



# Automated Planning

## Domain-Configurable Planning: Planning with Control Formulas

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- Recall the fundamental assumption that we **only** specify
  - Structure: Objects and state variables
  - Initial state and goal
  - **Physical** preconditions and **physical** effects of actions

**We only specify what can be done**

**The planner should decide what should be done**

**But even the most sophisticated heuristics and domain analysis methods  
lack our intuitions and background knowledge...**

## How can we make a planner take advantage of what we know?

- Planners taking advantage of additional knowledge can be called:
  - Knowledge-rich
  - Domain-configurable
  - (Sometimes incorrectly called “domain-dependent”)

# Comparisons (1)

More effort

Higher  
performance

## Domain-specific

Must write an entire planner  
Can specialize the planner for very high performance

## Domain-configurable

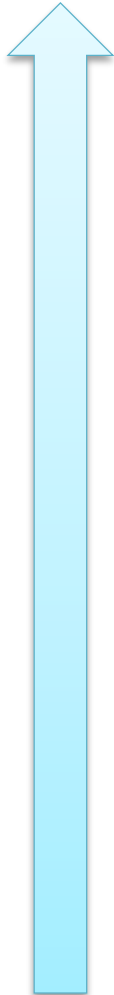
High-level (but sometimes complex) domain definition  
Can provide more information for high performance

## “Domain-independent”

Provide minimal information about actions  
Less efficient

# Comparisons (2)

Larger problem classes  
can be handled efficiently



## **Domain-configurable**

Easier to improve expressivity and efficiency  
→ Often practically useful for a larger set of domains!

## **“Domain-independent”**

Should be useful for a wide range of domains

## **Domain-specific**

Only works in a single domain

# **Domain-Configurable: Prioritization and Pruning**

# Two Kinds of Search Guidance (1)

**Prioritization:** Which part of a search tree should be visited first?  
Could use heuristic functions, could use other methods...

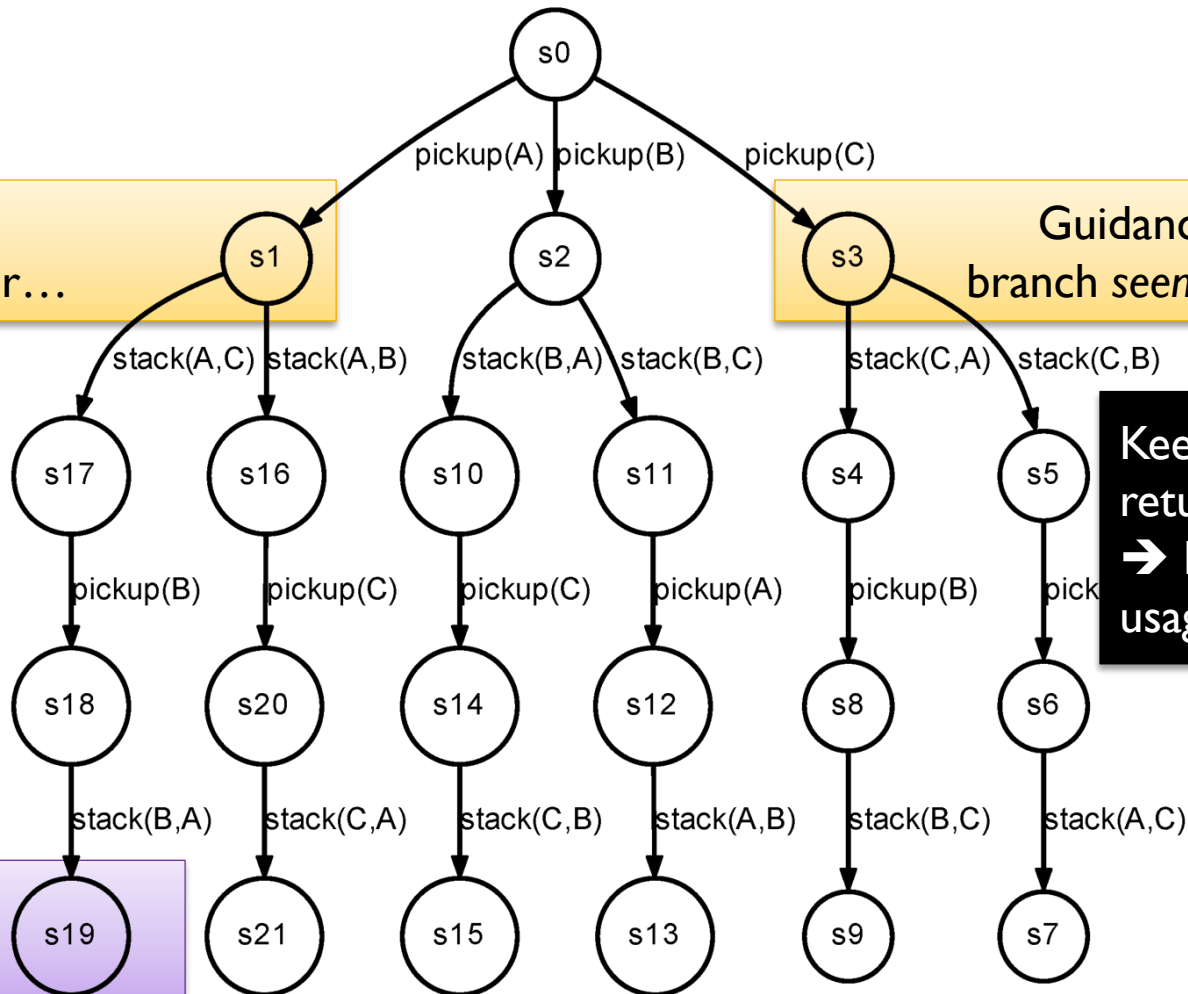
Guidance says: This branch seems better...

Go this way first

Guidance says: This branch seems worse...

Keep this, maybe return later  
→ high memory usage

Goal:  
B on C on A



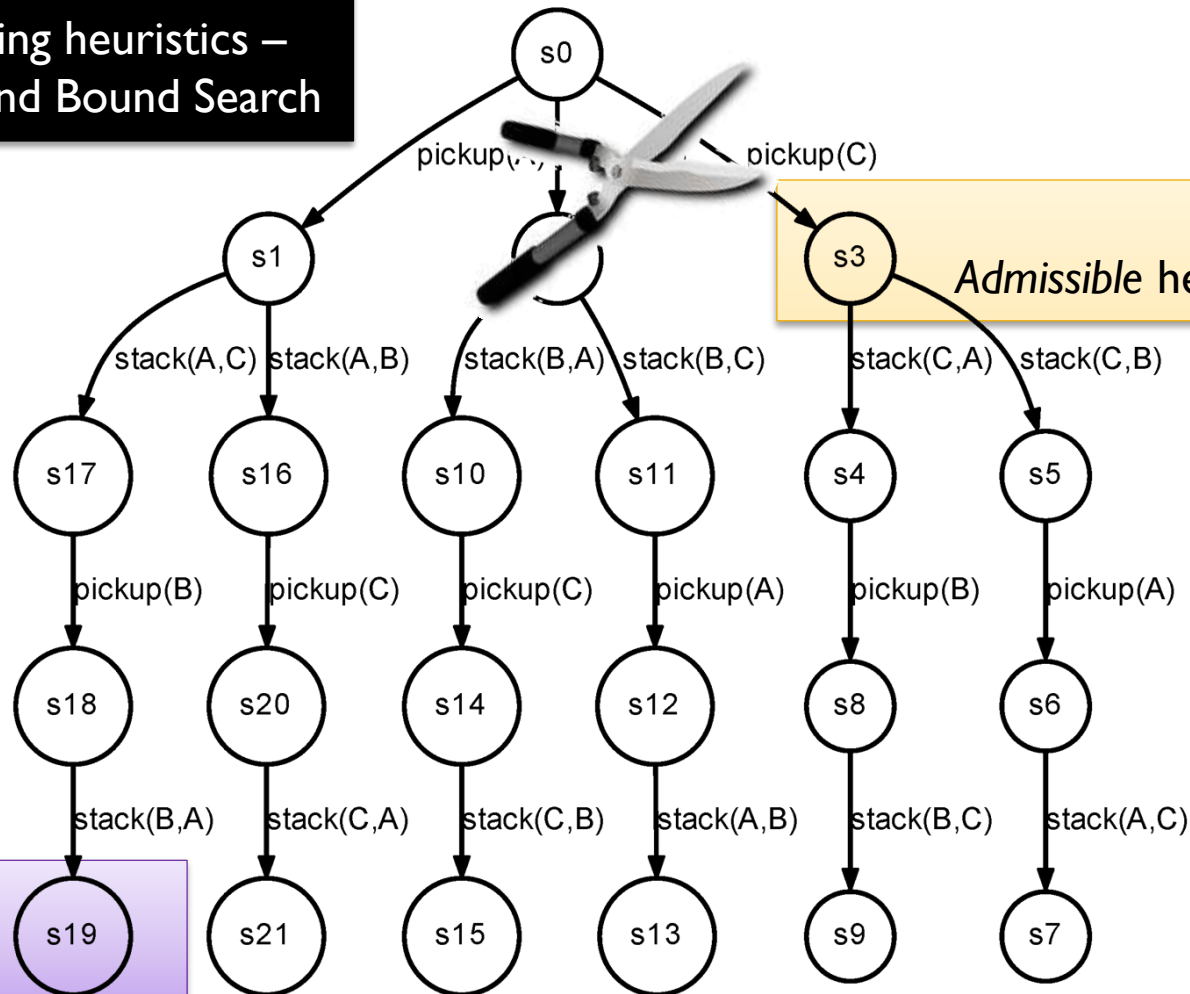
- Properties of prioritization:
  - We can always return to a node later
  - No need to be absolutely certain of your priorities
- This is why many domain-independent heuristics work well
  - Provide *reasonable* advice in *most* cases



# Two Kinds of Search Guidance (2)

**Pruning:** Which part of a search tree are definitely useless?  
Prune them!

Can be done using heuristics –  
example: Branch and Bound Search



Cost  $g(n)=1$   
Admissible heuristic  $h(n)=4$   
Any solution  
below  $s_3$   
will cost  
at least 5

**Prune!**  
Never  
consider the  
node or its  
descendants  
again...

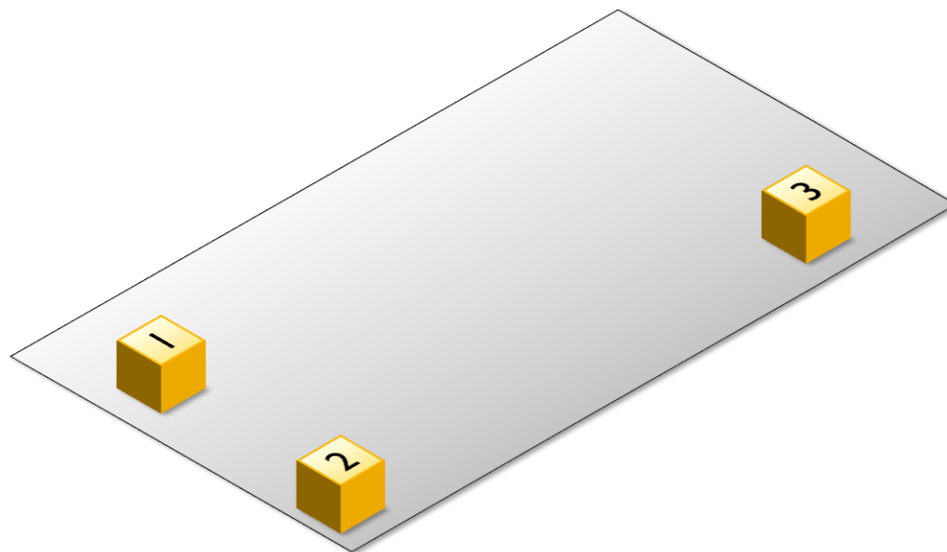
We found a  
solution of cost 4

- Can we prune when we search for the **first** solution?
  - A single mistake may *remove all paths to solutions*
  - → Difficult to find good *domain-independent* pruning criteria

# Example: Emergency Services Logistics

## ■ Emergency Services Logistics

- Goal: `at(crate1, loc1), at(crate2, loc2), at(crate3, loc3)`
- Now: `at(crate1, loc1), at(crate2, loc2)`



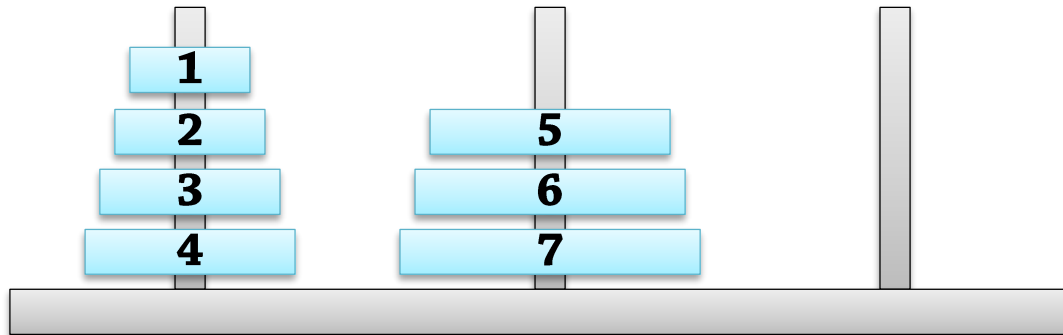
- Picking up crate1 again is **physically possible**
- It “destroys” `at(crate1, loc1)`, which is a goal – **obviously stupid!**

The **branch** beginning with `pickup(crate1)` could be **pruned** from the tree!  
How do we **detect** this in a domain-independent way?

# Example: Towers of Hanoi

Should we always prevent the destruction of achieved goals?

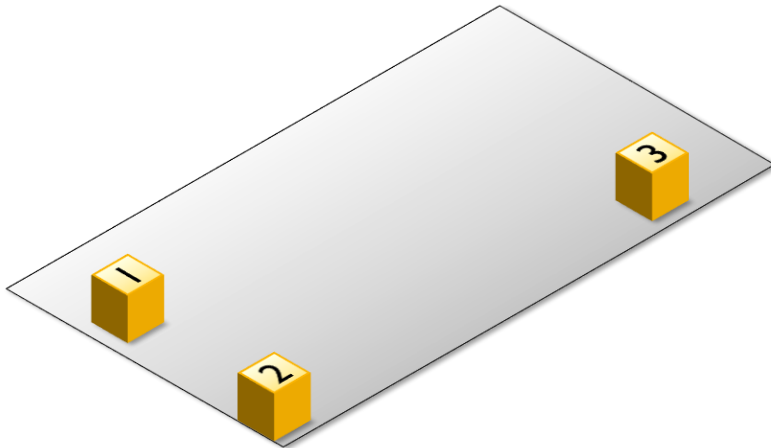
- Goal: on(1,2), on(2,3), on(3,4), on(4,5), on(5,6), on(6,7)
- Now: on(1,2), on(2,3), on(3,4), on(5,6), on(6,7)



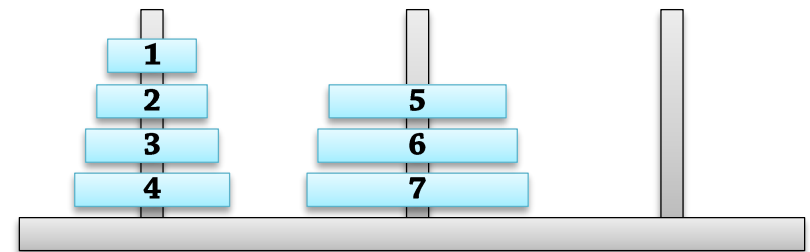
- Moving disk 1 to the third peg is possible but “destroys” a goal fact: on(1,2)
  - Is this also obviously stupid?
  - No, it is necessary! Disk 1 is blocking us from moving disk 4...

→ Heuristics may or may not detect:

Picking up crate 1 is bad



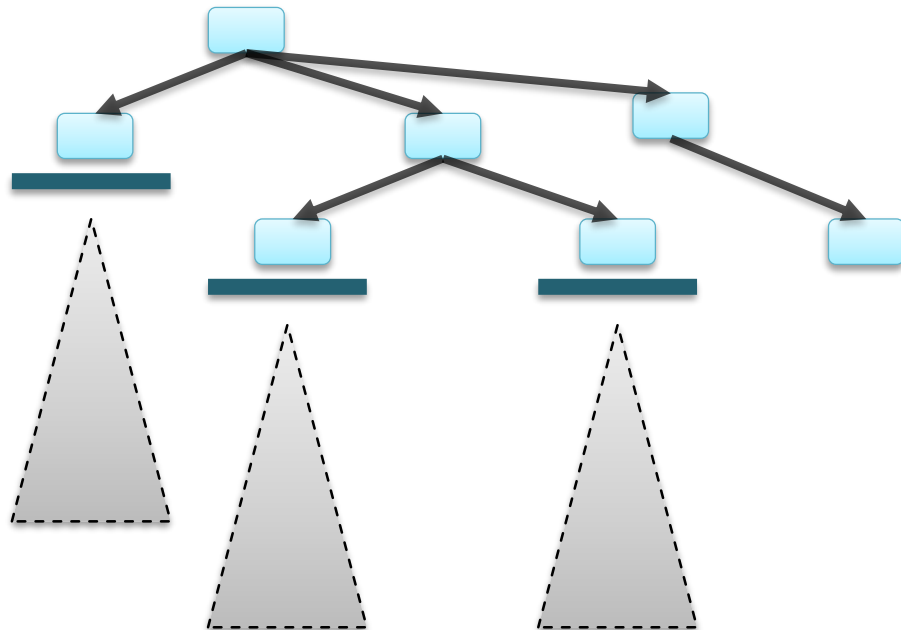
Moving disk 1 is good



Will generally depend on the entire state  
+ which alternative states exist,  
not just the fact that you "destroy goal achievement"

Might delay investigating either alternative for a while,  
return to try this later

- With a **domain-configurable planner**:
  - We *could* provide *domain-specific heuristics*
    - Strongly discouraging the destruction of goals in Emergency Services Logistics
    - Would keep the *option* to investigate such actions later (not necessary!)
  - We can directly provide stronger domain-specific **pruning criteria**



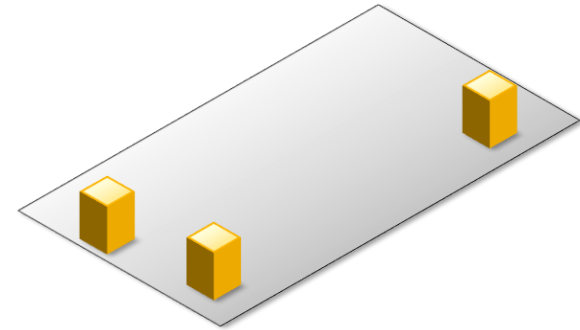
# Planning with Control Formulas

- **Control formulas**: One way of specifying when to prune
  - Motivation
  - Examples
  - Formalism
  - Evaluation of control formulas



## Simplest control information: Precondition Control

- **operator** `pickup(robot, crate, location)`
  - **precond:**
    - `at(robot, location), at(crate, location)`
    - `handempty(robot)`
    - ...and **the goal doesn't require that crate should end up at location!**



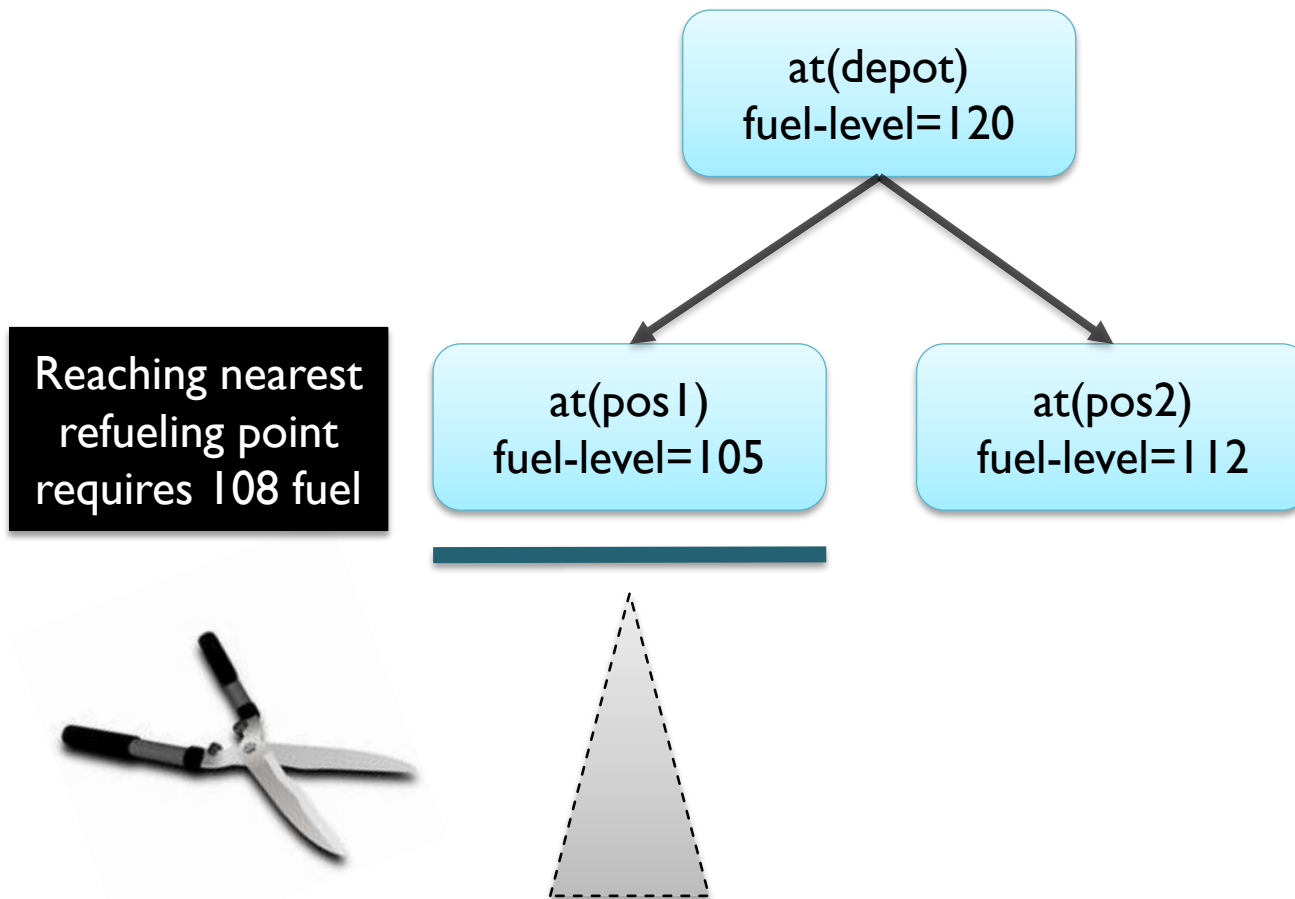
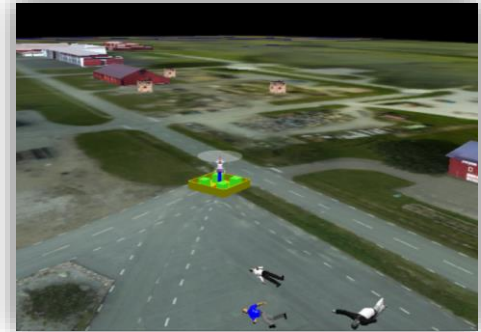
How to express this, given that the goal requires `at(crate, loc)`?

- Alternative 1: **New predicate** "`destination(crate, loc)`"
  - *Duplicates* the information already specified in the goal
  - **precond:** `¬destination(crate, location)`
- Alternative 2: **New language extension** "`goal( $\phi$ )`"
  - Evaluated in the set of goal states, not in the current state
  - **precond:** `¬goal(at(crate, location))`

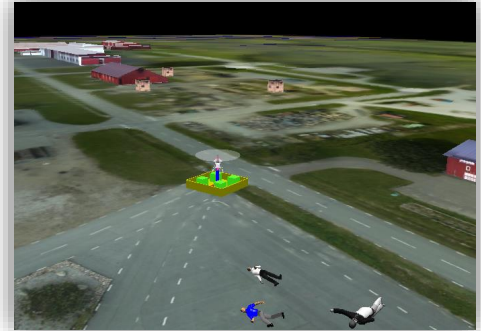
Supported by  
all planners

Requires  
extensions, but  
more convenient

- A UAV should never be where it **can't reach** a refueling point
  - Can't possibly extend such plans into solutions



- A UAV should never be where it **can't reach** a refueling point
  - If this happens in a plan, we can't possibly extend it into a solution satisfying the goal
- How to express this?



## Using preconditions again?

Must be verified for **every** action:  
fly, scan-area, take-off, ...

Must be checked even when  
the UAV is idle, hovering

Inconvenient!

## Using state constraints?

Defined **once**,  
applied to **every generated state**

```

$$\forall(u: \text{uav}) [$$

$$\quad \exists(rp: \text{refueling-point}) [$$

$$\quad \quad \text{dist}(u, rp) * \text{fuel-usage}(u) < \text{fuel-avail}(u)$$

$$\quad ]$$

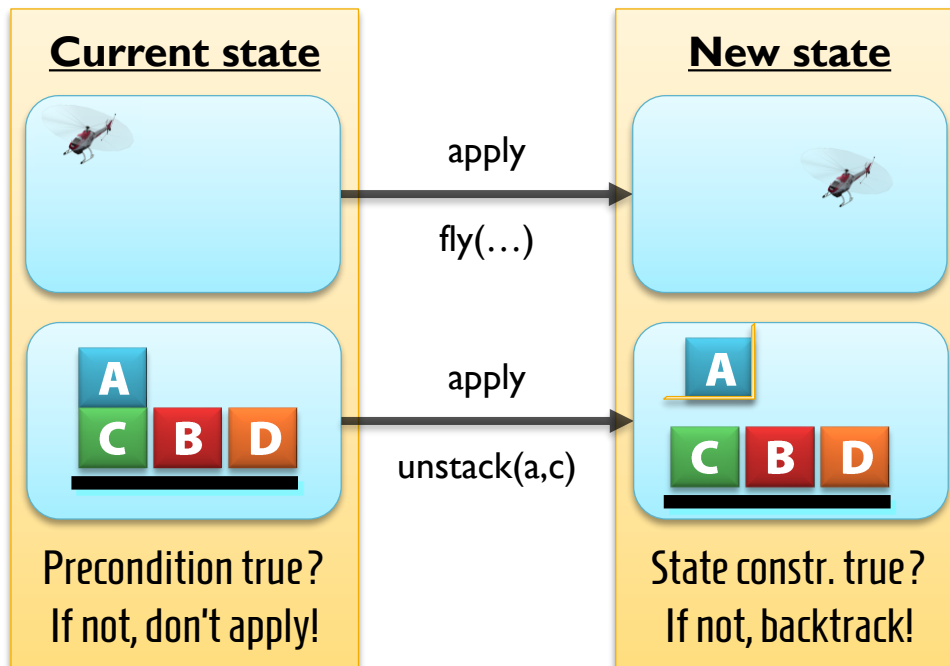
$$]$$

```

Comparatively simple extension!

# Testing State Constraints

- Testing such state constraints is simple
  - Apply an action → new state is generated
    - Formula false in that state → Prune!
  - Similar to preconditions
    - But tested in the state after an action is applied, not before!



# Temporal Conditions (1)

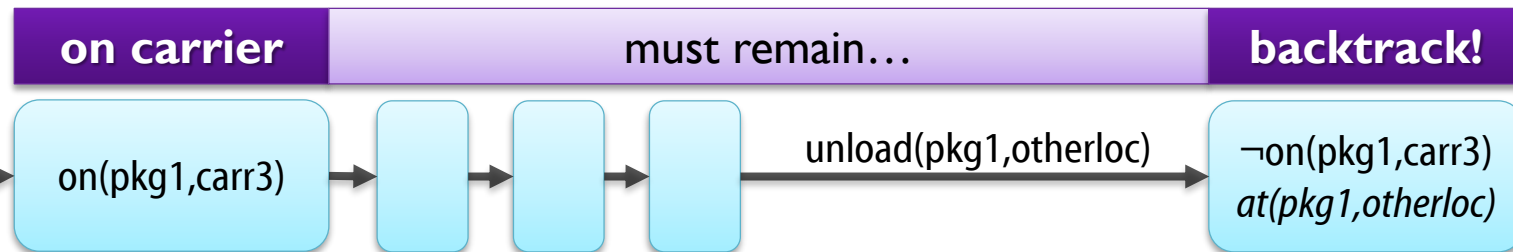
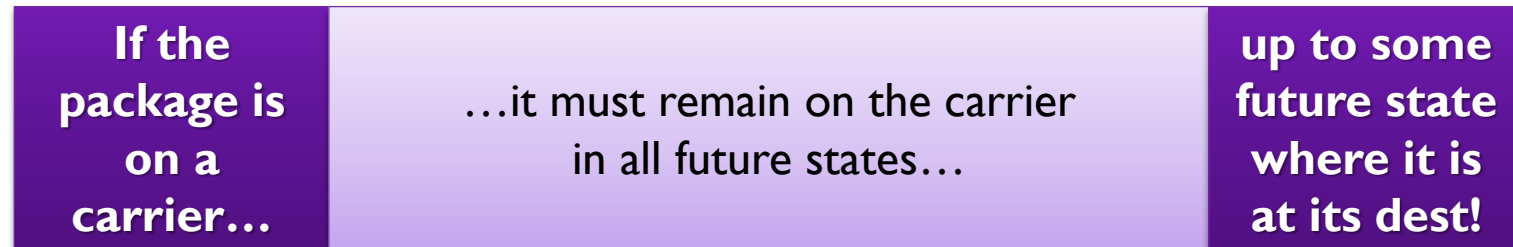
- A package on a carrier should **remain there** until it reaches its destination
  - For any plan  $\pi$  where we move it prematurely, there is a more efficient plan  $\pi'$  where we don't

How to express this as a single formula?



# Temporal Conditions (2)

- “A package on a carrier should **remain** there **until** it reaches its destination”

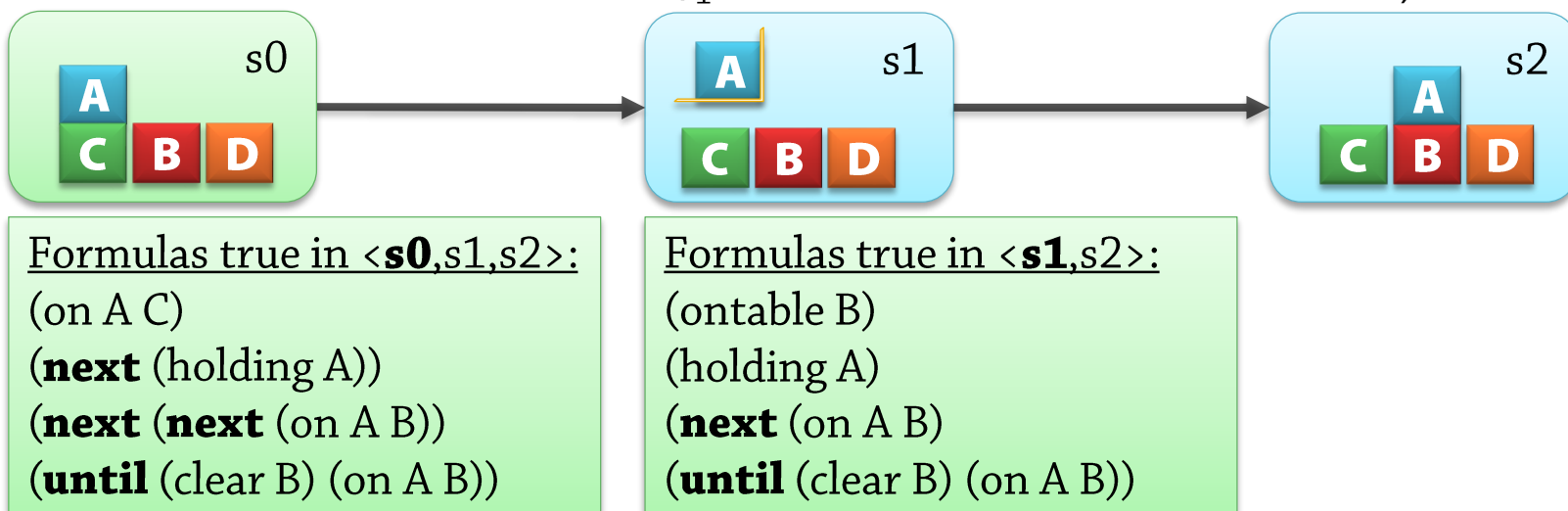


We need a formula constraining an entire **state sequence**, not a single state!

In planning, this is called a **control formula** or **control rule**

## We need to extend the logical language!

- One possibility: Use **Linear Temporal Logic** (as in TLplan)
  - All formulas evaluated relative to a *state sequence* and a *current state*
  - Assuming that  $f$  is a formula:
    - $\bigcirc f$  – (**next**  $f$ )  $f$  is true in the next state
    - $\Diamond f$  – (**eventually**  $f$ )  $f$  is true either now **or** in some future state
    - $\Box f$  – (**always**  $f$ )  $f$  is true now **and** in all future states
    - $f_1 \cup f_2$  – (**until**  $f_1 f_2$ ) ( $f_2$  is true now), **or** ( $f_2$  is true in some future state  $s'$  and  $f_1$  is true in all states until/before then)



- “A package on a carrier should remain there until it reaches its destination”

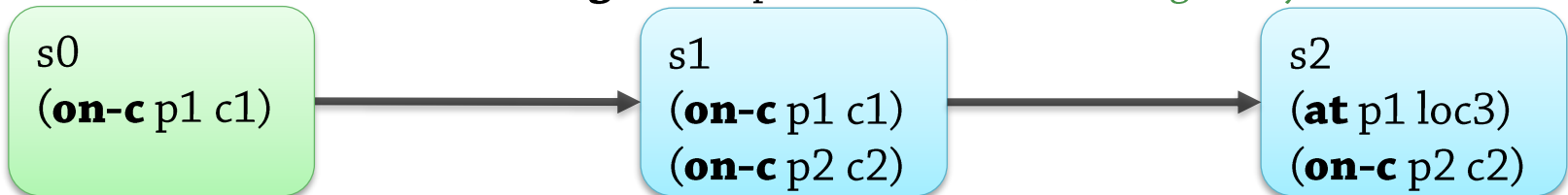
(forall (?var) (type-predicate ?var)  $\phi$ ):  
 $\forall v. \text{type-predicate}(v) \rightarrow \phi$   
For all values of ?var that satisfy type-predicate,  $\phi$  must be true

- (always  
    (**forall** (?c) (carrier ?c)                   ;; For all carriers  
      (**forall** (?p) (package ?p)               ;; For all packages  
        (**implies**  
          (on-carrier ?p ?c)               ;; If the package is on the carrier  
          (**until** (on-carrier ?p ?c)       ;; ...then it remains on the carrier  
              (**exists** (?loc)               ;; until there exists a location  
                (at ?p ?loc)               ;; where it is, and  
                (**goal** (at ?p ?loc))))   ;; where the goal says it should be  
          ))))  
    ))))  
■ Should be true starting in the initial state



# Control Formula

- **(always**  
    **(forall** (?c) (carrier ?c)                   ;; For all carriers  
    **(forall** (?p) (package ?p)                ;; For all packages  
    **(implies**  
        (on-carrier ?p ?c)                   ;; If the package is on the carrier  
        **(until** (on-carrier ?p ?c)           ;; ...then it remains on the carrier  
            **(exists** (?loc)                ;; until there exists a location  
                (at ?p ?loc)               ;; where it is, and  
                **(goal** (at ?p ?loc))))   ;; where the goal says it should be



always  
→  
time 0

p1 on c1 here

Remains on c1 until at its destination

always  
→  
time 1

p1 on c1 here

p2 on c2 here

Until at its dest

Until at its dest

always  
time 2

p2 on c2 here ...

# Finding Control Formulas

- How do we come up with good control rules?
  - Good starting point: "Don't be stupid!"
  - Trace the search process – suppose the planner tries this:



- Placing F on top of B is stupid, because we'll have to remove it later
  - Would have been better to put F on the table!
- Conclusion: Should not extend a good tower the wrong way
  - *Good tower*: a tower of blocks that will never need to be moved

# Blocks World Example (continued)

- Rule 1: Every goodtower must always remain a goodtower
  - **(forall** (?x) (clear ?x) ;; For all blocks that are clear (at the top of a tower)  
    **(implies**  
        (goodtower ?x) ;; If the tower is good (no need to move any blocks)  
        **(next** (or ;; ...then in the next state, either:  
            (clear ?x) ;; ?x remains clear (didn't extend the tower)  
            **(exists** (?y) (on ?y ?x) ;; or there is a block ?y which is on ?x  
                            (goodtower ?y)) ;; which is a goodtower  
        )))

s0

s1

s2

s3

goodtower(x)? → clear(x) or  
goodtower(y)

What about the rest?

# Blocks World Example (continued)

## ■ Rule 1, second attempt:

### ■ (always

**(forall** (?x) (clear ?x) ;; For all blocks that are clear (at the top of a tower)

### **(implies**

(goodtower ?x) ;; If the tower is good (no need to move any blocks)

**(next** (or ;; ...then in the next state, either:

(clear ?x) ;; ?x remains clear (didn't extend the tower)

**(exists** (?y) (on ?y ?x) ;; or there is a block ?y which is on ?x

(goodtower ?y)) ;; which is a goodtower

))))

s0

s1

s2

s3

goodtower(x)? → clear(x) or  
goodtower(y)

goodtower(x)? → clear(x) or  
goodtower(y)

goodtower(x)? → clear(x) or

# Supporting Predicates

- Some planners allow us to **define** a predicate recursively

- goodtowerbelow**(x) means we **will not have to move** x

$$\text{goodtowerbelow}(x) \Leftrightarrow [\text{ontable}(x) \wedge \neg \exists [y: \mathbf{GOAL}(\text{on}(x,y))]]$$

∨

$$\begin{aligned} & \exists [y: \text{on}(x,y)] \{ \\ & \quad \neg \mathbf{GOAL}(\text{ontable}(x)) \wedge \\ & \quad \neg \mathbf{GOAL}(\text{holding}(y)) \wedge \\ & \quad \neg \mathbf{GOAL}(\text{clear}(y)) \wedge \\ & \quad \forall [z: \mathbf{GOAL}(\text{on}(x,z))] (z = y) \wedge \\ & \quad \forall [z: \mathbf{GOAL}(\text{on}(z,y))] (z = x) \wedge \\ & \quad \text{goodtowerbelow}(y) \end{aligned}$$

}



goodtowerbelow: B, C, H

X is on the table,  
and shouldn't be on anything else

X is on something else

Shouldn't be on the table,  
shouldn't be holding it,  
shouldn't be clear

If x should be on z, then it is (z is y)

If z should be on y, then it is (z is x)

The remainder of the tower is also good



# Supporting Predicates

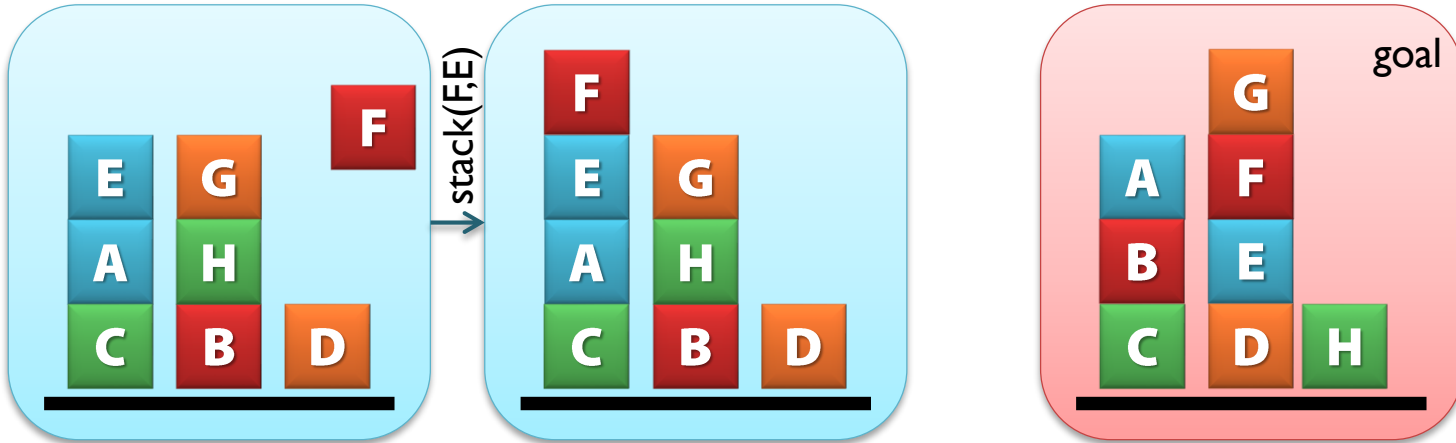
- **goodtower**(x) means x is the block at the top of a good tower
  - $goodtower(x) \Leftrightarrow clear(x) \wedge \neg GOAL(holding(x)) \wedge goodtowerbelow(x)$
- **badtower**(x) means x is the top of a tower that isn't good
  - $badtower(x) \Leftrightarrow clear(x) \wedge \neg goodtower(x)$



goodtower: B  
goodtowerbelow: B, C, H  
badtower: G, E  
(neither: D, A)



## ■ Step 2: Is this stupid?



- Placing **F on top of E** is stupid, because we have to move E later...
  - Would have been better to put F on the table!
  - But E was not a goodtower, so the previous rule didn't detect the problem
- Never put anything on a badtower!
  - (always
    - (forall (?x) (clear ?x) ;; For all blocks at the top of a tower
    - (implies
      - (badtower ?x) ;; If the tower is bad (must be dismantled)
      - (next (not (exists (?y) (on ?y ?x)))))) ;; Don't extend it!



## ■ Step 3: Is this stupid?



## ■ Picking up F is stupid!

- It is on the table, so we can wait until its destination is ready:



- (always

(**forall** (?x) (clear ?x) ;; For all blocks at the top of a tower

(**implies**

(**and** (ontable ?x)

(exists (?y) (goal (on ?x ?y)) (not (goodtower ?y))))

(**next** (not (holding ?x))))))

# Pruning using Control Formulas

# Pruning using Control Formulas



- How do we decide when to prune the search tree?
  - Obvious idea:
    - Take the state sequence corresponding to the current action sequence
    - Evaluate the formula over that sequence
    - If it is false: Prune / backtrack!

## ■ Problem:

### ■ (always

(**forall** (?c) (carrier ?c)

;; For all carriers

(**forall** (?p) (package ?c)

;; For all packages

(**implies**

(on-carrier ?p ?c)

;; If the package is on the carrier

(**until** (on-carrier ?p ?c)

;; ...then it remains on the carrier

(**exists** (?loc)

;; until there exists a location

(at ?p ?loc)

;; where it is, and

(**goal** (at ?p ?loc))))

;; where the goal says it should be

))))

No package on a carrier  
in the initial state:  
Everything is OK



s0

**"Every boat I own  
is a billion-dollar yacht  
(because I own zero boats)"**

## ■ Problem:

### ■ (always

(**forall** (?c) (carrier ?c)

;; For all carriers

(**forall** (?p) (package ?c)

;; For all packages

(**implies**

(on-carrier ?p ?c)

;; If the package is on the carrier

(**until** (on-carrier ?p ?c)

;; ...then it remains on the carrier

(**exists** (?loc)

;; until there exists a location

(at ?p ?loc)

;; where it is, and

(**goal** (at ?p ?loc))))

;; where the goal says it should be

))))

When we add an action  
placing a package  
on a carrier...

...there is no future state  
where the package is  
at its destination!

s0

s1  
(on-carrier p4 c4)

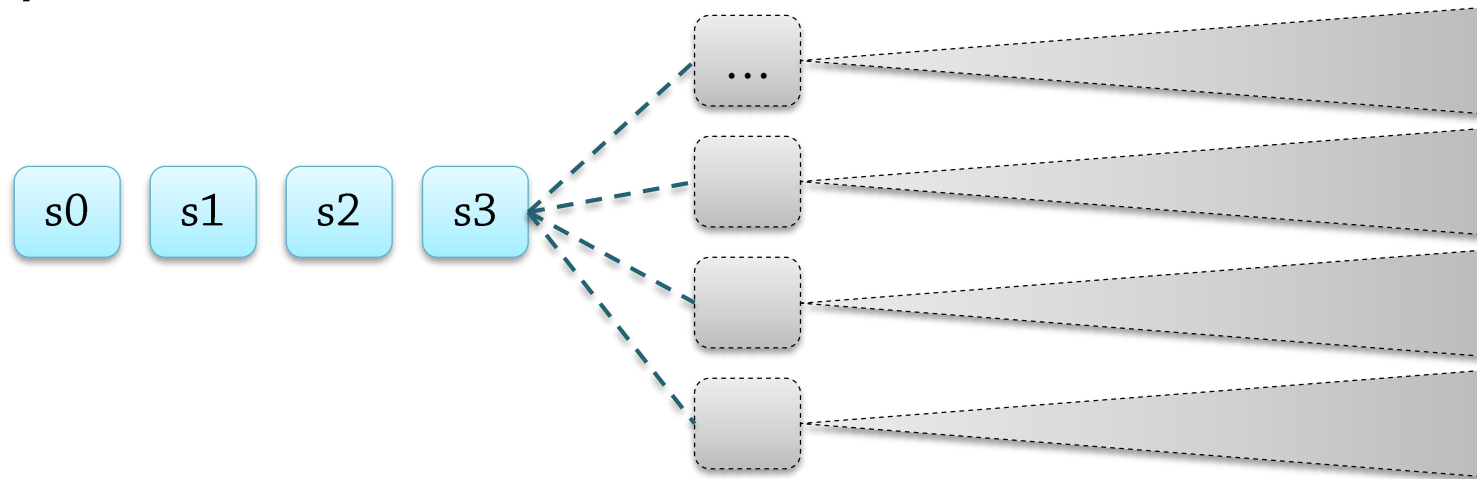
The formula is violated,  
but only because the solution is not *complete* yet!  
We must be allowed to continue,  
generating new states...

# Evaluation 3: What's Wrong?



- We had an obvious idea:
  - Take the state sequence corresponding to the current plan
  - Evaluate the formula over that sequence
  - If it is false: Prune / backtrack!
- This is actually wrong!
  - Formulas should hold in the state sequence of the solution
  - But they don't have to hold in every intermediate action sequence...

## ■ Analysis:



We have applied some actions, yielding a sequence of states

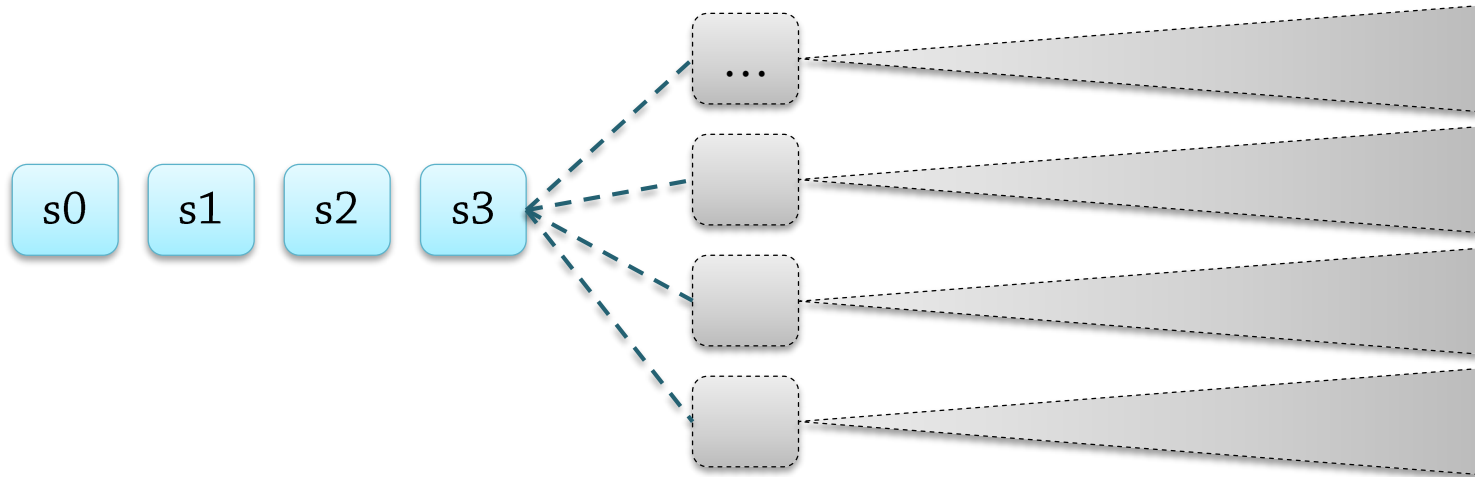
We intend to generate additional actions and states, but right now we don't know which ones

The control formula should be satisfied by the entire state sequence corresponding to a solution

We only know some of those states

Should only backtrack if we can prove that you can't find additional states so that the control formula becomes true

## ■ Analysis 2:



The control formula should be satisfied  
by the entire state sequence corresponding to a solution

Evaluate those **parts** of  
the formula that refer to  
known states

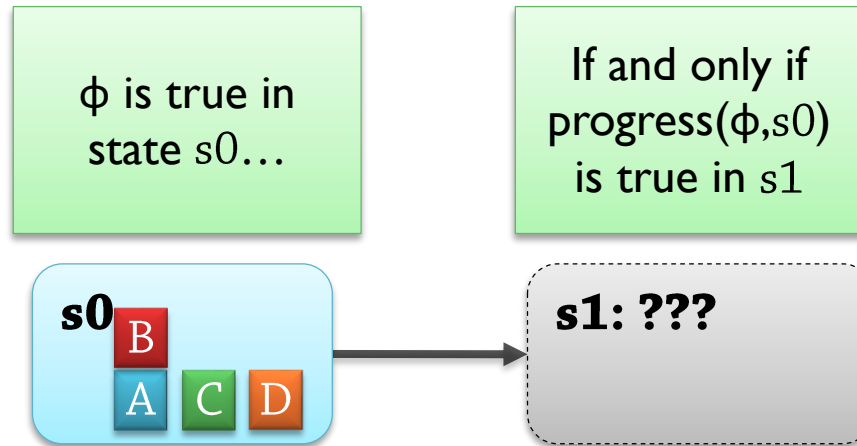
**Leave** other parts of the formula  
to be evaluated later

If the result can be proven to be **FALSE**, then backtrack



# Progressing Temporal Formulas (1)

- We use formula progression
  - We progress a formula  $\Phi$  through a single state  $s$  at a time
    - First the initial state, then each state generated by adding an action
  - The result is a new formula
    - Containing conditions that we must "postpone", evaluate starting in the next state



# Progressing Temporal Formulas (2)

- More intuitions?

- Suppose you are reading a book. A *page* is analogous to a *state*.

"The figure appears 5 pages from here"  
is true on page 7



"The figure appears 4 pages from here"  
is true on page 8

"Fig 1 appears 3 pages from here  
and fig 2 appears 5 pages from here"  
is true on page 7



"Fig 1 appears 2 pages from here  
and fig 2 appears 4 pages from here"  
is true on page 8

"Starting where I am now,  
there's a figure on every page"  
is true on page 7



There actually is a figure on page 7, and  
"Starting where I am now,  
there's a figure on every page"  
is true on page 8

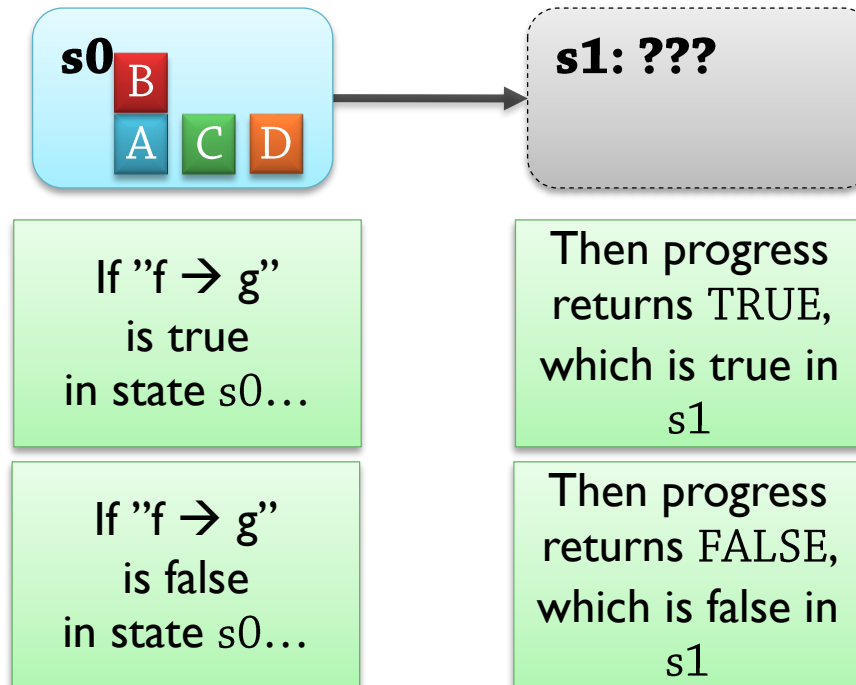
"If there's a figure on this page,  
there is no figure on the next page  
[otherwise I don't care]"  
is true on page 7



Check if there is a figure on this page.  
If so:  $f = \text{"There's no figure on this page"}$ .  
Otherwise:  $f = \text{"true"}$ .  
Check whether  $f$  is true on page 8.

# Progressing Temporal Formulas (3)

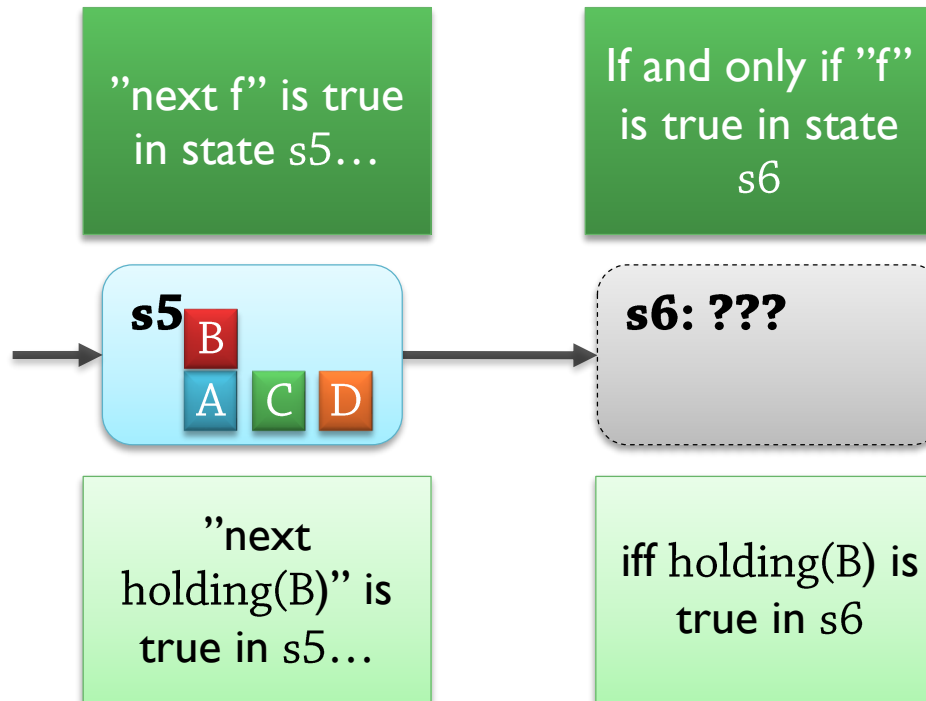
- Base case: Formulas **without** temporal operators (“ $\text{on}(A,B) \rightarrow \text{on}(C,D)$ ”)
  - Must be true **here**, in **this** state
  - $\text{progress}(\Phi, s) = \text{TRUE}$  if  $\Phi$  holds in  $s$  (we already know how to test this)
  - $\text{progress}(\Phi, s) = \text{FALSE}$  otherwise



# Progressing Temporal Formulas (4)

## ■ Simple case: next

- $\text{progress}(\text{next } f, s) = f$ 
  - Because "next  $f$ " is true in this state iff  $f$  is true in the next state
  - This is by definition what  $\text{progress}()$  should return!



Additional cases are discussed in the book (always, eventually, until, ...)

# Progression in Depth First Search

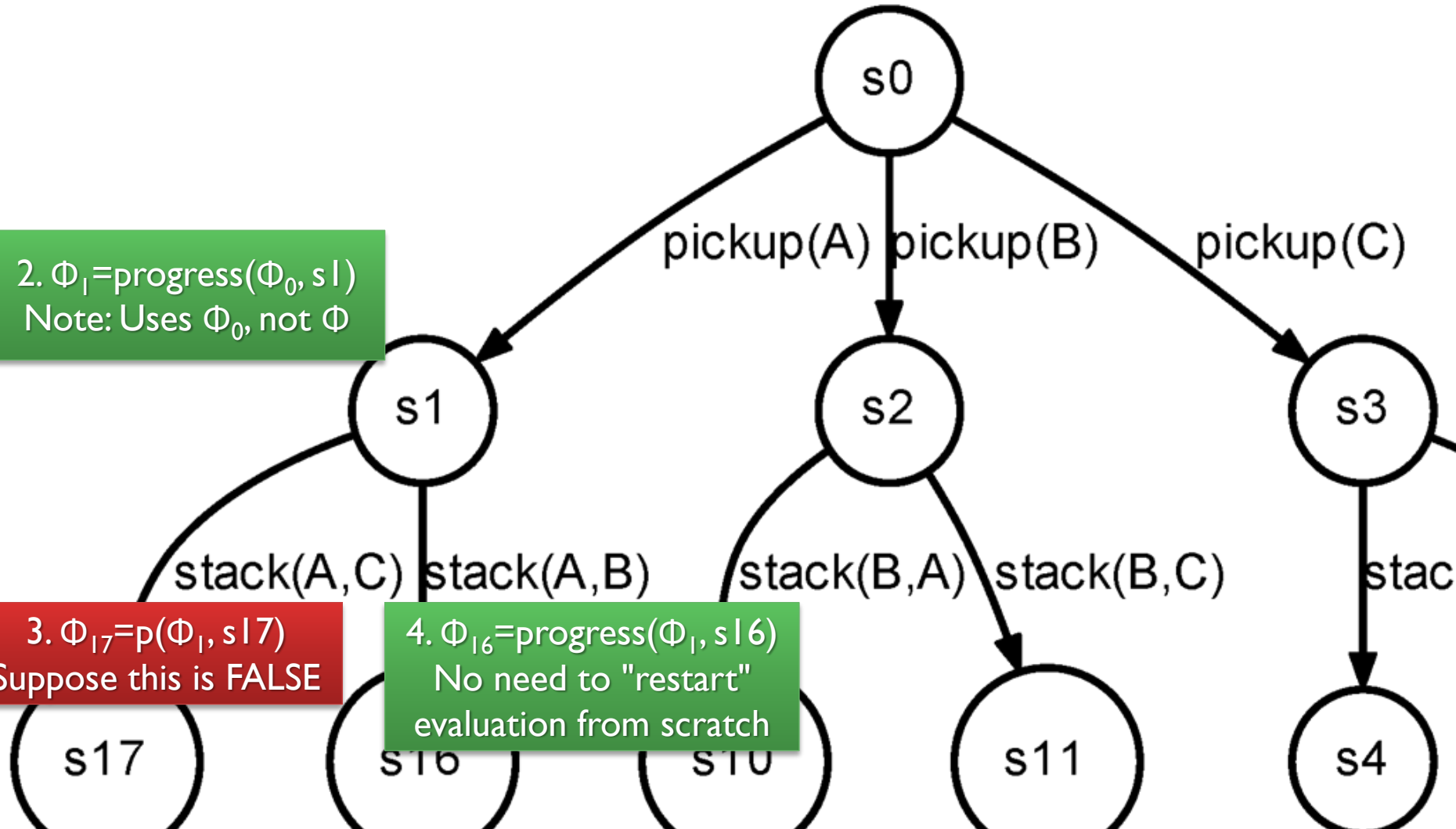
$\Phi$  = original control formula

1. Calculate and store  $\Phi_0 = \text{progress}(\Phi, s_0)$   
Resolves all references to values in state  $s_0$ !

2.  $\Phi_1 = \text{progress}(\Phi_0, s_1)$   
Note: Uses  $\Phi_0$ , not  $\Phi$

3.  $\Phi_{17} = p(\Phi_1, s_{17})$   
Suppose this is FALSE

4.  $\Phi_{16} = \text{progress}(\Phi_1, s_{16})$   
No need to "restart"  
evaluation from scratch



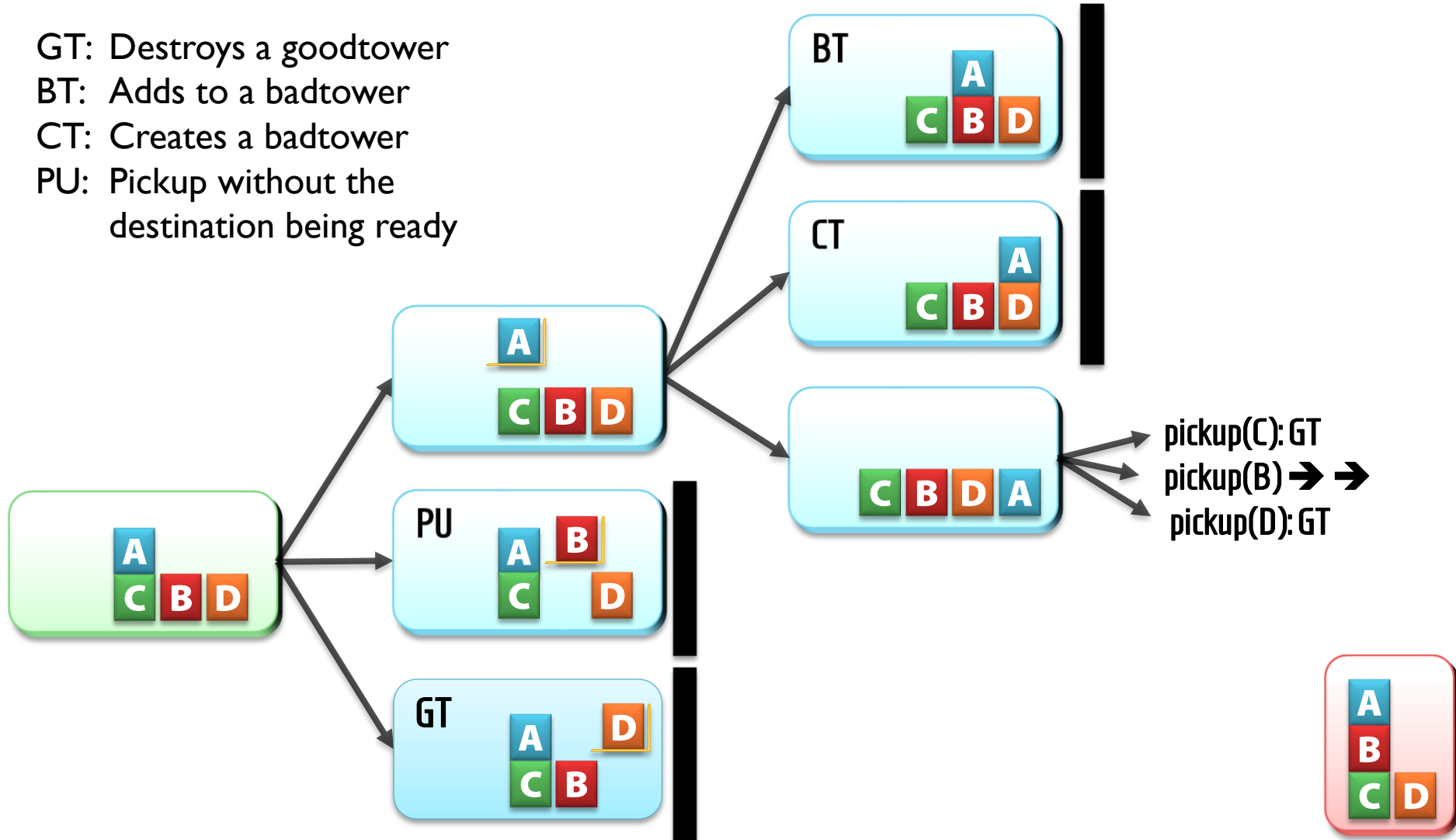
# DFS with Pruning

GT: Destroys a goodtower

BT: Adds to a badtower

CT: Creates a badtower

PU: Pickup without the  
destination being ready



- 2000 International Planning Competition
  - **TALplanner** received the top award for a “hand-tailored” (i.e., domain-configurable) planner
- 2002 International Planning Competition
  - **TLplan** won the same award
- Both of them (as well as SHOP, an HTN planner):
  - Ran **several orders of magnitude** faster than the “fully automated” (i.e., not domain-configurable) planners
    - especially on large problems
  - Solved problems on which other planners ran out of time/memory
  - Required a **considerably greater modeling effort** for each planning domain

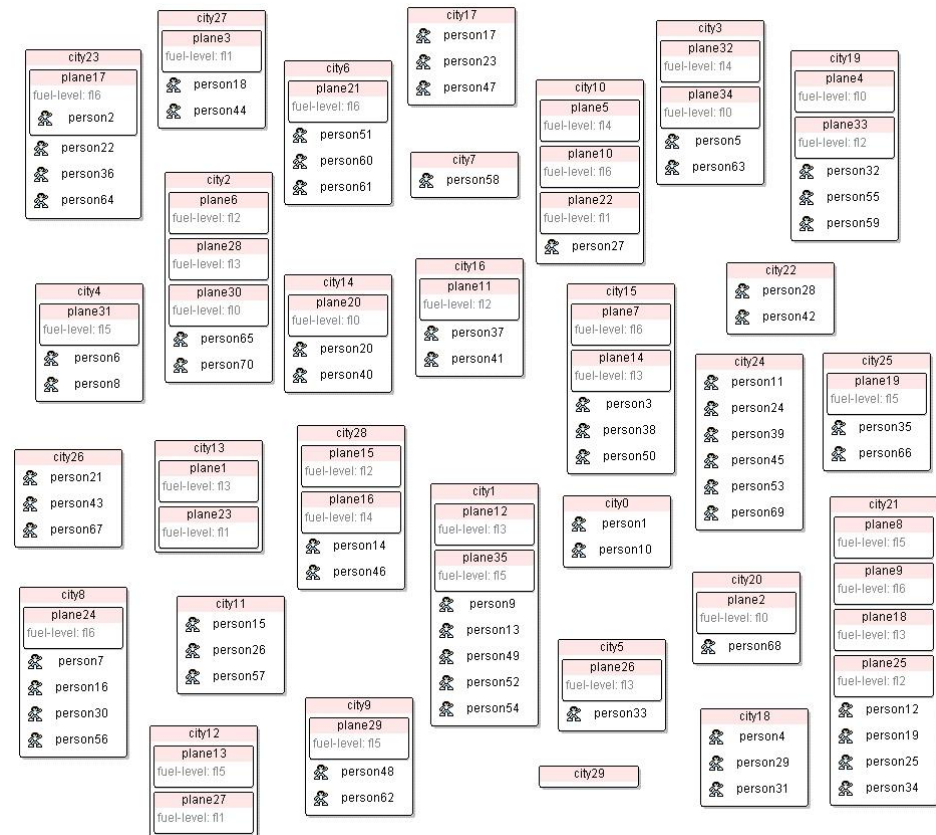
# TALplanner: A demonstration



# TALplanner Example Domain

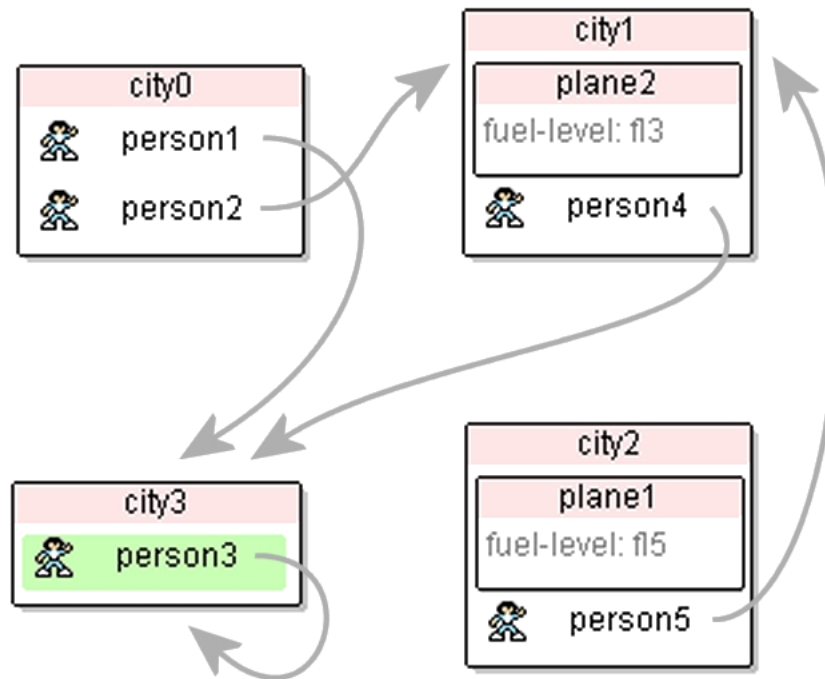
## ■ Example Domain: ZenoTravel

- Planes move people between cities (board, debark, fly)
- Planes have limited fuel level; must refuel
- Example instance:
  - 70 people
  - 35 planes
  - 30 cities



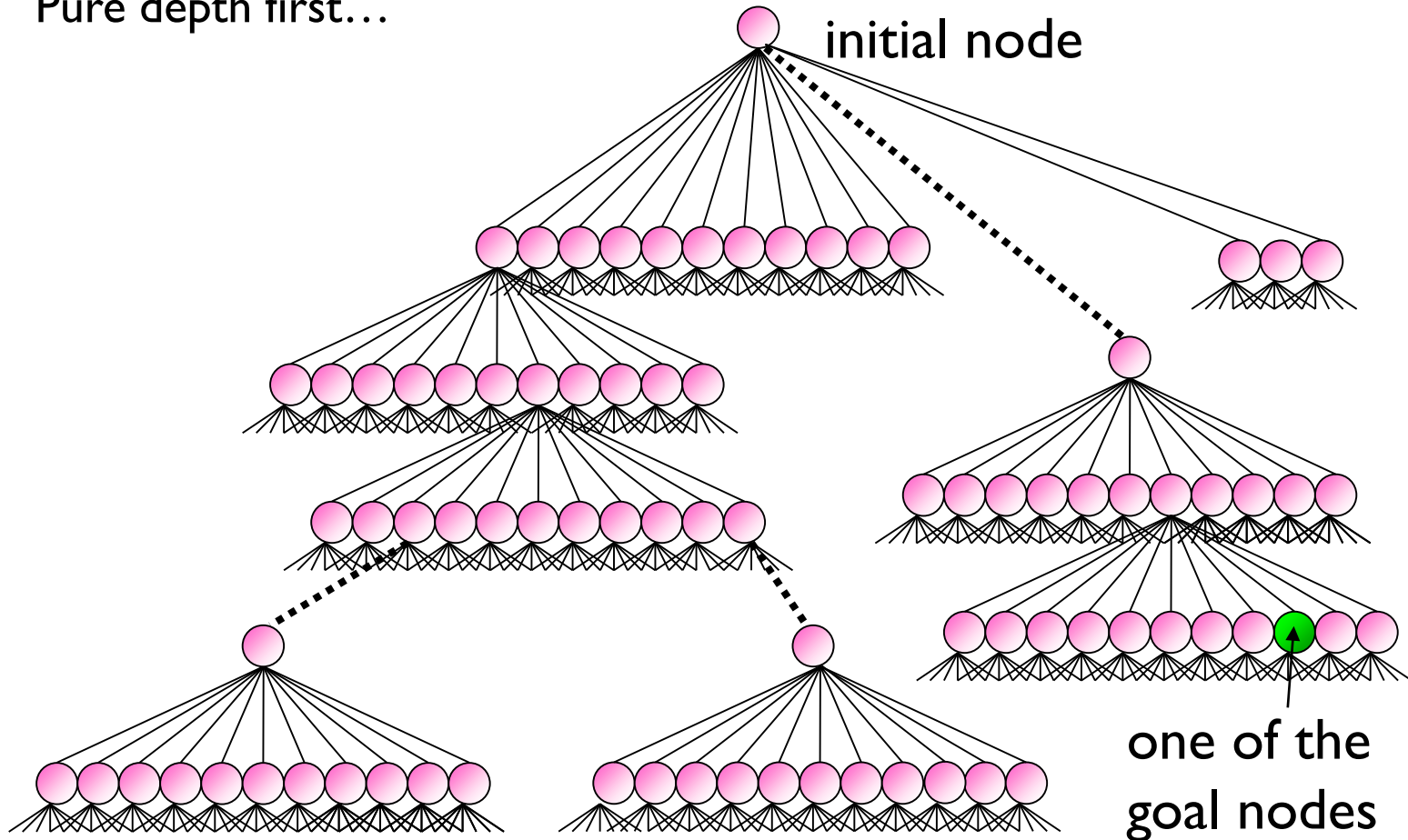
# ZenoTravel Problem Instance

- A smaller problem instance



# What Just Happened?

- No additional domain knowledge specified yet!
  - Pure depth first...



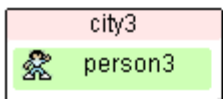
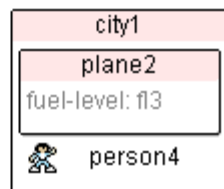
- **First problem** in the example:
  - Passengers debark whenever possible.
  - Rule: "At any timepoint, if a passenger debarks, he is at his goal."
- **#control**:name "only-debark-when-in-goal-city"  
    **forall**  $t, person, aircraft$  [  
         $[t]$  **in**( $person, aircraft$ )  $\rightarrow$   
         $[t+1]$  **in**( $person, aircraft$ )  $\vee$   
        **exists**  $city$  [  
             $[t]$  **at**( $aircraft, city$ )  $\wedge$   
            **goal**(**at**( $person, city$ )) ] ]

$[t]$ : "now"  
 $[t+1]$ : "next"

- **Second problem** in the example:

- Passengers board planes, even at their destinations
- Rule: "At any timepoint, if a passenger boards a plane, he was not at his destination."
- #**control**:name "only-board-when-necessary"  
    **forall**  $t, person, aircraft$  [  
        ( $[t]$  **!in**( $person, aircraft$ )  $\wedge$   
         $[t+1]$  **in**( $person, aircraft$ ))  $\rightarrow$   
        **exists**  $city1, city2$  [  
             $[t]$  **at**( $person, city1$ )  $\wedge$   
            **goal**(**at**( $person, city2$ ))  $\wedge$   
             $city1 \neq city2$  ] ]

# Zeno Travel, second attempt



# What's Wrong This Time?



- Only constrained passengers
- Forgot to constrain airplanes
  - Which cities are reasonable destinations?
    - 1. A passenger's destination
    - 2. A place where a person wants to leave
    - 3. The airplane's destination

- #control :name "planes-always-fly-to-goal"  
    **forall** t, aircraft, city [  
        [t] at(aircraft, city) →  
        ([t+1] at(aircraft, city)) |  
        **exists** city2 [  
            city2 != city &  
            ([t+1] at(aircraft, city2)) &  
            [t] reasonable-destination(aircraft, city2) ]]
- #**define** [t] reasonable-destination(aircraft, city):  
    [t] has-passenger-for(aircraft, city) |  
    **exists** person [  
        [t] at(person, city) &  
        [t] in-wrong-city(person) ] |  
    **goal**(at(aircraft, city)) &  
    [t] empty(aircraft) &  
    [t] all-persons-at-their-destinations-or-in-planes ]



# Zeno Travel, third attempt

