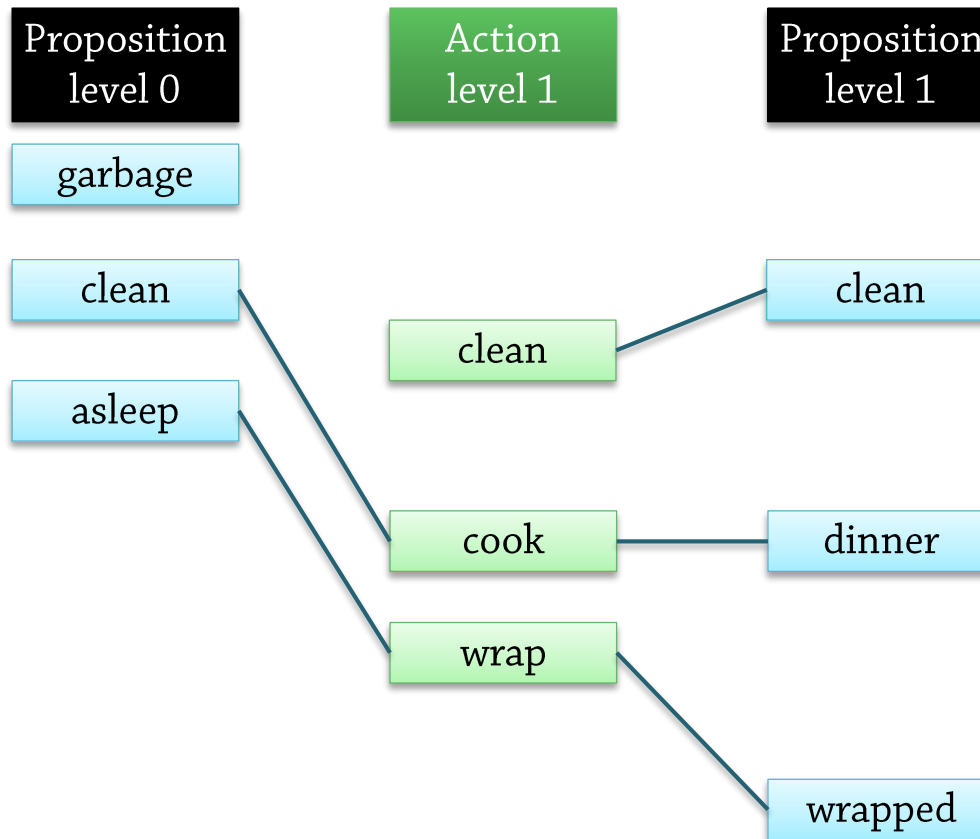
<u>Action</u>	<u>Prec</u>	<u>Effects</u>
cook	clean	dinner
serve	dinner	served
wrap	asleep	wrapped
clean	–	clean

**Build a graph
with actions linking
to preconds and effects**

**Assumes conjunctive
preconds, effects!**

RPG 3: Interpretation

- Here we see:
 - Which propositions can we make true in one step?
 - Which actions would we need?



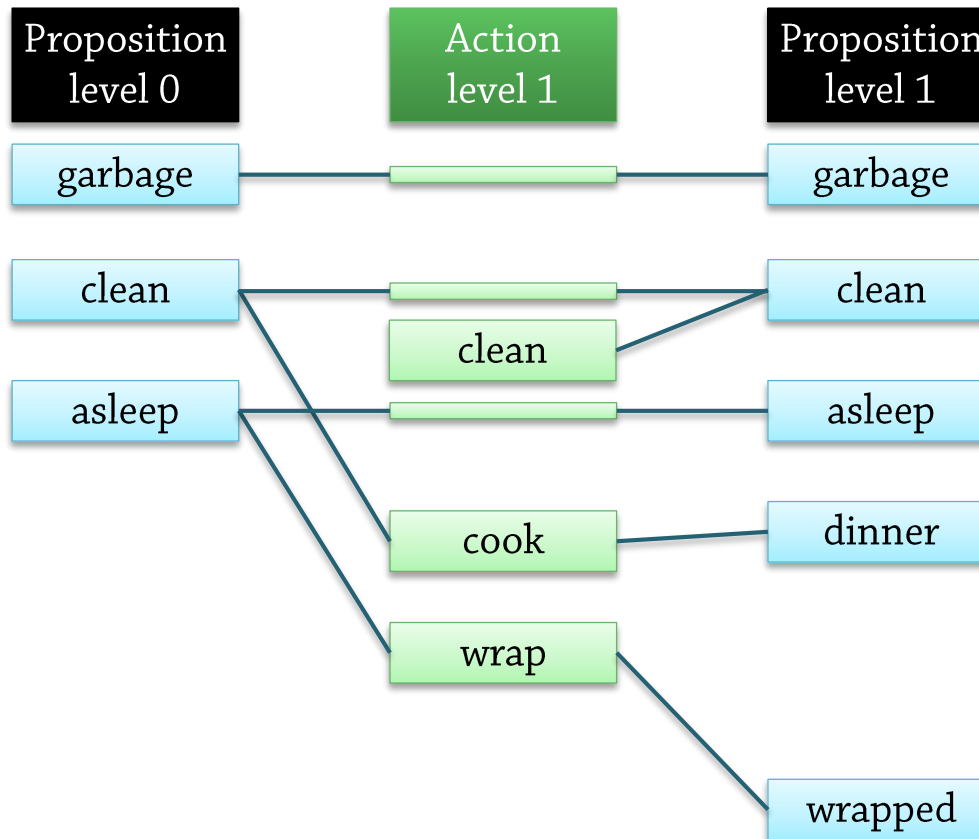
<u>Action</u>	<u>Prec</u>	<u>Effects</u>
cook	clean	dinner
serve	dinner	served
wrap	asleep	wrapped
clean	–	clean

But wait!

**Prop level 1 is missing
"garbage", which
could *remain* true
from prop level 0...**

RPG 4: Maintenance Actions

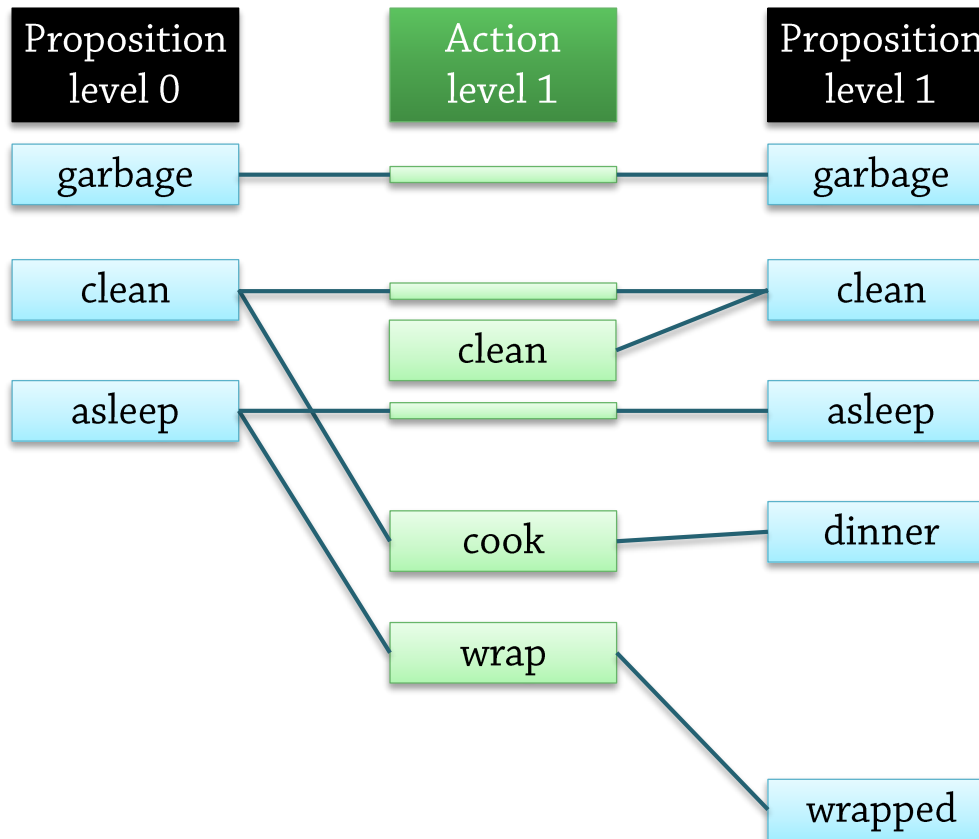
- Solution: "No-op" or "maintenance" actions
 - One for each proposition (fact) that exists
 - No need to treat *persistence* separately



<u>Action</u>	<u>Prec</u>	<u>Effects</u>
cook	clean	dinner
serve	dinner	served
wrap	asleep	wrapped
clean	–	clean

noop-clean
precond: clean
effect: clean
noop-garbage
...

- What does this mean for the actions?



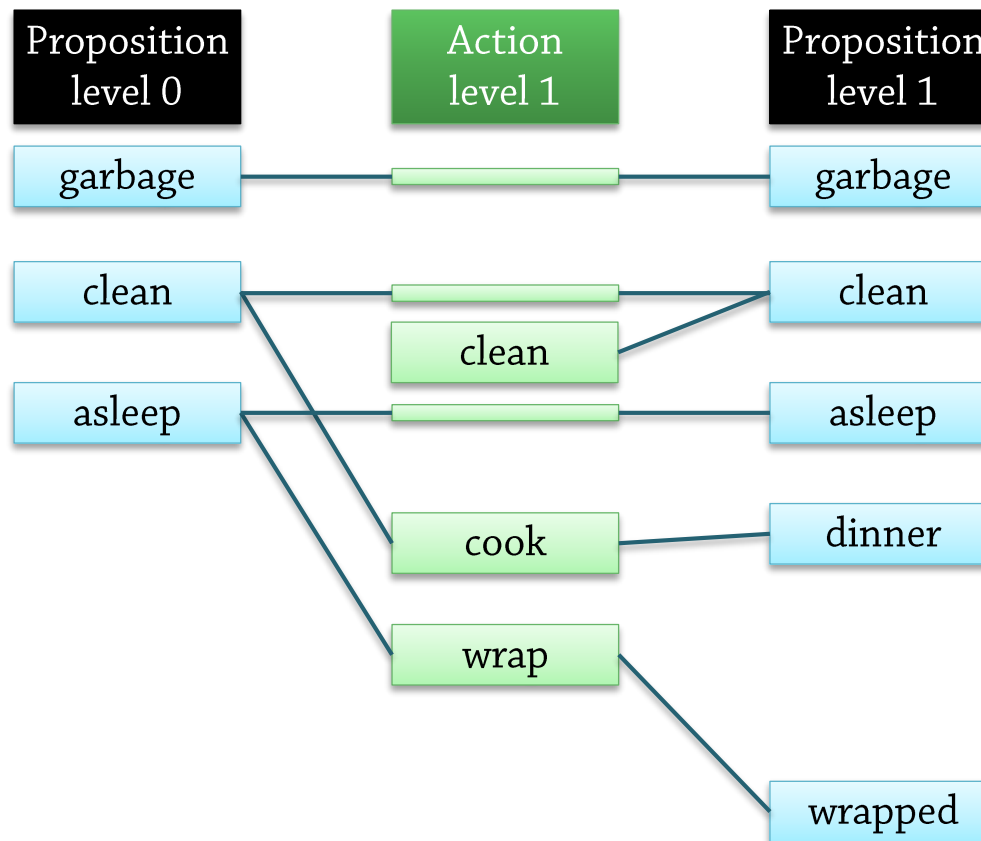
<u>Action</u>	<u>Prec</u>	<u>Effects</u>
cook	clean	dinner
serve	dinner	served
wrap	asleep	wrapped
clean	–	clean
noop...		

First action could be clean, cook or wrap

First actions could be any combination of clean, cook or wrap

**None can invalidate the others' preconditions:
No negative effects!**

- What does this mean for the facts?



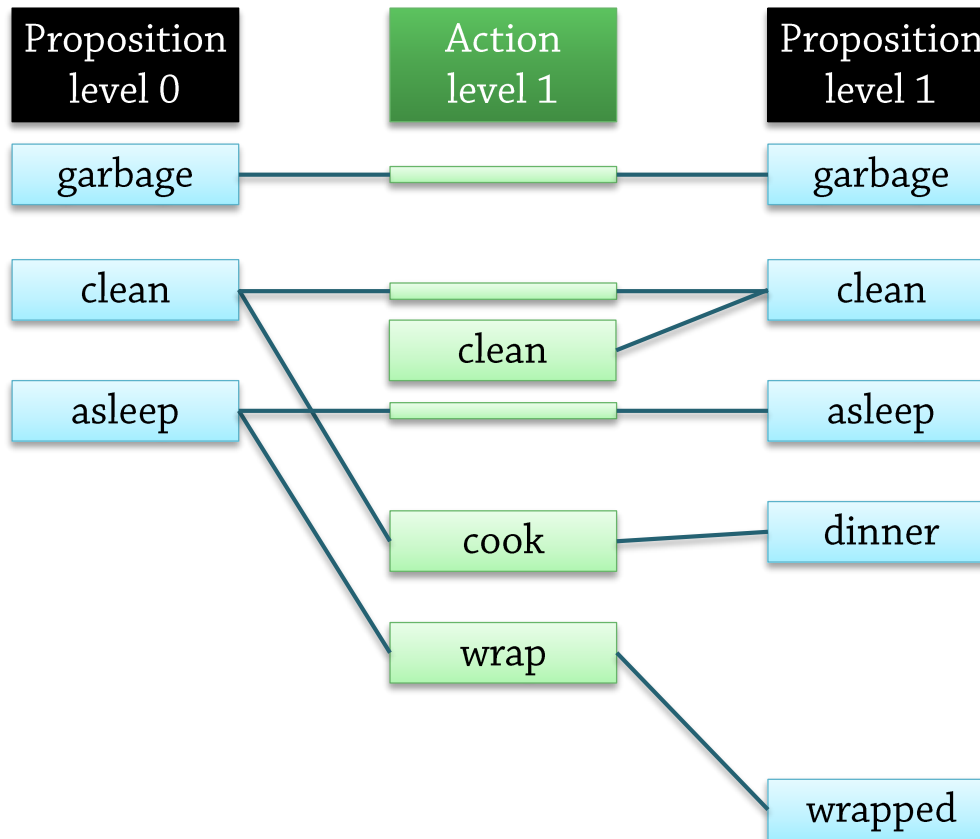
<u>Action</u>	<u>Prec</u>	<u>Effects</u>
cook	clean	dinner
serve	dinner	served
wrap	asleep	wrapped
clean	–	clean
noop...		

We can **choose** actions that achieve any subset of { **garbage, clean, asleep, dinner, wrapped** } and we don't have to care about their order!

Given delete relaxation!

In reality, negative effects interfere... but we aim for a heuristic!

- Can we reach the goal now?
 - No, can't achieve served yet...



<u>Action</u>	<u>Prec</u>	<u>Effects</u>
cook	clean	dinner
serve	dinner	served
wrap	asleep	wrapped
clean	–	clean
noop...		

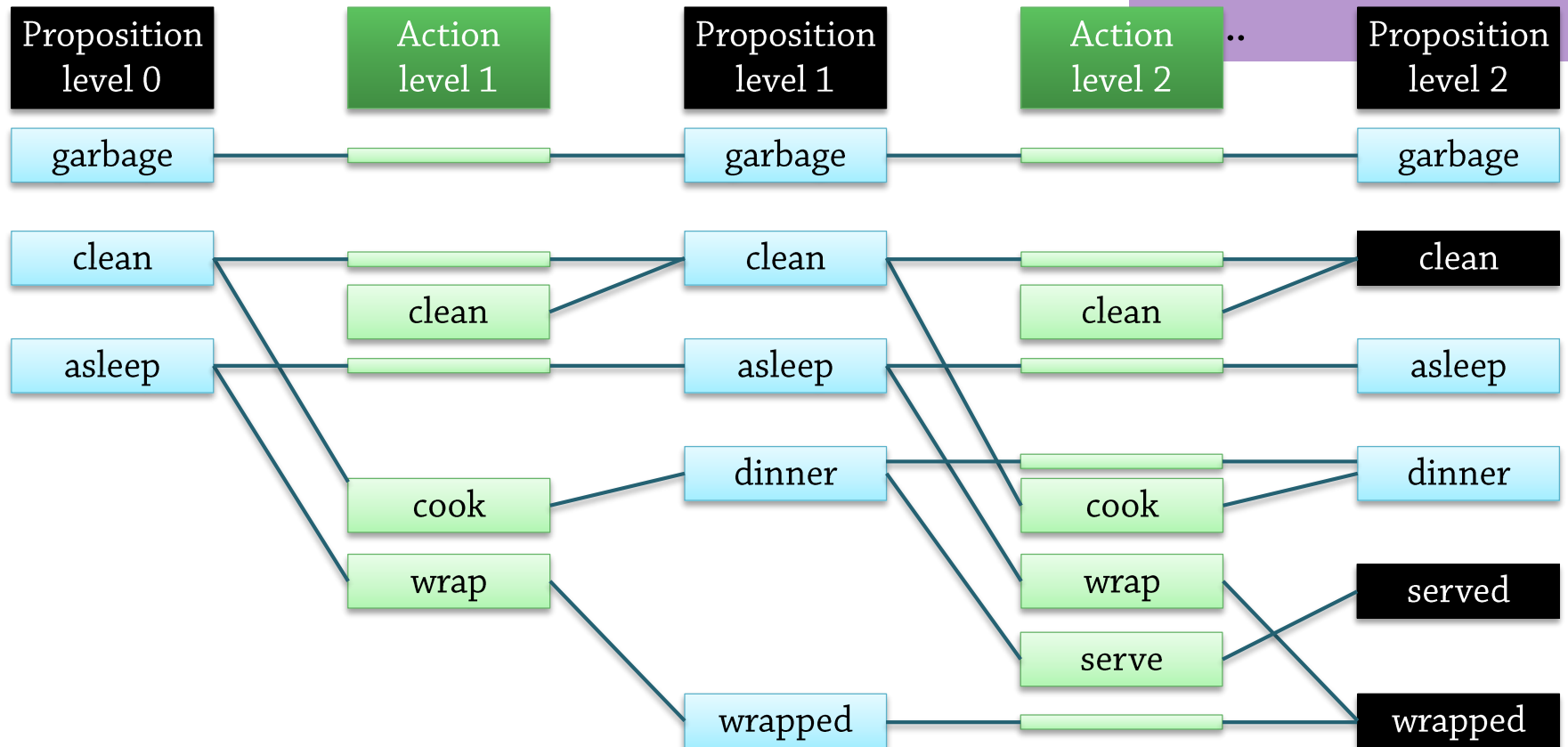
We need *dinner*
before serve

Level 1 is only for actions
whose preconds are true
at the start

Chains of dependencies
→
Many levels in the graph

- Let's add another level
 - Achieves all goals
 - Can select actions from the graph

<u>Action</u>	<u>Prec</u>	<u>Effects</u>
cook	clean	dinner
serve	dinner	served
wrap	asleep	wrapped
clean	–	clean



$g = \{\text{clean, served, wrapped}\}$

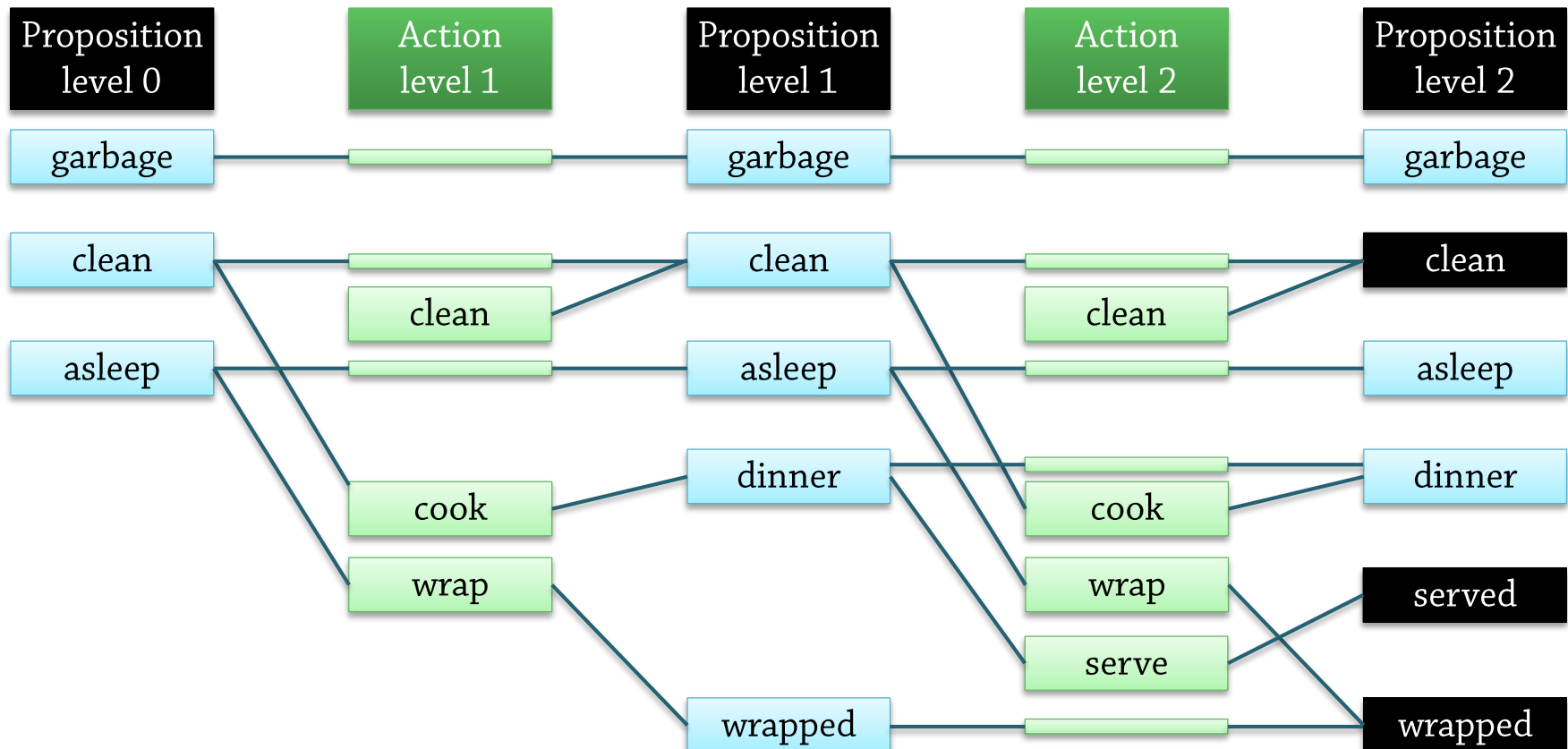
Heuristic Function: Based on Solution Extraction

Solution Extraction

- For each goal fact, choose one action achieving it

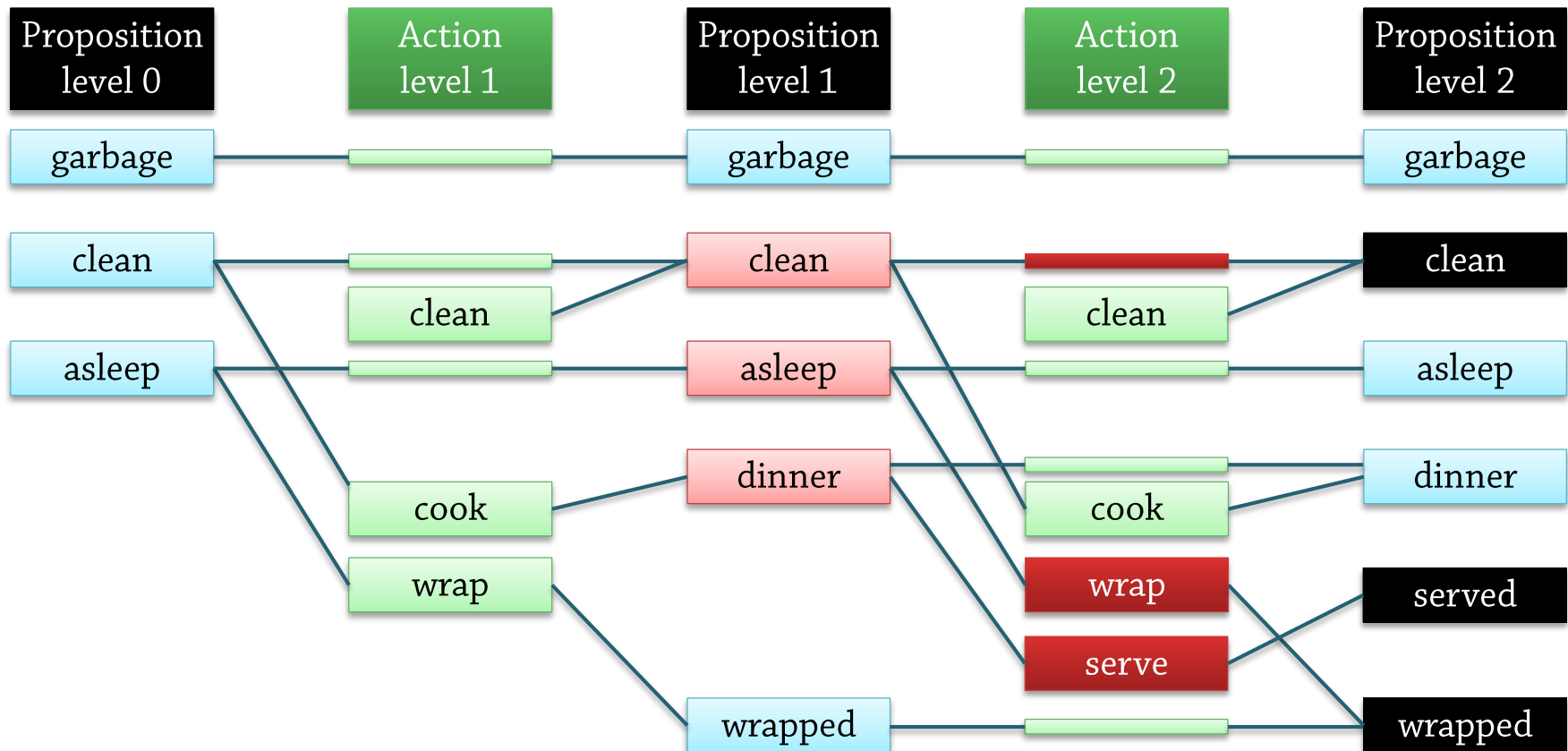
- clean \rightarrow noop-clean **or** clean
- served \rightarrow serve
- wrapped \rightarrow wrap **or** noop-wrapped

$2*1*2 = 4$ alternatives!
All work,
but some may result in
shorter plans... Why?



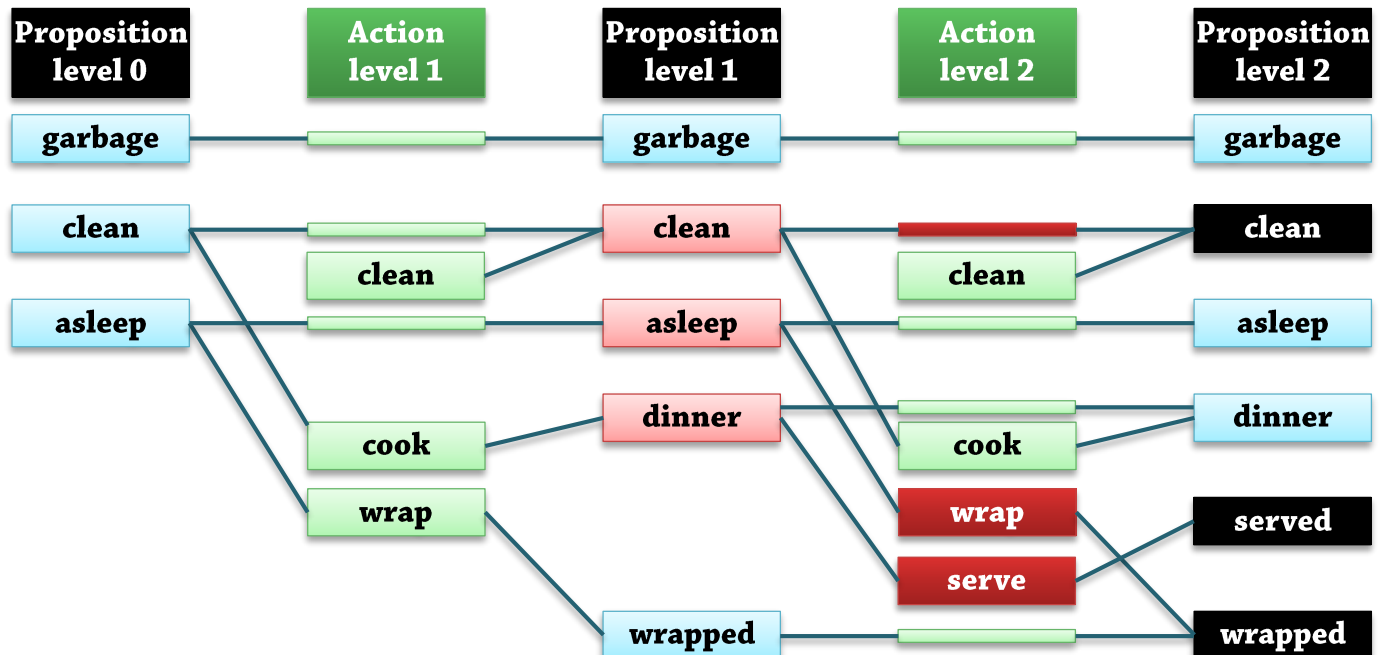
Solution Extraction (2)

- For all **selected** actions in level 2 (marked red):
 - Must first achieve their preconditions!
 - This is a new goal to achieve by selecting actions at level 1



Solution Extraction (3)

- Unlike backward search in **goal space**:
 - Simpler concept of relevance: No negative effects that interfere
 - At each level, select **sets** of actions, together achieving **all** goal facts
 - No need to consider "what the single selected action didn't achieve"
 - Simpler backward chaining: Instead of γ^{-1} , just conjoin preconds of selected actions
 - Already built a graph from the initial state
 - And no possibility of negative effect interference → we *can* reach the initial state

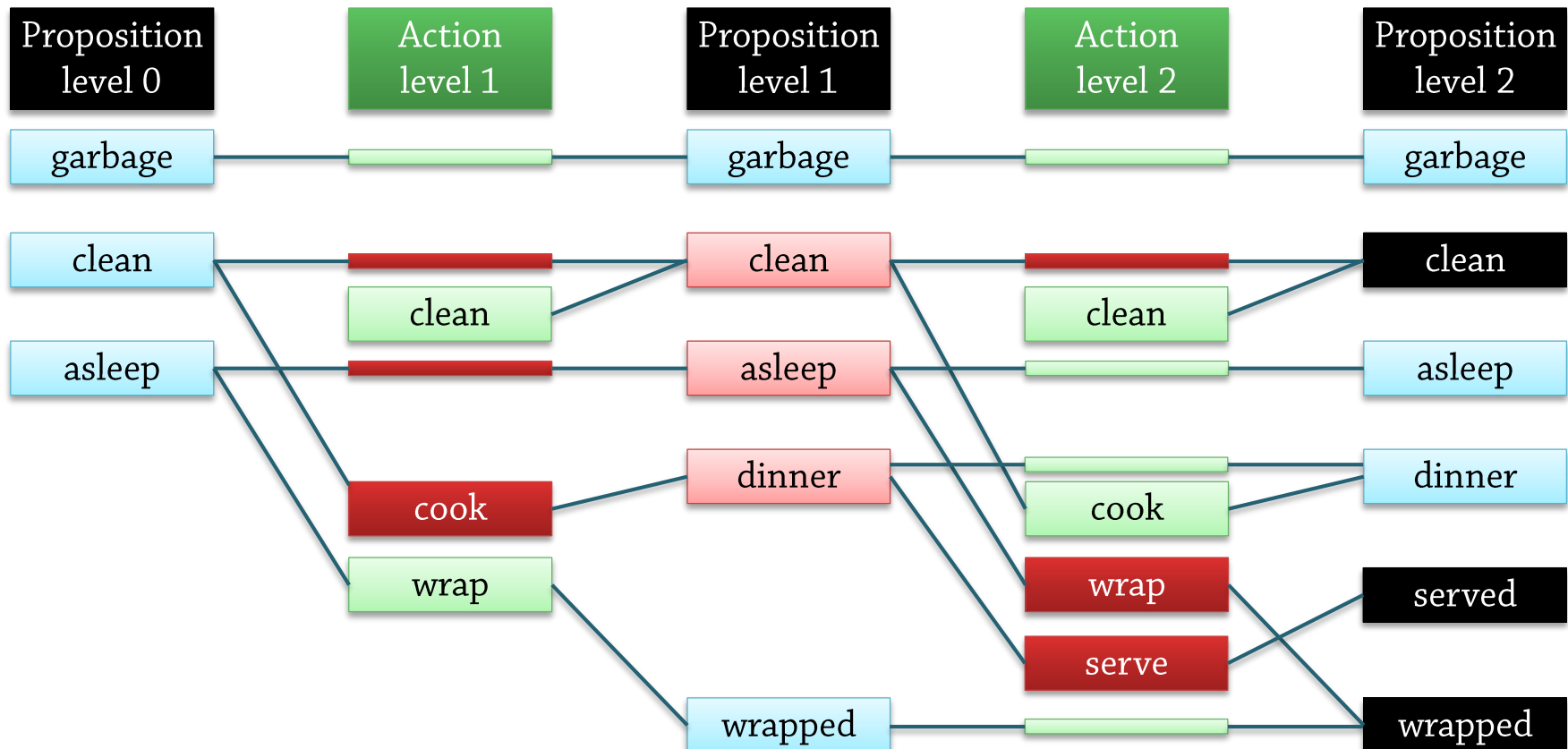


Solution Extraction (4)

- Final relaxed plan:

- First cook
- Then wrap and serve, in some order
- $h_{FF}(n) = 3$, assuming the algorithm chose this order!

Relaxed plan:
Not a solution to the **original** problem!



Solution Extraction (5)

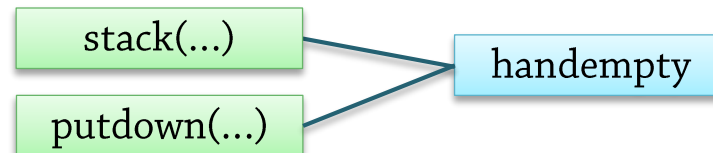
- Does the choice of actions matter?

- Choosing a noop action may mean fewer actual actions



- Different actions chosen at one level:

- May lead to different actions at previous levels
- Which then leads to different preconds to satisfy...



- And so on...

- Not equivalent to $h^+(n)$: Would require an **optimal** relaxed plan

- Would have to test different action selections
- May require additional **levels** (with fewer selected actions per level)

Actual solution
extraction algorithm
in FF
uses backward search
in the RPG
+ *heuristics*
for this search!

Properties of Relaxed Planning Graphs



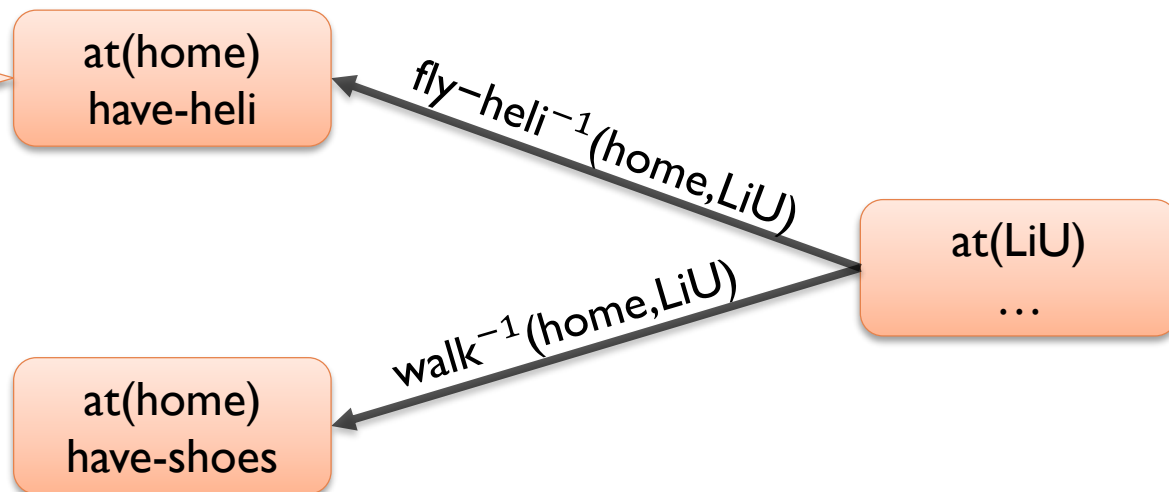
- The **relaxed planning graph** considers **positive** interactions
 - For example, when one action achieves multiple goals
 - Ignores **negative** interactions
- Can extract a **Graphplan-optimal** relaxed plan (minimal number of levels / "parallel" steps) in **polynomial** time

Original Inspiration: GraphPlan

BACKWARD SEARCH

- We know if the **effects** of an action can contribute to the goal
- Need **guidance** to determine which backward paths will lead to (good) solutions

Large search tree, no path to initial state?



One approach: Use heuristics. But other methods exist...

- Suppose that we could quickly determine:
 - **possibly-reachable**(s_0, s) – may state s be reachable from s_0 ?

Possibly reachable

Actually reachable
(not known
which ones!)

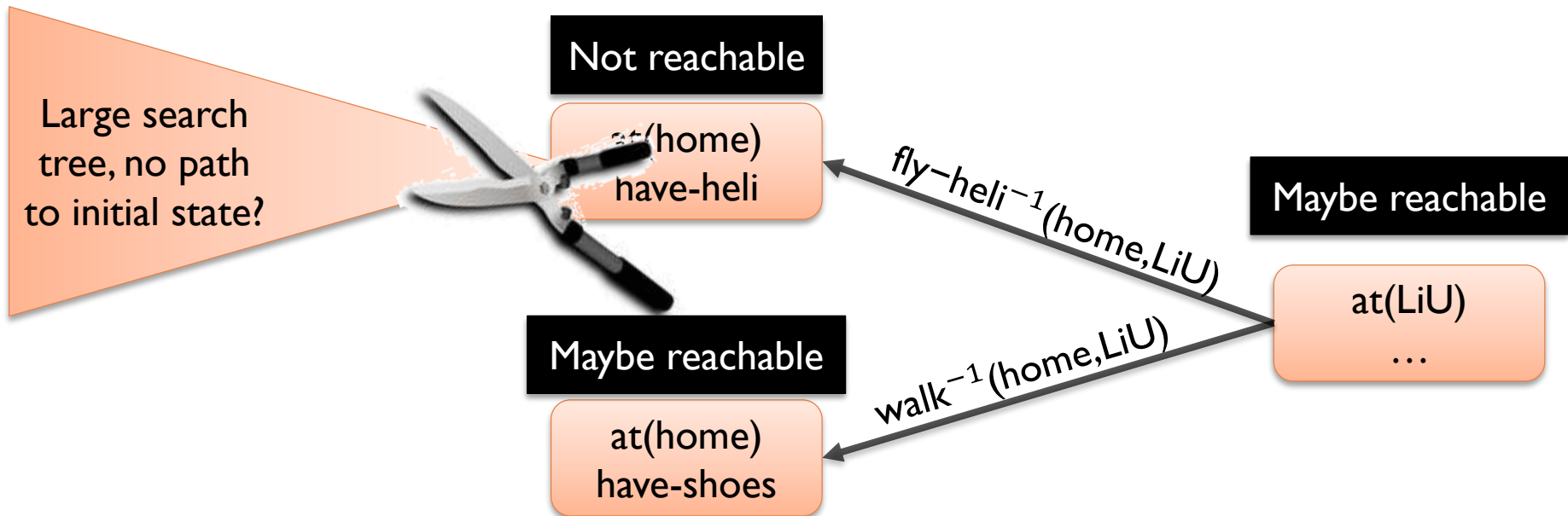
Unreachable...

Not (possibly reachable)

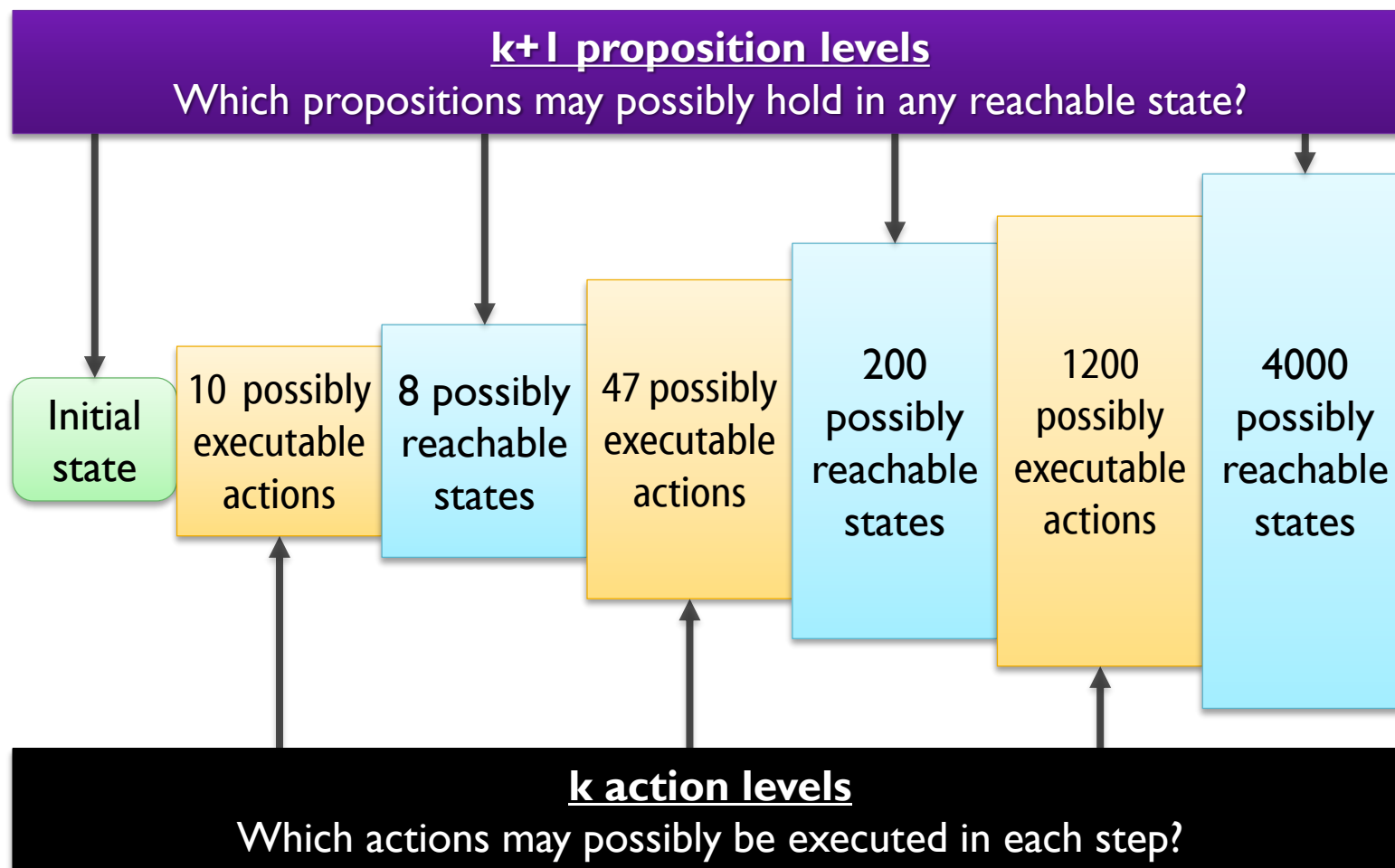
Definitely
unreachable...

Reachable States

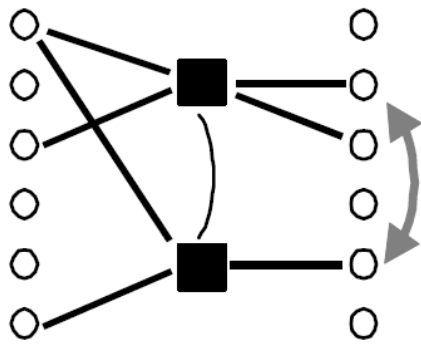
- Then we could **prune** many "fruitless branches":



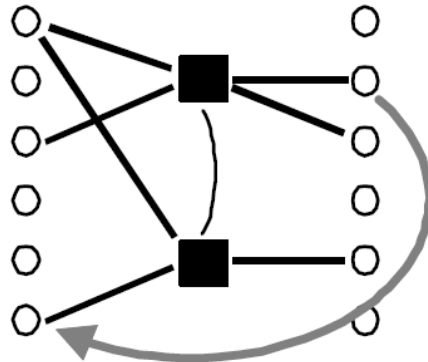
- A (non-relaxed) **Planning Graph**:
 - Useful to *generate states* – also useful in *backwards search*!



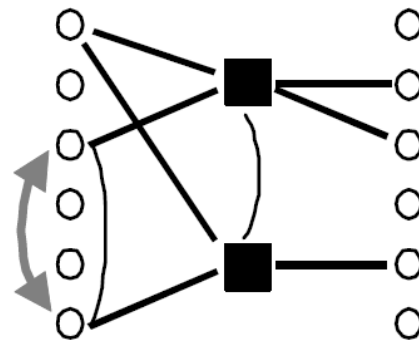
Negative Effects → Mutual Exclusion



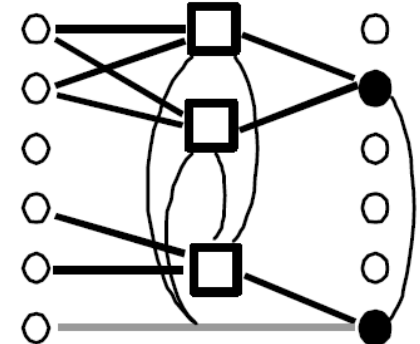
Inconsistent Effects



Interference



Competing Needs

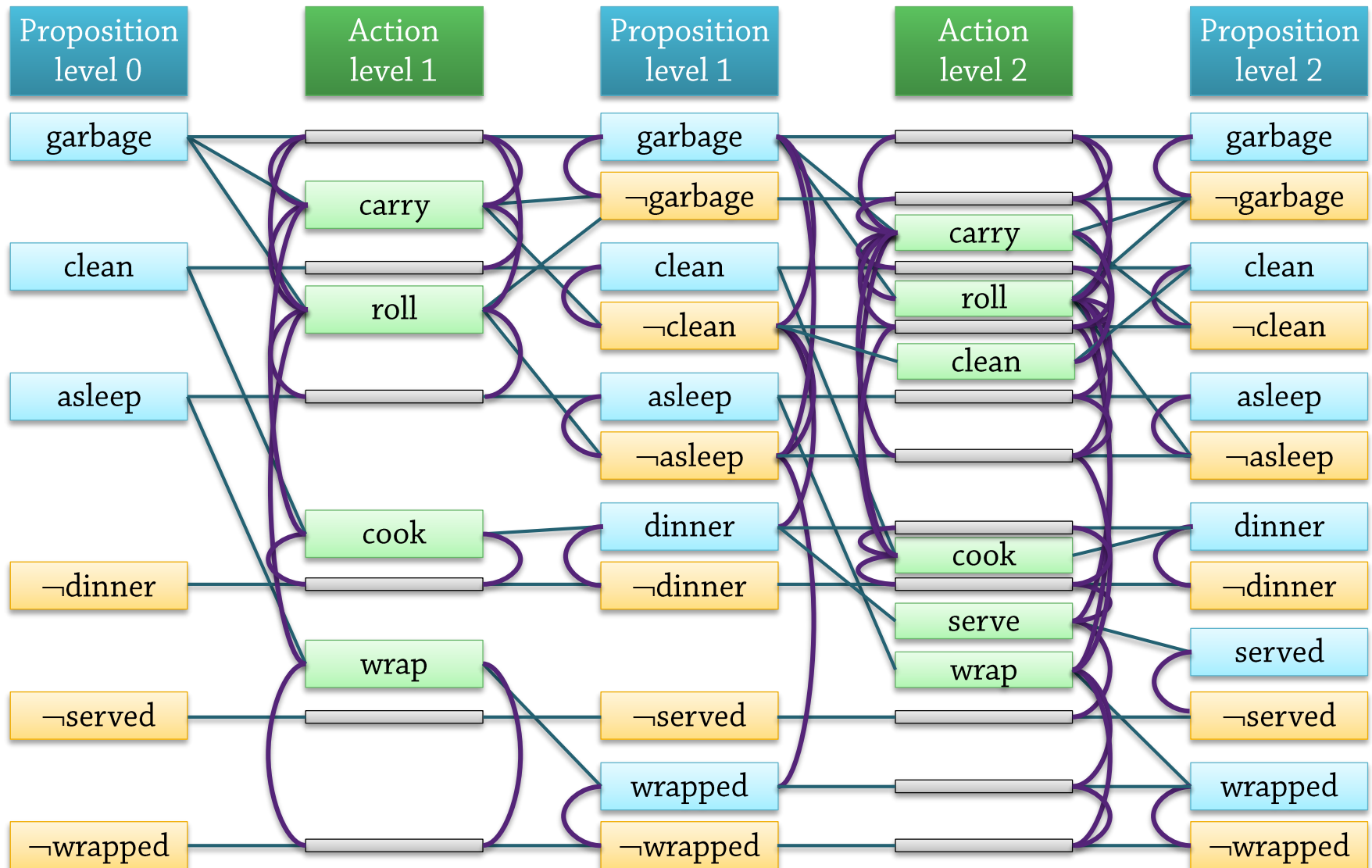


Inconsistent Support

- Two **actions** at the same action level are mutex (can't be selected together) if
 - *Inconsistent effects*: an effect of one negates an effect of the other
 - *Interference*: one deletes a precondition of the other
 - **Competing needs**: they have mutually exclusive preconditions (*not shown*)
- Otherwise:
 - Both might appear at the same time step in a solution plan
- Two **literals** at the same proposition level are mutex if
 - *Inconsistent support A*: one is the negation of the other,
 - *Inconsistent support B*: **all ways of achieving them are pairwise mutex**

Recursive propagation of mutexes

Example



All goal literals are present in level 2, and none of them are (known to be) mutex!