TDDD43 Advanced Data Models and Databases

Graph Data Systems

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Based on slides by Olaf Hartig



Outline

- Graph Data Models
- Query Languages
- Graph Processing Systems



Graphs are Everywhere

- Transportation networks
- Bibliographic networks
- Computer networks
- Social networks
- Topic maps
- Knowledge bases
- Protein interactions
- Biological food chains
- etc.





Different Graph Data Systems

- Triple stores
 - Data model: RDF
 - Typically, pattern matching queries
- Graph databases
 - Prevalent data model: property graphs
 - Typically, navigational queries
- Graph processing systems
 - Prevalent data model: generic graphs
 - Typically, complex graph analysis tasks



Graph Data Models



Recap of RDF Data Model

- Data is represented as a set of triples
 - A triple: (subject, predicate, object)
- Subject: resources
- Predicate: properties
- Object: literals or resources



- Such a set of triples may be understood as a graph
 - Triples as directed edges
 - Subjects and objects as vertexes
 - Edges labeled by predicate
- W3C recommendation and standardization



Property Graph

- *"A property graph is made up of nodes, relationships, and properties."*
- Nodes contain properties [...] in the form of arbitrary key-value pairs. The keys are strings and the values are arbitrary data types.
- A relationship always has a direction, a label, and a start node and an end node.
- Like nodes, relationships can also have properties." [1]

[1] Ian Robinson, Jim Webber, and Emil Eifr em. Graph Databases. O'Reilly Media, 2013.



(Labeled) Property Graph





(Labeled) Property Graph

- Directed multigraph
 - Multiple edges between the same pair of nodes
- Any node and any edge may have a label
- Any node and any edge may have an arbitrary set of keyvalue pairs ("properties")





Property Graphs versus RDF Graphs

- Similarities
 - Directed multigraphs
 - Labels on edges and on nodes
 - Attributes with values on nodes
- Differences
 - No edge properties in RDF graphs
 - Edge labels cannot appear as nodes in a PG (in RDF, we may have <s1, p1, o1> and <p1, p2, o2>)
 - No multivalued (node) properties in a PG
 - Node and edge identifiers in a PG are local to the PG, while URIs in RDF graphs are globally unique identifiers



• Given a set of RDF triples

ex:restaurant_A rdf:type ex:Restaurant ex:restaurant_A ex:hasWebsite "http://resaurtantA.org" ex:restaurant_A ex:hasSite ex:Linköping ex:restaurant_A ex:startDate "2012-02-01"

ex:restaurant_B rdf:type ex:Restaurant ex:restaurant_B ex:hasWebsite "http://resaurtantB.org" ex:restaurant_B ex:hasSite ex:Linköping ex:restaurant_B ex:startDate "2013-02-01"

ex:Linköping rdf:type ex:City



• Given a set of RDF triples

ex:restaurant_A rdf:type ex:Restaurant
ex:restaurant_A ex:hasWebsite "http://resaurtantA.org"
ex:restaurant_A ex:hasSite ex:Linköping
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ex:restaurant_B rdf:type ex:Restaurant
ex:restaurant_B ex:hasWebsite "http://resaurtantB.org"
ex:restaurant_B ex:hasSite ex:Linköping
ex:restaurant_B ex:startDate "2013-02-01"

ex:Linköping rdf:type ex:City

Nodes



• Given a set of RDF triples

ex:restaurant_Ardf:typeex:Restaurantex:restaurant_Aex:hasWebsite "http://resaurtantA.org"ex:restaurant_Aex:hasSiteex:restaurant_Aex:startDate"2012-02-01"

ex:restaurant_B rdf:type ex:Restaurant
ex:restaurant_B ex:hasWebsite "http://resaurtantB.org"
ex:restaurant_B ex:hasSite ex:Linköping
ex:restaurant_B ex:startDate "2013-02-01"

ex:Linköping rdf:type ex:City

Nodes Labels (Nodes)



• Given a set of RDF triples

ex:restaurant_A rdf:type ex:Restaurant ex:restaurant_A ex:hasWebsite "http://resaurtantA.org" ex:restaurant_A ex:hasSite ex:Linköping ex:restaurant_A ex:startDate "2012-02-01"

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ex:Linköping rdf:type ex:City

Labels (Edges)



• Given a set of RDF triples

ex:restaurant_A rdf:type ex:Restaurant ex:restaurant_A ex:hasWebsite "http://resaurtantA.org" ex:restaurant_A ex:hasSite ex:Linköping ex:restaurant_A ex:startDate "2012-02-01"

ex:restaurant_B rdf:type ex:Restaurant ex:restaurant_B ex:hasWebsite "http://resaurtantB.org" ex:restaurant_B ex:hasSite ex:Linköping ex:restaurant_B ex:startDate "2013-02-01"

ex:Linköping rdf:type ex:City

Properties



Generic Graphs

- Data model
 - Directed multigraphs
 - Arbitrary user-defined data structure can be used as value of a vertex (node) or an edge (e.g., a Java object)
- Example (Apache Flink Gelly API for Graph processing)

```
// create new vertexes with a Long ID and a String value
Vertex<Long, String> v1 = new Vertex<Long, String>(1L, "foo");
Vertex<Long, String> v2 = new Vertex<Long, String>(2L, "bar");
Edge<Long, Double> e = new Edge<Long, Double>(1L, 2L, 0.5);
```

- Pros: give users maximum flexibility for representing graphs
- Cons: systems cannot provide built-in operators related to vertex data or edge data



Examples of Graph DB Systems

- Systems that focus on graph databases
 - Neo4j
 - Sparksee
 - Titan
 - Infinite Graph
- Multi-model NoSQL databases with support

for graphs

- OrientDB
- ArangoDB
- Triple stores with Apache TinkerPop support
 - Stardog





Apache TinkerPop

- Graph computing framework
 - Vendor-agnostic



- For graph databases (a graph structure API)
 - Formerly known as Blueprints API
 - Creating and modifying property graphs
 - Example:

Graph graph = ...

Vertex marko = graph.addVertex(T.label, "person", T.id, 1, "name", "marko", "age", 29); Vertex vadas = graph.addVertex(T.label, "person", T.id, 2, "name", "vadas", "age", 27); marko.addEdge("knows", vadas, T.id, 7, "weight", 0.5f);

- For graph analytic systems (a process API)
 - Graph-parallel engine
 - Graph traversal/query, based on Gremlin language







Gremlin Graph Traversal (Query) Language

- Part of the Apache TinkerPop framework
- Powerful domain-specific language (DSL) with embeddings in different programming languages
- Expressions specify a concatenation of traversal steps
 - A chain of operations/functions that are evaluated from left to right

g.V().has('name', 'marko').out('knows').values('name')





Gremlin Examples

g.V().has('name', 'marko').out('knows').values('name')

- **g**: for the current graph traversal
- V(): for all vertices in the graph
- has('name', 'marko'): filters the vertices
 down to those with 'name' property 'marko'
- out('knows'): traverse outgoing 'knows' edges
- values('name'): extracts the values of 1
 'name' property



Result:



Gremlin Examples

g.V().has('name', 'marko').out('knows').values('name').path()

- g: for the current graph traversal
- V(): for all vertices in the graph
- has('name', 'marko'): filters the vertices down to those with 'name' property 'marko'

Graph Data Systems

- out('knows'): traverse outgoing 'knows' edges
- values('name'): extracts the values of 'name' property
- *path()*: returns the history of the traverser



Result:

==> [v[1],v[2],vadas]

==> [v[1],v[4],josh]

g.V().has('name', 'marko').repeat(out()).times(2).path().by('name')

```
Result: ==> [marko, josh, ripple]
==> [marko, josh, lop]
```

g.V().until('name', 'ripple').repeat(out()).path().by('name')

- times(N): the number of traverses (N)
- **by('name')**: element property projection
- *repeat()*: loops over a traversal given some break predicate





or

Cypher

- Declarative graph database query language
- Proprietary (used by Neo4j)
- The OpenCypher project aims to deliver an open specification
- Example
 - Recall our initial Gremlin example g.V().has('name', 'marko').out('knows').values('name')
 - In Cypher, we could express this query as follows: MATCH({name: 'marko'})-[:knows]->(x) RETURN x.name



Possible Clauses in Cypher Queries

- CREATE creates nodes and edges
- DELETE removes nodes, edges, properties
- SET sets values of properties
- MATCH specifies a *pattern* to match in the data graph
- WHERE filters pattern matching results
- RETURN which nodes / edges / properties in the matched data should be returned
- UNION merges results from two or more queries
- WITH chains subsequent query parts (like piping in Unix commands)
 - manipulate the output before it is passed on to the following query parts



Node Patterns in Cypher

• Node patterns may have different forms

() – matches any node

(:person)-> – matches nodes whose label is person

({name: 'marko'}) - matches nodes having a property name='marko' (:person {name: 'marko'}) - matches nodes having both the label

person and a property name='marko'

- Every node pattern can be assigned a variable
 - Can be used to refer to the matching node in another query clause or to express joins
 - For instance, (x), (x:person)



Relationship Patterns in Cypher

- Relationship pattern must be placed between two node patterns and it may have different forms
 - --> or <-- matches any edge (with the given direction)
 - -[:knows]-> matches edges whose label is knows
 - -[{weight:0.5}]-> matches edges having a property weight=0.5
 - -[:knows {weight:0.5}]-> matches edges having both the label knows and a property weight=0.5

-[:knows*..4]-> – matches paths of knows edges of up to length 4

- Every relationship pattern can be assigned a variable
 - For instance, -[x:knows]->



More complex Cypher Patterns

- Node patterns and relationship patterns are just basic building blocks that can be combined into more complex patterns
 - *MATCH*: searches for an existing node, relationship, label, property, or pattern in the database (like SELECT in SQL).
 - *RETURN*: specifies what values or results you might want to return from a Cypher query.
- Examples:

```
MATCH (a)-[:knows]->()-[:knows]->(a)
RETURN a
```

```
MATCH p=shortestPath(
```

```
(:person {name: 'marko'})-[*]->(:person {name: 'josh'})
```

```
RETURN p
```



Filtering in Cypher

- Pattern matching results can be filtered out by using *WHERE* clause
- Examples:
 - MATCH (a:person)-[x:knows]->(b:person) WHERE x.weight >0.5 AND x.weight<0.9 RETURN a, b
 - MATCH ()-[x:knows]->()
 WHERE exists(x.weight)
 RETURN x
 - MATCH (a)-[:knows]->(b)-[x:knows]->(c)
 WHERE NOT (a)-[:knows]->(c)
 RETURN a, b, c



Updating in Cypher

- CREATE, SET, DELETE, REMOVE
- Examples:
 - CREATE (friend:Person {name: 'Mark'}) RETURN friend
 - MATCH (a:person)-[x:knows]->(b:person)
 SET x.weight = 0.5
 RETURN x
 - MATCH ()-[x:knows]->()
 WHERE NOT exists(x.weight)
 DELETE x
 - MATCH (a:person)-[:knows]->(b)-[x:knows]->(c) REMOVE a.organization



Graph Processing Systems



Complex Graph Analysis Tasks?

- Tasks that require an iterative processing of the entire graph or large portions
- Examples
 - Centrality analysis (e.g., PageRank)
 - Clustering, connected components
 - Graph coloring
 - All-pairs shortest path
 - Graph pattern mining (e.g., frequent sub-graphs, community detection)
 - Machine learning











Properties of Computation on Graphs

- Dependency graph
 - Dependencies among vertexes
- Local updates
 - The value of a vertex is only influenced by its neighbours
- Iterative Computation
 - E.g., PageRank





PageRank

- Google Search
- A link analysis algorithm
- An algorithm to rank web pages in results from search engine
 - Measuring the importance of website pages
 - Counting number and quality of links to a page for determining how important a website is



Example: PageRank, simplified version



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

 $PR_k(v)$: the value of a webpage v in the kth iteration of computing v_{in} : the set of vertexes that have outgoing edges (link) to v v_{out} : the set of vertexes that have incoming edges from v

	k=0	k=1	k=2	k=3	k=4	k=5	k=6
<i>PR</i> _{<i>k</i>} (V1)	0.25						
<i>PR</i> _k (V2)	0.25						
<i>PR</i> _k (V3)	0.25						
<i>PR</i> _k (V4)	0.25						



Example: PageRank



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

 $PR_{2}(V1) = PR_{1}(V3)/|V3_{out}| + PR_{1}(V4)/|V4_{out}|$ = PR_{1}(V3)/1 + PR_{1}(V4)/2 = 0.25/1 + 0.25/2 = 0.375

	k=0	k=1	k=2	k=3	k=4	k=5	k=6
<i>PR</i> _{<i>k</i>} (V1)	0.25	0.37					
<i>PR</i> _k (V2)	0.25						
PR _k (V3)	0.25						
<i>PR_k(V4)</i>	0.25						



Example: PageRank



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

 $PR_{2}(V1) = PR_{1}(V3)/|V3_{out}| + PR_{1}(V4)/|V4_{out}|$ = PR_{1}(V3)/1 + PR_{1}(V4)/2 = 0.25/1 + 0.25/2 = 0.375

	k=0	k=1	k=2	k=3	k=4	k=5	k=6		
<i>PR</i> _{<i>k</i>} (V1)	0.25	0.37	0.43	0.45	0.39	0.38	0.38		
<i>PR</i> _{<i>k</i>} (V2)	0.25	0.08	0.12	0.14	0.11	0.13	0.13		
<i>PR</i> _{<i>k</i>} (V3)	0.25	0.33	0.27	0.29	0.29	0.28	0.28		
<i>PR</i> _k (V4)	0.25	0.20	0.16	0.20	0.19	0.19	0.19		
Convergence									



Observation

 Many such algorithms iteratively propagate data along the graph structure by transforming intermediate vertex and edge values



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

$$PR_{2}(V1) = PR_{1}(V3)/|V3_{out}| + PR_{1}(V4)/|V4_{out}|$$

$$= PR_{1}(V3)/1 + PR_{1}(V4)/2$$

$$= 0.25/1 + 0.25/2$$

$$= 0.375$$



Can we use MapReduce?





Can we use MapReduce?



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

$$PR_2(V1) = PR_1(V3) / |V3_{out}| + PR_1(V4) / |V4_{out}|$$

$$= PR_1(V3) / 1 + PR_1(V4) / 2$$

$$= 0.25 / 1 + 0.25 / 2$$

0.375

- Map:
 - produces weights of a vertex that assigns to other vertexes e.g., (V3, (0.25, [V1])), (V4, (0.125, [V1, V3]))

=

- For iterations, keeps topology information, e.g., (V3, [V1]), (V4, [V1,V3])
- For checking convergence, keeps vertexes' values, e.g., (V3, 0.25), (V4, 0.25)
- Reduce
 - Handle all the above (3 kinds) information, computes new values and compares with values from last iteration



Can we use MapReduce?

- MapReduce does not directly support iterative algorithms
- Materializing intermediate results at each M/R iteration harms performance
- Extra M/R job on each iteration for checking whether a fixed point has been reached
- Additional issue for graph algorithms
 - Invariant graph-topology data reloaded and reprocessed at each iteration
 - Wastes I/O, CPU, and network bandwidth





Graph Processing Systems

- Pregel Family
- GraphLab Family
- Other Systems





Vertex-centric Abstraction

- Many such algorithms iteratively propagate data along the graph structure by transforming intermediate vertex and edge values
 - These transformations are defined in terms of functions on the values of adjacent vertexes and edges
 - Hence, such algorithms can be expressed by specifying a function that can be applied to any vertex separately
- "Think like a vertex"





Vertex-centric Abstraction

- Vertex compute function consists of three steps:
 - 1. Read all incoming messages from neighbors
 - 2. Update the value of the vertex
 - 3. Send messages to neighbors
- Additionally, the function may "vote to halt" if a local convergence criterion is met
- Overall execution can be parallelized!
- Terminates when all vertexes have halted and no messages in transit



- 1. Read all incoming messages from neighbors
- 2. Update the value of the vertex
- 3. Send messages to neighbors

Additionally, the function may "vote to halt" if a local convergence criterion is met



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

	k=0	k=1	k=2	k=3	k=4	k=5	k=6
<i>PR</i> _{<i>k</i>} (V1)	0.25						
PR _k (V2)	0.25						
PR _k (V3)	0.25						
<i>PR</i> _{<i>k</i>} (V4)	0.25						



1. Read all incoming messages from neighbors

- 2. Update the value of the vertex
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Additionally, the function may "vote to halt" if a local convergence criterion is met



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

	k=0	k=1	k=2	k=3	k=4	k=5	k=6
<i>PR</i> _{<i>k</i>} (V1)	0.25						
PR _k (V2)	0.25						
PR _k (V3)	0.25						
<i>PR</i> _{<i>k</i>} (V4)	0.25						



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	k=0	k=1	k=2	k=3	k=4	k=5	k=6
PR _k (V1)	0.25						
PR _k (V2)	0.25						
PR _k (V3)	0.25						
<i>PR</i> _{<i>k</i>} (V4)	0.25	0.20					



- 1. Read all incoming messages from neighbors
- 2. Update the value of the vertex
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Additionally, the function may "vote to halt" if a local convergence criterion is met



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

	k=0	k=1	k=2	k=3	k=4	k=5	k=6
<i>PR</i> _k (V1)	0.25	0.37					
<i>PR</i> _{<i>k</i>} (V2)	0.25	0.08					
<i>PR</i> _{<i>k</i>} (V3)	0.25	0.33					
<i>PR</i> _{<i>k</i>} (V4)	0.25	0.20					



- 1. Read all incoming messages from neighbors
- 2. Update the value of the vertex

3. Send messages to neighbors

Additionally, the function may "vote to halt" if a local convergence criterion is met



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

	k=0	k=1	k=2	k=3	k=4	k=5	k=6
<i>PR</i> _{<i>k</i>} (<i>V</i> 1)	0.25	0.37					
<i>PR</i> _{<i>k</i>} (V2)	0.25	0.08					
<i>PR</i> _{<i>k</i>} (V3)	0.25	0.33					
<i>PR</i> _{<i>k</i>} (<i>V</i> 4)	0.25	0.20					



- 1. Read all incoming messages from neighbors
- 2. Update the value of the vertex
- 3. Send messages to neighbors

Additionally, the function may "vote to halt" if a local convergence criterion is met



$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

$PR_k(V1)$ 0.250.370.430.350.390.38 $PR_k(V2)$ 0.250.080.120.140.110.13 $PR_k(V3)$ 0.250.330.270.290.290.28 $PR_k(V4)$ 0.250.200.160.200.190.19		k=0	k=1	k=2	k=3	k=4	k=5	k=6
PR_k(V2) 0.25 0.08 0.12 0.14 0.11 0.13 PR_k(V3) 0.25 0.33 0.27 0.29 0.29 0.28 Log PR_k(V4) 0.25 0.20 0.16 0.20 0.19 0.19 Convert	<i>PR</i> _{<i>k</i>} (<i>V</i> 1)	0.25	0.37	0.43	0.35	0.39	0.38	
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$$PR_{k+1}(v) = \sum_{v' \in v_{in}} PR_k(v') / |v'_{out}|$$

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Apache Flink: iterative Graph Processing: https://nightlies.apache.org/flink/flink-docs-release-1.7/dev/libs/gelly/iterative_graph_processing.html



Bulk Synchronous Parallel (BSP)

- Bulk Synchronous Parallel (BSP) programming model
 - A sequence of iterations (each called a superstep)
 - Supersteps with synchronization barriers
 - During a superstep, a user-defined function is invoked for each vertex
- BSP algorithms features
 - Concurrent computation: every participating processor may perform local computations
 - Communication: The processes exchange data to facilitate remote data storage
 - Barrier synchronization: When a process reaches this point (the barrier), it waits until all other processes have reached the same barrier
- Application
 - Google Pregel
 - BSP on top of Hadoop (open project)





Google Pregel (vertex-centric)

- To solve problems which are difficult to solve using MapReduce
- Each vertex has two statuses:
 - Active and inactive (halt)
- Initially, every vertex is active
- Each vertex sends messages to neighbors
- Within a superstep: after a vertex receives a message, based on its function and criterion, it may need to compute a new value (active) or not (inactive)
- Start next superstep, the computation ends until all vertex are inactive (no need to compute)



Google Pregel



- In each superstep, each vertex executes one user-defined function
- Vertices communicate with other vertices through messages
- A vertex can send a message to any other vertex in the graph, as long as it knows its unique ID
 - In each superstep, all active vertices execute the same user-defined computation in parallel
 - User only need to define one vertex compute function



MapReduce versus Pregel

MapReduce

- Requires passing of entire graph topology from one iteration to the next
- Intermediate result after each iteration is stored on disk and then read again from disk
- Programmer needs to write a driver program to support iterations, and another M/R job to check for fixed point

Pregel

- Graph topology is not passed across iterations, vertexes only send their state to their neighbors
- Main memory based
- Usage of supersteps and master-client architecture makes programming easy



Google Pregel





power-law degree distribution!



Google Pregel (BSP) Limitations

- In the BSP (bulk synchronous parallel) model, performance is limited by slowest worker machine
 - Many real-world graphs have power-law degree distribution, which may lead to few highly-loaded workers
 - A single vertex has more out-edges than in-edges, or vice versa





Possible optimizations to balance the workload

- Decompose the vertex program
- Sophisticated graph partitioning
- Graph-centric abstraction
- Asynchronous execution (instead of BSP)



Possible optimizations to balance the workload

- Decompose the vertex program
 Sophisticated graph partitioning
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- Asynchronous execution (instead of BSP)



Combiner

- Takes two messages and combines them into one associative, commutative function
- Can be used to aggregate messages before sending them to the worker node that has the target vertex
- Example:
 - In the vertex-centric PageRank, messages are values $m_{IN} = \left(\frac{PR_k(v')}{|v'_{out}|}\right)$ of each incoming neighbor v_{in} .
 - In the vertex function these values are summed up
 - Parts of this sum may be computed by worker nodes that have some of the incoming neighbor vertexes





Signal/Collect Model

- Also known as Scatter-Gather Iterations, vertex-centric
- Scatter/Signaling (edge function):
 - Every edge uses the value of its source vertex to compute a message ("signal") for the target vertex
 - Executed on the worker that has the source vertex
 - Main task: produces the messages that a vertex will send to other vertices
- Gather/Collecting (vertex function):
 - Every vertex computes its new value based on the messages received from its incoming edges
 - Executed on the worker that has the target vertex
 - Main task: updates the vertex value using received messages



Pregel vs Scatter-Gather

- Similarities
 - Vertex-centric
 - Pregel, Scatter-Gather, parallelism based on vertex computations
- Differences
 - In Pregel, user defines one single vertex compute function
 - In Scatter-Gather, user defines two functions
 - Scatter function for sending messages
 - Gather function for updating values
 - Scatter-Gather decouples sending messages and updating values
 - Easy to maintain



Possible optimizations to balance the workload

Decompose the vertex program

Sophisticated graph partitioning

- Graph-centric abstraction
- Asynchronous execution (instead of BSP)



Graph Partitioning







Original graph

Vertex partitioning/Edge-cut

Edge partitioning/Vertex-cut

- The goals of graph partitioning
 - Load balancing, to decrease memory usage
 - Minimize cuts, to decrease communications
- Unfortunately, the problem is NP-complete
- Various heuristics and approximation algorithms





Vertex-Cut

- PowerGraph, a framework for large-scale machine learning and graph computation
- PowerGraph introduced a partitioning scheme that "cuts" vertexes such that the edges of high-degree vertexes are handled by multiple workers
 - improved work balance
- Power-law graphs (some node has a large number of edges) have good vertex-cuts
 - Communication is linear in the number of machines each vertex spans
 - Vertex-cut minimizes this number
 - Hence, reduced network traffic



Summary

- NoSQL Data Models
 - Key-value model
 - Document model
 - Wide-Column model
 - Graph Data Model
 - Graph Processing for generic graphs





