



## An Integrated Framework for the Design and Optimization of SOC Test Solutions\*

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*Received September 6, 2001; Revised January 16, 2002*

Editor: Krishnendu Chakrabarty

**Abstract.** We propose an integrated framework for the design of SOC test solutions, which includes a set of algorithms for early design space exploration as well as extensive optimization for the final solution. The framework deals with test scheduling, test access mechanism design, test sets selection, and test resource placement. Our approach minimizes the test application time and the cost of the test access mechanism while considering constraints on tests and power consumption. The main feature of our approach is that it provides an integrated design environment to treat several different tasks at the same time, which were traditionally dealt with as separate problems. We have made an implementation of the proposed heuristic used for the early design space exploration and an implementation based on Simulated Annealing for the extensive optimization. Experiments on several benchmarks and industrial designs show the usefulness and efficiency of our approach.

**Keywords:** SOC test, test scheduling, test access mechanism design, test resource partitioning, test resource placement, test conflicts, power consumption

### 1. Introduction

The testing of System-on-Chip (SOC) is a crucial and time consuming problem due to the increasing design complexity. Therefore it is important to provide the test designer with support to develop an efficient test solution.

The work-flow for a test designer developing a test solution consists typically of two consecutive parts: an early design space exploration and an extensive optimization for the final solution. During the process, conflicts and limitations must be carefully considered. For instance, tests may be in conflict with each other due to the sharing of test resources; and power consumption must be controlled, otherwise the system may be damaged during test. Furthermore, test

resources such as external testers support a limited number of scan-chains and have a limited test memory, which also introduce constraints.

Research has been going on in developing techniques for test scheduling, test access mechanism (TAM) design and testability analysis. For example, a framework to support the design of test solutions for SOC with Built-In Self-Test (BIST) has been proposed by Benso et al. [2]. In this paper, we combine and generalize several approaches in order to create an integrated framework for the development of SOC test solutions where:

- tests are scheduled to minimize the total test time,
- a minimal TAM is designed,
- test resources are floor-planned, and
- test sets for each core with test resources are selected.

The above set of tasks is performed in a single algorithm, which considers test conflicts, power limitation

\*This work has partially been supported by the Swedish Agency for Innovation System (VINNOVA) and Ericsson.

and test resource constraints [17–19]. The algorithm is suitable for early design space exploration due to its low computational complexity, which is an advantage since it will be used iteratively many times.

Chakrabarty showed that test scheduling is equal to the open-shop scheduling [4], which is known to be NP-complete and the use of heuristics are therefore justified. Several heuristics have been proposed [1, 4, 7, 9, 11, 15, 23, 27]; however, they have been evaluated using rather small benchmarks. For such benchmarks, a technique based on Mixed-Integer Linear-Programming (MILP) can be used [7]. A disadvantage is the complexity of solving the MILP model since the size of it quickly grows with the number of tests making it infeasible for large industrial designs. We have therefore made an implementation based on Simulated Annealing for the extensive optimization of the test schedule and the TAM design for the final solution [16]. We have performed experiments on several benchmarks and on an Ericsson design consisting of 170 tests to show the efficiency and usefulness of our approach.

The rest of the paper is organised as follows. Related work is outlined in Section 2 and the system modelling is introduced in Section 3. Factors affecting the test solution are presented in Section 4. The integrated algorithm is described in Section 5 and how we used Simulated Annealing is outlined in Section 6. The paper is concluded with experimental results in Section 7 and conclusions are in Section 8.

## 2. Related Work

The basic problem in test scheduling is to assign a start time for all tests. In order to minimize the test application time, tests are scheduled as concurrent as possible, however, various types of constraints must be considered.

A test to be scheduled consists of a set of test vectors produced or stored at a test source (placed on-chip or off-chip). The test response from the test is evaluated at a test sink (placed on-chip or off-chip). When applying a test, a test conflict may occur, which must be considered during the scheduling process. For instance, often a testable unit is tested by several test sets (usually an external test set and a on-chip test set are required to reach high test quality). If several tests are used for a testable unit, only one test can be applied to the testable unit at a time.

Constraints on power consumption must be considered otherwise the system can be damaged. During

testing mode, the power consumption is usually higher compared to normal operation [12]. For instance, consider a memory, which often is organized in memory banks. During normal operation, only a single bank is activated. However, during testing mode, in order to test the system in the shortest possible time it is desirable to concurrently activate as many banks as possible [9].

The use of different test resources may entail constraints on test scheduling. For instance, external testers have limitations of bandwidth due to that a scan chain operates usually at a maximum frequency of 50 MHz [13]. External testers can usually only support a maximum of 8 scan chains [13], resulting in long test application time for large designs. Furthermore, an external tester's memory is limited by its size [13].

Zorian proposed a test scheduling technique for fully BISTed systems where test time is minimized while power constraint is considered [27]. The tests are scheduled in sessions where tests at cores placed physically close to each other are grouped in the same test session. In a fully BISTed system, each core has its dedicated test source and test sink; and there might not be any conflicts among tests, i.e. the tests can be scheduled concurrently. However, in the general case, conflicts among tests may occur. Garg et al. proposed a test scheduling technique where test time is minimized for systems with test conflicts [11] and for core-based systems a test scheduling technique is proposed by Chakrabarty [4, 7]. Chou et al. proposed an analytic test scheduling technique where test conflicts and power constraints are considered [9]. A resource graph is used to model the system where an arc between a test and a resource indicate that the resource is required for the test, Fig. 1. From the resource graph, a test compatibility graph (TCG) is generated (Fig. 2) where each test is a node and an arc between two nodes indicates that the tests can be scheduled concurrently. For instance  $t_1$  and  $t_4$  can be scheduled at the same time. Each test is attached with its test time and its power consumption and the maximal allowed power consumption is 10. The tests  $t_1$  and  $t_5$  are compatible, however, due to the power limit they cannot be scheduled at the same time.

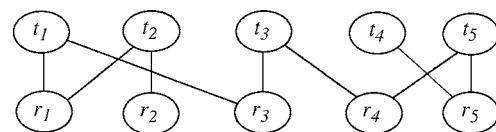


Fig. 1. Resource graph of an example system.

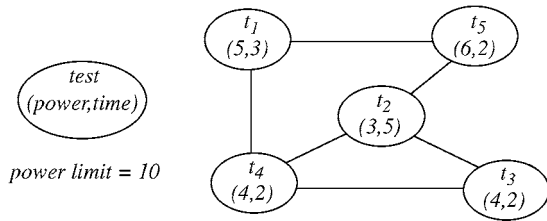


Fig. 2. Test compatibility graph (TCG) of the example system (Fig. 1).

Another test scheduling approach is proposed by Muresan et al. where constraints among tests and on power consumption are considered [23]. Favour is given to reduce the test time by allowing new tests to start even if all tests in a session are not completed. Iyengar and Chakrabarty proposed a pre-emptive test scheduling technique where the test for a testable unit may be interrupted and resumed later, i.e. the test set is partitioned into several test sets [15]. Using a scheme by Craig et al. the above discussed scheduling techniques can be grouped in [10]:

- nonpartitioned testing,
- partitioned testing with run to completion, and
- partitioned testing.

The differences among the grouping are illustrated with five tests ( $t_1, \dots, t_5$ ) in Fig. 3. The scheduling strategies proposed by Zorian [27] and Chou et al. [9] are nonpartitioned (Fig. 3(a)), the strategy proposed by Muresan et al. is partitioned testing with run to completion (Fig. 3(b)) and the approach proposed by Iyengar and Chakrabarty [15] is partitioned testing (Fig. 3(c)).

A test infrastructure is responsible for the transportation of test vectors from test sources to cores under test

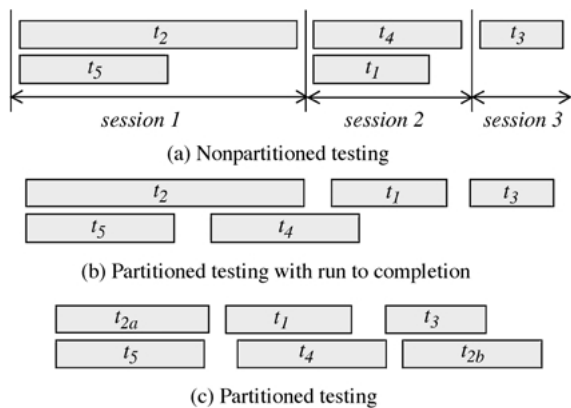


Fig. 3. Scheduling approaches.

and test responses from cores under test to test sinks. It consists of two parts; one for the test data transportation and one for the control of the transportation. In the approach for fully BISTed systems proposed by Zorian [27], tests at cores placed physically close to each other are grouped in the same test session. The main advantage is that the same control structure can be used for all tests in the session, which minimizes the routing of control wires. In general, systems are not tested with a BIST structure only for each testable unit and therefore a TAM is required [5, 6, 8, 24]. Chakrabarty proposed an integer linear programming (ILP) for the allocation of TAM width [5, 6, 8] and the effect on test time for systems using various design styles for test access with the TestShell wrapper is analysed by Aertes and Marinissen [1].

To ease test access the cores can be placed in wrappers such as Boundary scan [3], TestShell [20] or P1500 [14, 22]. The Boundary scan technique, developed for PCB designs, suffers from long testing time due to the shifting process, and it becomes even worse for SOC designs since the amount of test data to be transported increases. An alternative is to use an architectures as proposed by Aertes and Marinissen (Fig. 4(a-c)) where the test time only depends on the number of flip-flops within the cores and the number of test vectors, i.e. the transportation to and from a core is free [1]. The daisy-chained architecture uses a clocked bypass, however, Marinissen et al. have also proposed a wrapper design library allowing bypass structures without clock delay [21].

The above scheduling techniques all assume that all testable units have their selected test sets. Sugihara et al. proposed a technique for selecting test sets where each

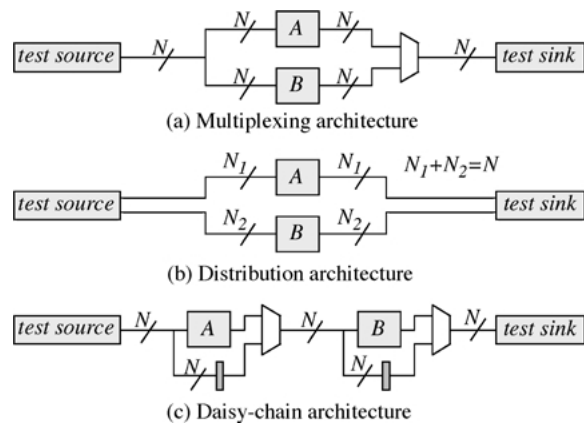


Fig. 4. Multiplexing, distribution and daisy-chain architecture [1].

core may be tested by one test set from an external tester and one test set from a dedicated test generator for the core [25].

### 3. System Modelling

This section describes the formal notation we use to model the SOC under test. An example of a system under test is given in Fig. 5 where each core is placed in a wrapper to ease test access. A DFT technique is added to each core and in this example all cores are tested using the scan technique. The test access port (*tap*) is the connection to an external tester and for instance the test source, *test source 1*, and test sink, *test sink 1*, are implemented on-chip [17, 18]. Applying several sets of tests, where each test set is produced or stored at a test source and the test response is analysed at a test sink, tests the system.

The system in Fig. 5 can be modelled as a *design with test*,  $DT = (C, R_{source}, R_{sink}, p_{max}, T, source, sink, core, constraint, mem, bw)$ , where:

$C = \{c_1, c_2, \dots, c_n\}$  is a finite set of cores where each core  $c_i \in C$  is characterized by  $p_{idle}(c_i)$ : idle power;  $R_{source} = \{r_1, r_2, \dots, r_p\}$  is a finite set of test sources;  $R_{sink} = \{r_1, r_2, \dots, r_q\}$  is a finite set of test sinks;  $p_{max}$ : maximal allowed power at any time;  $T = \{t_1, t_2, \dots, t_o\}$  is a finite set of tests, each consisting of a set of test vectors. Several tests form a *core test (CT)* and each core,  $c_i$ , can be associated with several core tests,  $CT_{ij} (j = 1, 2, \dots, l)$ .

Each test  $t_i$  is characterized by:

- $\tau_{test}(t_i)$ : test time for test  $t_i$ ,
- $p_{test}(t_i)$ : test power for test  $t_i$ ,
- $bw(t_i)$ : bandwidth required for  $t_i$
- $mem(t_i)$ : memory required for test pattern storage.

*source*:  $T \rightarrow R_{source}$  defines the test sources for the tests;

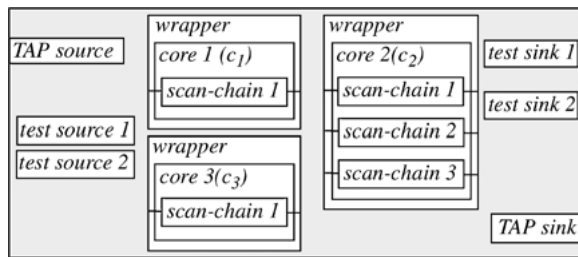


Fig. 5. An example system.

*sink*:  $T \rightarrow R_{sink}$  defines the test sinks for the tests;  
*core*:  $T \rightarrow C$ : the core where a test is applied;  
*constraint*:  $T \rightarrow 2^C$ : the set of cores required for a test;  
*mem*( $r_i$ ): memory available at test source  $r_i \in R_{source}$ ;  
*bw*( $r_i$ ): bandwidth at test source  $r_i \in R_{source}$ .

For each test, one test sink and one test source are required. In our model, it is possible for every test to combine any type of test source (on-chip or off-chip) with any type of test sink (on-chip or off-chip), which is important to allow high flexibility. To further give the designer a high flexibility to explore different combinations of tests, it is possible to define several set of tests ( $CT_{ij}$ ) for each core where each such set tests the core.

Given a system as in Fig. 5 where for each of the cores  $c_1, c_2, c_3$ , one CT exists. For core  $c_1$ ,  $CT_{11} = \{t_1, t_2\}$ , for core  $c_2$ ,  $CT_{21} = \{t_4, t_5\}$  and for  $c_3$ ,  $CT_{31} = \{t_3\}$ . The on-chip test source 1 is required by  $t_1$  and  $t_3$  and the on-chip test sink 1 is required by  $t_3$  and  $t_5$ . The resource graph in Fig. 1 and the test compatibility graph in Fig. 2 model the system when  $r_3$  (test source 1) is needed by  $t_1$  and  $t_3$  and  $r_4$  (test sink 1) needed by  $t_3$  and  $t_5$ .

### 4. The SOC Test Issues

In this section we discuss the different issues considered by our SOC test framework. We also demonstrate the importance of considering them in an integrated manner.

#### 4.1. Test Scheduling

The test scheduling problem can be seen as placing all tests in a diagram as in Fig. 6 while satisfying all constraints. For instance,  $t_1$  and  $t_2$  cannot be applied at the same time since both tests the same core,  $c_1$  (example in Section 3).

The basic difference between our scheduling technique [17, 18] and the approaches proposed by Zorian [27] and Chou et al. [9] is, besides that we design the TAM while scheduling the tests, that Zorian and Chou et al. do not allow new tests to start until all tests in

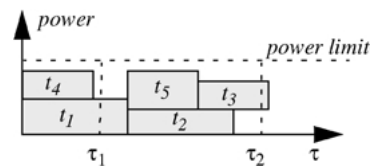


Fig. 6. Example of test scheduling.

a session are completed. It means that if  $t_3$  is about to be scheduled it cannot be scheduled as in Fig. 6. In the approach proposed by Muresan et al. [23],  $t_3$  can be scheduled if it is completed no later than  $t_2$ .

In our approach it is optional if tests may start before all tests in a session are completed (nonpartitioned testing) or not (partitioned testing with run to completion). The advantage of using the latter is that it gives more flexibility.

Let a schedule  $S$  be an ordered set of tests such that:

$$\{S(t_i) < S(t_j) \mid \tau_{start}(t_i) \leq \tau_{start}(t_j), i \neq j, \\ \forall t_i \in S, \forall t_j \in S\},$$

where  $S(t_i)$  defines the position of test  $t_i$  in  $S$ ;  $t_{start}(t_i)$  denotes the time when test  $t_i$  is scheduled to start, and  $\tau_{end}(t_i)$  its completion time:  $\tau_{end}(t_i) = \tau_{start}(t_i) + \tau_{test}(t_i)$ .

For each test,  $t_i$ , the start time and the wires for test data transportation have to be determined before it is inserted into the schedule,  $S$ .

Let the Boolean function  $scheduled(t_i, \tau_1, \tau_2)$  be true if test  $t_i$  is scheduled in such a way that the test time overlaps with the time interval  $[\tau_1, \tau_2]$ , i.e.,

$$\{t_i \in S \wedge \neg(\tau_{end}(t_i) < \tau_1 \vee \tau_{start}(t_i) > \tau_2)\}.$$

An example to illustrate the function  $scheduled$  for a set of scheduled tests is shown in Fig. 7.

The Boolean function  $scheduled(r_i, \tau_1, \tau_2)$  is true if a source  $r_i$  is used by a test  $t_j$  between  $\tau_1$  and  $\tau_2$ , i.e.:

$$\{\exists t_j \in S \mid r_i = source(t_j) \wedge scheduled(t_j, \tau_1, \tau_2)\}.$$

A similar definition is used if a sink  $r_i$  is scheduled (used by any test) between  $\tau_1$  and  $\tau_2$ . The Boolean function  $scheduled(constraint(t_i), \tau_1, \tau_2)$  is true if:

$$\{\exists t_j \in S \mid core(t_j) \in constraint(t_i) \\ \wedge scheduled(t_j, \tau_1, \tau_2)\}.$$

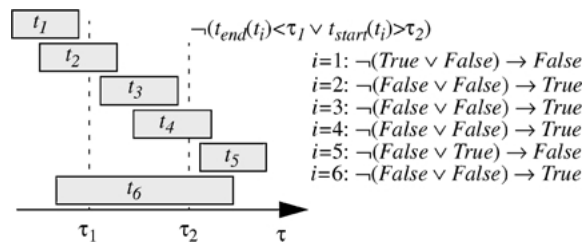


Fig. 7. The function  $scheduled$ .

## 4.2. Power Consumption

Generally speaking, there are more switching activities during the testing mode of a system than when it is operated under the normal mode. The power consumption of a CMOS circuit is given by a static part and a dynamic part where the latter dominates and can be characterized by:

$$p = C \times V^2 \times f \times \alpha$$

where the capacitance  $C$ , the voltage  $V$ , and the clock frequency  $f$  are fixed for a given design [26]. The switch activity  $\alpha$ , on the other hand, depends on the input to the system, which during testing are test vectors and therefore the power dissipation varies depending on the test vectors.

An example illustrating the test power dissipation variation over time  $\tau$  for two test  $t_i$  and  $t_j$  is in Fig. 8. Let  $p_i(\tau)$  and  $p_j(\tau)$  be the instantaneous power dissipation of two compatible tests  $t_i$  and  $t_j$ , respectively, and  $P(t_i)$  and  $P(t_j)$  be the corresponding maximal power dissipation.

If  $p_i(\tau) + p_j(\tau) < p_{max}$ , the two tests can be scheduled at the same time. However, instantaneous power of each test vector is hard to obtain. To simplify the analysis, a fixed value  $p_{test}(t_i)$  is usually assigned for all test vectors in a test  $t_i$  such that when the test is performed the power dissipation is no more then  $p_{test}(t_i)$  at any moment.

The  $p_{test}(t_i)$  can be assigned as the average power dissipation over all test vectors in  $t_i$  or as the maximum power dissipation over all test vectors in  $t_i$ . The former approach could be too optimistic, leading to an undesirable test schedule, which exceeds the test power

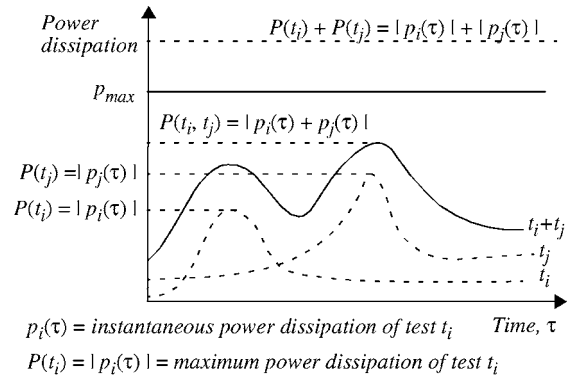


Fig. 8. Power dissipation as a function of time [9].

constraints. The latter could be too pessimistic; however, it guarantees that the power dissipation will satisfy the constraints. Usually, in a test environment the difference between the average and the maximal power dissipation for each test is often small since the objective is to maximize the circuit activity so that it can be tested in the shortest possible time [9]. Therefore, the definition of power dissipation  $p_{test}(t_i)$  for a test  $t_i$  is usually assigned to the maximal test power dissipation ( $P(t_i)$ ) when test  $t_i$  alone is applied to the device. This simplification was introduced by Chou et al. [9] and has been used by Zorian [27] and by Muresan et al. [23]. We will use this assumption also in our approach.

Let  $p_{sch}(\tau_1, \tau_2)$  denote the peak power between  $\tau_1$  and  $\tau_2$ :

$$\max \left\{ \sum_{\forall t_i \text{ scheduled}(t_i, \tau)} p_{test}(t_i) - p_{idle}(core(t_i)) + \sum_{\forall c_i \in C} p_{idle}(c_i), \tau \in [\tau_1, \tau_2] \right\},$$

where  $scheduled(t_i, \tau) = scheduled(t_i, \tau, \tau)$ .

As an example, applying the function  $p_{sch}(\tau_1, \tau_2)$  on the schedule for a system with 5 tests as in Fig. 6, with  $\tau_1$  and  $\tau_2$  as indicated in the figure, returns  $p_{test}(t_2) + p_{test}(t_5) + p_{idle}(c_3)$ , the peak power consumption between  $\tau_1$  and  $\tau_2$ .

In our approach, the maximal power consumption should not exceed the power constraint,  $p_{max}$ , for a schedule to be accepted. That is,  $p_{sch}(0, \infty) \leq p_{max}$ .

#### 4.3. Test Source Limitations

A test source usually has a limited bandwidth. For instance, external tester may only support a limited number of scan chains at a time [13]. There could also be a limitation in the number of available pins. For each test source, this information is given in the attribute bandwidth.

The function  $bw_{alloc}(r_i, \tau_1, \tau_2)$  gives the maximal number of wires allocated between  $\tau_1$  and  $\tau_2$  for a source  $r_i$ , i.e.:

$$\max \left\{ \sum_{\forall t_j \text{ scheduled}(t_j, \tau) \wedge r_i = source(t_j)} |t_{wires}(t_j)|, \tau \in [\tau_1, \tau_2] \right\}.$$

For instance, in Fig. 9 a test source  $r_1$  feeds test  $t_5$  using wire  $w_2$  and  $w_3$ . In this example,  $bw(r_1) = 6$  and

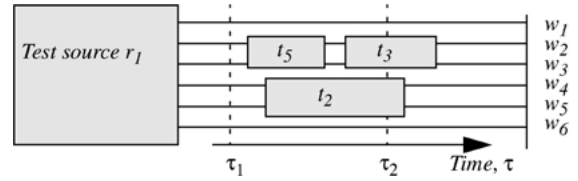


Fig. 9. The TAM allocation.

$bw_{alloc}(r_i, \tau_1, \tau_2) = 4$  since wire  $w_2$  and  $w_3$  are used by  $t_3$  and  $t_5$  and  $w_5$  and  $w_6$  are used by  $t_2$ .

A test generator (test source) may use a memory for storing the test patterns. In particular, external test generators use such a memory with a limited size, which may lead to additional constraints on test scheduling [13].

The function  $mem_{alloc}(r_i, \tau_1, \tau_2)$  gives the allocated memory between time  $\tau_1$  and  $\tau_2$  for a given source  $r_i$ , i.e.:

$$\max \left\{ \sum_{\forall t_j \text{ scheduled}(t_j, \tau) \wedge r_i = source(t_j)} mem(t_j), \tau \in [\tau_1, \tau_2] \right\}.$$

#### 4.4. Test Set Selection

A test set is attached with its test power consumption, test application time, bandwidth requirement and memory requirement (Section 3). The required test source and the test sink are also defined for each test set. In the approach proposed by Sugihara et al. each testable unit can be tested by two test sets using a dedicated BIST resource and an external tester [25]. In our approach, we assume that an arbitrary number of test sets can be used for each testable unit where each test set can be specified using any type of test resource. For instance, we allow the same test resource to be used by several test sets at different testable units. The major advantage is that the designer can define and explore a wider range of test sets. Due to that the test resources are defined for each test set it is possible to make a comparison of different test sets not only in terms of the number of test vectors but also in respect to test resources.

For each testable unit, the designer defines a core test set where each set is a set of test vectors. For instance, if the following  $CT_{11} = \{t_1, t_2\}$ ,  $CT_{12} = \{t_6\}$ ,  $CT_{13} = \{t_7, t_8, t_9\}$  is given for core  $c_1$ . One of  $CT_{11}$ ,  $CT_{12}$  or  $CT_{13}$  must be selected and all tests within the selected CT must be scheduled and no other tests from any other CT for core  $c_1$  should be scheduled.

#### 4.5. Test Access Mechanism

A test infrastructure transports and controls the flow of test data in the system under test. The Boundary scan technique can be used for these purposes, however, it suffers from long testing times and due to the amount of test data to be transported in the system, we assume an infrastructure consisting of test wires (lines). It means we add needed number of test wires from test sources to cores and from cores to test sinks. The time to transport a test vector from a test source to a core and the time to transport test response from a core to a test sink is neglected, which means that the test time is determined by the test vectors and design characteristics of each core.

When adding a TAM between a test source and a core or between a core and a test sink, and the test data has to pass another core,  $c_i$ , several routing options are possible:

1. through the core  $c_i$  using its transparent mode;
2. through an optional bypass structure of core  $c_i$ ; and
3. around core  $c_i$  and not connecting it to the TAM.

The model in Fig. 10(a) of the example system in Fig. 5 illustrates the advantage of alternatives 1 and 2 (Fig. 10(b)) compared to alternative 3 (Fig. 10(c)) since the TAM can be reused in the former two cases. However, a delay may be introduced when the core is in transparent mode or its by-pass structure is used as in the TestShell [22]. On the other hand, Marinissen et al. recently proposed a library of wrapper cells allowing a flexible design where it is possible to design non-clocked bypass structures of TAM width [21]. In the following, we assume that bypass may be solved using such non-delay mechanism.

When designing the TAM, two problems must be solved:

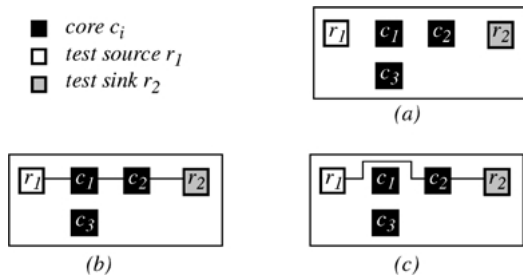


Fig. 10. Illustrating TAM design alternatives using the example in Fig. 5.

Table 1. Test data for the cores in System S.

Core	Index $i$	External test cycles, $e_i$	BIST cycles, $b_i$	Placement	
				$x$	$y$
c880	1	377	4096	10	10
c2670	2	15958	64000	20	10
c7552	3	8448	64000	10	30
s953	4	28959	217140	20	30
s5378	5	60698	389214	30	30
s1196	6	778	135200	30	10

- the design and routing of the TAMs, and
- the scheduling of tests using the TAMs.

In order to minimize the routing, few and short wires are desired. However, such approach increases the test time of the system. For instance, consider System S [4] (Table 1) where we added the floor planning ( $x, y$  co-ordinates for each core). A minimal TAM would be a single wire starting at the TAP, connecting all cores and ending at the TAP. However, such TAM leads to high test application time since no tests can be applied concurrently, all tests have to be applied in a sequence.

The system (for instance the example system in Fig. 5 or System S) can be modelled as a directed graph,  $G = (V, A)$ , where  $V$  consists of the set of cores (the testable units),  $C$ , the set of test sources,  $R_{source}$ , and the set of test sinks,  $R_{sink}$ , i.e.  $V = C \cup R_{source} \cup R_{sink}$  [17, 18]. An arc  $a_i \in A$  between two vertices  $v_i$  and  $v_j$  indicates a TAM (a wire) where it is possible to transport test data from  $v_i$  to  $v_j$ . Initially no TAM exists in the system, i.e.  $A = \emptyset$ . However, if the functional infrastructure may be used, it can be included in  $A$  initially. A test wire  $w_i$  is a path of edges  $\{(v_0, v_1), \dots, (v_{n-1}, v_n)\}$  where  $v_0 \in R_{source}$  and  $v_n \in R_{sink}$ . Let  $\Delta y_{ij}$  be defined as  $|y(v_i) - y(v_j)|$  and  $\Delta x_{ij}$  as  $|x(v_i) - x(v_j)|$ , where  $x(v_i)$  and  $y(v_i)$  are the  $x$ -placement respectively the  $y$ -placement for a vertex  $v_i$  and the distance between vertex  $v_i$  and  $v_j$  is:

$$dist(v_i, v_j) = \sqrt{(\Delta y_{ij})^2 + (\Delta x_{ij})^2}.$$

The Boolean function  $scheduled(w_i, \tau_1, \tau_2)$  is true when a wire  $w_i$  is used between  $\tau_1$  to  $\tau_2$ :

$$\{\exists t_j \in S \mid w_i \in tam(t_j) \wedge scheduled(t_j, \tau_1, \tau_2)\},$$

where  $tam(t_j)$  is the set of wires allocated for test  $t_j$ .

The information of the nearest core in four directions, *north*, *east*, *south* and *west*, is stored for each

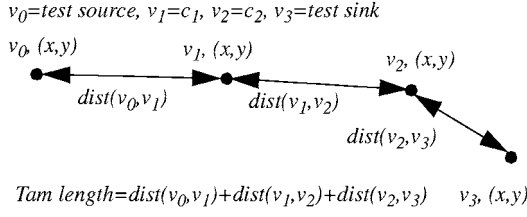


Fig. 11. Computing the TAM length.

vertex. The function  $south(v_i)$  gives the closest vertex south of  $v$ :

$$south(v_i) = \left\{ v_j \left| \left( \frac{\Delta y_{ij}}{\Delta x_{ij}} > 1 \vee \frac{\Delta y_{ij}}{\Delta x_{ij}} < -1 \right), \right. \right. \\ \left. \left. y(v_j) < y(v_i), i \neq j, \min \{ dist(v_i, v_j) \} \right. \right\}.$$

The functions  $north(v_i)$ ,  $east(v_i)$  and  $west(v_i)$  are defined in similar ways. The function  $insert(v_i, v_j)$  inserts a directed arc from vertex  $v_i$  to vertex  $v_j$  if and only if the following is true:

$$\{ south(v_i, v_j) \vee north(v_i, v_j) \vee west(v_i, v_j) \\ \vee east(v_i, v_j) \}.$$

where  $south(v_i, v_j)$  is true if  $v_i = south(v_i)$ .

The function  $closest(v_i, v_j)$  gives a vertex,  $v_k$ , in the neighbourhood of  $v_i$  with the shortest distance to  $v_j$ . The function  $add(v_i, v_j)$  adds arcs from  $v_i$  to  $v_j$  in the following way: (1) find  $v_k = closest(v_i, v_j)$ ; (2) add an arc from  $v_i$  to  $v_k$ ; (3) if  $v_k = v_j$ , terminate otherwise let  $v_i = v_k$  and go to (1).

The total length of a path is the sum of the length of all individual edges. An example to illustrate the calculation of the length of a test wire on the example system (Fig. 5) defined as a path is in Fig. 11 (in this path core  $c_3$  is not included).

#### 4.6. Test Floor-planning

In the approach proposed by Sugihara et al. each testable unit is tested by a test sets using a dedicated BIST resource and an external tester [25]. However, we allow the sharing of test resources and if a BIST resource is shared among several cores, the floor-planning is not trivial.

For instance, if two cores in the example design (Fig. 5) both use a single on-chip test source and test sink, it is most feasible to place the test source at one core while the test sink is placed at the other core.

Initially, the test resources may not be placed. Our algorithm, described in the next section, determines their placement in this case.

## 5. The Heuristic Algorithm

In this section the issues discussed above are combined into an algorithm. The algorithm assumes that the tests are initially sorted according to a key  $k$ , which characterizes  $power(p)$ ,  $testtime(t)$  or  $power \times test\ time(p \times t)$ .

Let  $T$  be the ordered set of the tests, which are ordered based on the key  $k$ . If the scheduling approach is partitioned testing with run to completion the function  $nexttime(\tau_{old})$  gives the next time where it is possible to schedule a test:

$$\{ \tau_{end}(t_i) \mid \min(\tau_{end}(t_i)), \tau_{old} < \tau_{end}(t_i), \forall t_i \in S \},$$

otherwise if nonpartitioned testing is used the function  $nexttime(\tau_{old})$  is defined as:

$$\{ \tau_{end}(t_i) \mid \max(\tau_{end}(t_i)), \tau_{old} < \tau_{end}(t_i), \forall t_i \in S \}.$$

The algorithm depicted in Fig. 12 can basically be divided into four parts for:

- constraint checking,
- test resource placement,
- test access mechanism design and routing, and
- test scheduling.

A main loop is terminated when there exists a core test (CT) for each core such that all tests within the selected CT are scheduled. In each iteration at the loop over the tests in  $T$  a test  $cur$  is checked. A check is also made to determine if all constraints are fulfilled, i.e. it is possible to schedule test  $cur$  with a start at  $\tau$  and an end time at  $\tau_{end} = \tau + \tau_{test}$ :

- $\neg \exists t_f (t_f \in CT_{ij} \wedge t_f \in S \wedge cur \notin CT_{ij})$  checks that another core test set for current core is not used in the schedule,
- $p_{sch}(\tau, \tau_{end}) + p_{test}(cur) < p_{max}$  checks that the power constraint is not violated,
- $\neg scheduled(v_a, \tau, \tau_{end})$  checks that the test source is not scheduled during  $\tau$  to  $\tau_{end}$ ,
- $\neg scheduled(v_c, \tau, \tau_{end})$  checks that the test sink is not scheduled during  $\tau$  to  $\tau_{end}$ ,
- $\neg scheduled(constraint(cur), \tau, \tau_{end})$  checks that all cores required for  $cur$  are available during  $\tau$  to  $\tau_{end}$ ,



```

Sort T according to the key (p, t or p×t);
S=∅; τ=0;
until ∀bpq ∃CTpq ∀ts ∈ S do
  for all cur in T do
    va=source(cur);
    vb=core(cur);
    vc=sink(cur);
    τend=τ+ttest(cur);
    if all constraints are satisfied then begin
      ¬scheduled(va, 0, tend).floor-plan va at vb;
      ¬scheduled(vc, 0, tend).floor-plan vc at vb;
      for all required test resources begin
        new=length of a new wire wj connecting va, vb and vc;
        u=number of wires connecting va, vb and vc not
          scheduled from τ to τend;
        v=number of wires connecting va, vb and vc;
        for all min(v-u, bw(cur))wires wj
          extend=extend+length of an available wire(wj);
        if (bw(cur)>u)
          extend=extend+new×(par-u);
          move=par(va) × min{dist(va, vb), dist(vb, vc)};
          if (move≤min{extend, new × bw(cur)})
            vx, vy=min{dist(va, vb), dist(vb, vc)}, dist(va, vb)>0,
              dist(vb, vc)>0
            add par(va) wires between vx and vy;
            if (vx=source(cur)) then floorplan va at vb;
            if (vy=sink(cur)) then floorplan vc at vb;
          end
        for r = 1 to bw(cur)
          if there exists a not scheduled wire during τ to τend
            connecting va, vb and vc it is selected
          else
            if (length of a new wire < length of extending a wire wj)
              wj=add(va, vb)+add(vb, vc);
            else
              extend wire;
            schedule cur and remove cur from T;
          end;
        τ = nexttime(τ).
    end
  end

```

Fig. 12. The system test algorithm.

- the available bandwidth at test source  $v_a$  is checked to see if:  $bw(v_a) > bw(cur) + bw_{alloc}(v_a, \tau, \tau_{end})$  and
- the available memory test source  $v_a$  is checked to see if:  $mem(v_a) > mem(cur) + mem_{alloc}(v_a, \tau, \tau_{end})$ .

Then the placement of the test resources is checked. If the test resources are on-chip resources and not placed in the system, they are placed at core  $c_i$ . If they are floor-planned, a check is performed to determine if they are to be moved.

When the placement of the test resources for the selected test is determined, the test access mechanism is designed and routed. The basic question is if existing wires can be used or new wires must be added. If no routed connection is available connecting all required cores, the distance for adding a completely new

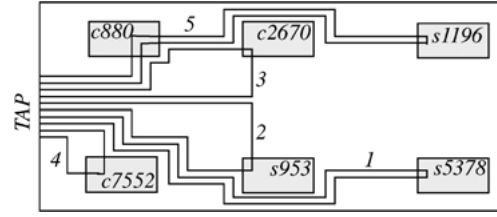


Fig. 13. TAM design using our heuristic on System S.

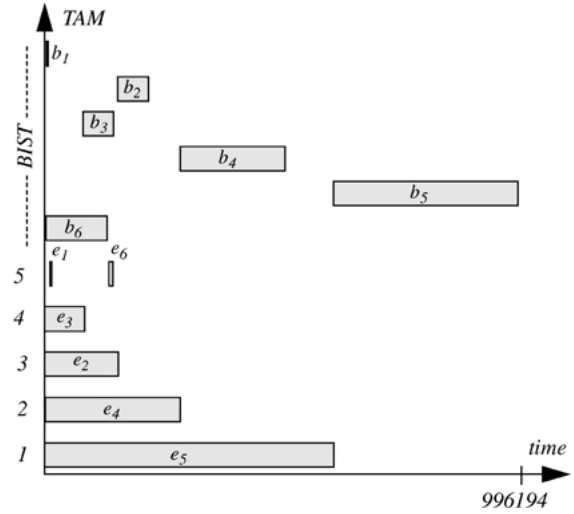


Fig. 14. TAM schedule on System S using our heuristic.

connection is re-calculated due to a possible moving of test resources.

Examples of the produced results from the algorithm using System S [4] (Table 1) are the TAM design as in Fig. 13 and the test schedule as in Fig. 14. The TAM wires 1 to 5 in Fig. 13 correspond to the TAM 1 to 5 in Fig. 14. For instance,  $b_5$  is the BIST test of core indexed 5 (s5378) and  $e_5$  is the external test of s5378 (note that the BIST tests  $b_i$  do not require a TAM but they are placed in Fig. 14 to illustrate when they are scheduled).

The computational complexity for the above algorithm, where the test access mechanism design is excluded in order to make it comparable with other approaches, comes mainly from sorting the tests and the two loops. The sorting can be performed using a sorting algorithm at  $O(n \times \log n)$ . The worst case occurs when in each loop iteration for the loops only one test is scheduled giving a complexity:

$$\sum_{i=0}^{|T|-1} (|T| - i) = \frac{n^2}{2} + \frac{n}{2}$$

The total worst case execution time is  $n \times \log n + n^2/2 + n/2$ , which is of  $O(n^2)$ . For instance, the approach by Garg et al. [11] and by Chakrabarty [4] both has a worst case complexity of  $O(n^3)$ .

## 6. Simulated Annealing

In this section we outline the Simulated Annealing (SA) technique and describe its adoption to be used for scheduling and TAM design. The technique proposed by Kirkpatrick et al. [16] uses a hill-climbing mechanism to avoid getting stuck in at local optimum.

### 6.1. The Simulated Annealing Algorithm

The SA algorithm (Fig. 15) starts with an initial solution and a minor modification creates a neighbouring solution. The cost of the new solution is evaluated and if it is better than the previous, the new solution is kept. A worse solution can be accepted at a certain probability, which is controlled by a parameter referred to as temperature.

The temperature is decreased during the optimization process, and the probability of accepting a worse solution decreases with the reduction of the temperature value. The optimization terminates when the temperature value is approximately zero.

### 6.2. Initial Solution and Parameter Selection

We use our heuristic described in Section 5 with an initial sorting of the tests based on *power* (using *time* and *power*  $\times$  *time* results after optimization in the same cost)

```

1: Construct initial solution,  $x^{now}$ ;
2: Initial Temperature:  $T=TI$ ;
3: while stop criteria not met do begin
4:   for  $i = 1$  to  $TL$  do begin
5:     Generate randomly a neighboring solution
        $x' \in N(x^{now})$ ;
6:     Compute change of cost function
        $\Delta C = C(x') - C(x^{now})$ ;
7:     if  $\Delta C \leq 0$  then  $x^{now} = x'$ 
8:     else begin
9:       Generate  $q = \text{random}(0, 1)$ ;
10:      if  $q < e^{-\Delta C/T}$  then  $x^{now} = x'$ 
11:    end;
12:   end;
13:   Set new temperature  $T = \alpha \times T$ ;
14: end;
15: Return solution corresponding to the minimum
    cost function;
```

Fig. 15. Simulated Annealing algorithm.

within the integrated test framework (Section 5) to create the initial solution [17, 18]. An example of an initial solution produced for System S is in Fig. 13 and Fig. 14.

The parameters, initial temperature  $TI$ , the temperature length  $TL$  and the temperature reduction factor  $\alpha$  ( $0 < \alpha < 1$ ) are all determined based on experiments.

### 6.3. Neighbouring Solution in Test Scheduling

In the case when only test scheduling is considered, i.e. the TAM is not considered or it is fixed and seen as a resource, we create a neighbouring solution by randomly selecting a test from an existing schedule and schedule it as soon as possible but not at the same place as it was in the original schedule. For instance, creating a neighbouring solution given a test schedule as in Fig. 6 with resource graph as in Fig. 1 and test compatibility graph as in Fig. 2, we randomly select a test, let say  $t_1$ . We try to schedule  $t_1$  as soon as possible but not with the same starting time as it had while fulfilling all constraints. Test  $t_1$  was scheduled to start at time 0 and no new starting point exists where constraints are fulfilled until end of  $t_3$  where  $t_1$  now is scheduled. In this case, the test time increases after the modification (getting out of a possible local minimum), however, only temporarily since in the next iteration a test may be scheduled at time 0 (where  $t_1$  used to be).

### 6.4. Neighbouring Solution in Test Scheduling and TAM Design

When both the test time and the TAM design are to be minimized, a neighbouring solution is created by randomly adding or deleting a wire and then the tests are scheduled on the modified TAM.

If the random choice is to add a wire, a test is randomly selected and a wire is added from its required test source to the core where the test is applied and from the core to the test sink for the test. For instance, if  $e_3$  in System S (Table 1) is selected, a wire is added from the TAP to core  $c7552$  and from core  $c7552$  to the TAP.

If the random choice is to delete a wire, a similar approach is applied. However, a check is performed to make sure that all tests can be applied.

### 6.5. Cost Function

The cost function of a test schedule,  $S$ , and the TAM,  $A$ , is:

$$C(S, A) = \beta_1 \times T(S) + \beta_2 \times L(A)$$

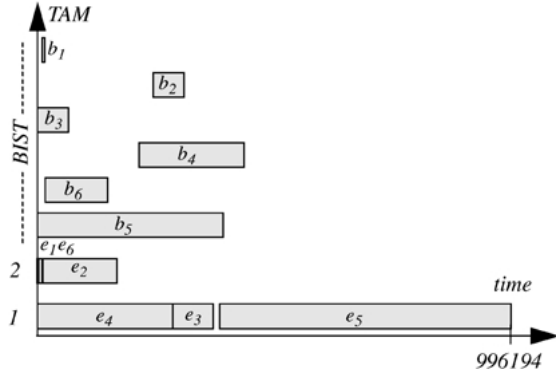


Fig. 16. Test schedule on System S using SA.

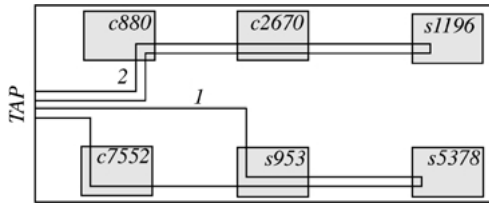


Fig. 17. TAM design using SA on System S.

where:  $T(S)$  is the test application time for a sequence of tests,  $S$ ,  $L(A)$  is the total length of the TAM,  $\beta_1, \beta_2$  are two designer-specified constants used to determine the importance of the test time and the TAM.

The test application time,  $T(S)$ , for a schedule,  $S$ , is:

$$T(S) = \{\max\{t_{end}(t_i) \mid \forall t_i(\max\{t_{end}(t_i)\}), t_i \in S\}\}$$

and the length,  $L(A)$ , of the TAM,  $A$ , is given by:

$$\sum_{w_j \in A} \sum_{j=0}^{|w_i|-1} dist(v_j, v_{j+1}), v_j, v_{j+1} \in w_i$$

For the test schedule,  $S$ , produced by SA for System S (Fig. 16) the test time,  $T(S)$  is 996194 (the end time of test  $e_5$ ) and the length of the TAM (Fig. 17) is 160. Comparing this to the results produced by our heuristic [18] shows that test time is the same while the TAM is reduced from 320 (Fig. 13) to 160 (Fig. 17).

## 7. Experimental Results

### 7.1. Benchmarks

We have used the System S [4], which has test conflicts (Table 1) while all other benchmarks and designs have test conflicts and power constraints like the ASIC Z

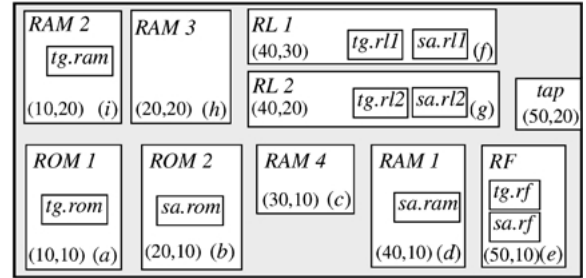


Fig. 18. ASIC Z floor-plan.

design presented by Zorian [27] with added data made by Chou et al. [9] (see the floor-plan in Fig. 18) and we added the placement  $(x, y)$  coordinates [18]. For instance, RAM2 is placed at  $(10, 20)$ , which means that the centre of RAM2 has  $x$ -coordinate 10 and  $y$ -coordinate 20. The design is fully BISTed with a power dissipation limit at 900 mW.

We have also used an extended ASIC Z design where each core is tested by two test sets (one external test and one BIST) and an interconnection test to a neighbouring core [17]; in total 27 tests.

We have also used a design with 10 tests presented by Muresan et al. [23] and an industrial design with characteristics given in Table 2. The power limitation for the industrial design example is 1200 mW and only one test may use the test bus or the functional pins (fp) at a time. Furthermore block-level tests may not be scheduled concurrently with top-level tests.

Table 2. Characteristics for the industrial design.

Test	Block	Test	Test time	Test power	Test port	
Block-level tests	A	Test A	515	379	Scan	
	B	Test B	160	205	Testbus	
	C	Test C	110	23	Testbus	
	E	Test E	61	57	Testbus	
	F	Test F	38	27	Testbus	
	I	Test I	29	120	Testbus	
	J	Test J	6	13	Testbus	
	K	Test K	3	9	Testbus	
	L	Test L	3	9	Testbus	
	M	Test M	218	5	Testbus	
	Top-level tests	A	Test N	232	379	fp
		N	Test O	41	50	fp
		B	Test P	72	205	fp
D		Test Q	104	39	fp	

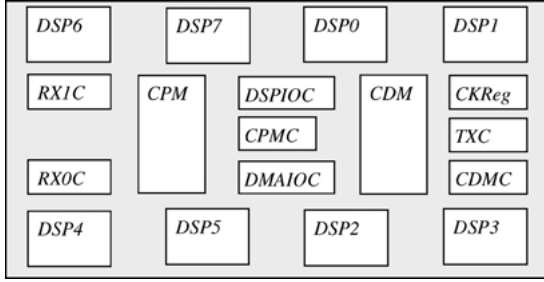


Fig. 19. The Ericsson design.

The largest design is the Ericsson design [17, 19] consisting of 8 DSP cores plus additional logic cores and memory banks, see Fig. 19. Design characteristics are in Table 3 where the following notations are used:

- $n$ : DSP core ( $0 \leq n \leq 7$ ),
- $i$ : common program memory (CPM) bank ( $0 \leq i \leq 7$ ),
- $j$ : common data memory (CDM) bank ( $0 \leq j \leq 9$ ),
- $l$ : local data memory (LDM) at a DSP core ( $0 \leq l \leq 3$ ),
- $m$ : local memory (LZM) bank at a DSP core ( $0 \leq m \leq 1$ ).

All logic blocks in the Ericsson design are tested by two test sets, one using external tester and one using on-chip resources, while memories are tested with one test set; in total 170 tests. The test access port may be used by more than one test concurrently. However, the other test resources cannot be used concurrently. Furthermore, only one test set may be applied concurrently to each block and maximal power dissipation is 5125 mW. For the implementation, we have simplified our system model (Section 3) regarding the TAM wire design and only allowing a single wire per test. When discussing about our algorithm we use *our1*, *our2* and *our3*, which corresponds to the initial sorting based on *test power*( $p$ ), *test time*( $t$ ) and *test power*  $\times$  *test time*( $p \times t$ ).

Unless stated, we use partitioned testing with run to completion, for the cost function (Section 6.5)  $\beta_1 = \beta_2 = 1$  and we have used a Sun Ultra10, 450 MHz CPU, 256 MB RAM.

## 7.2. Test Scheduling

We have compared our algorithm (nonpartitioned testing) with the nonpartitioned testing approaches proposed by Zorian [27] and Chou et al. [9]. We have used

Table 3. The Ericsson design characteristics.

Block	Test number	Test time	Test power	Test source	Test sink
RX0C	1	970	375	TAP	TAP
	2	970	375	TG <sub>0</sub>	TRA <sub>0</sub>
RX1C	3	970	375	TAP	TAP
	4	970	375	TG <sub>0</sub>	TRA <sub>0</sub>
DSPIOC	5	1592	710	TAP	TAP
	6	1592	710	TG <sub>0</sub>	TRA <sub>0</sub>
CPMC	7	480	172	TAP	TAP
	8	480	172	TG <sub>0</sub>	TRA <sub>0</sub>
DMAIOC	9	3325	207	TAP	TAP
	10	3325	207	TG <sub>0</sub>	TRA <sub>0</sub>
CKReg	11	505	118	TAP	TAP
	12	505	118	TG <sub>0</sub>	TRA <sub>0</sub>
CDMC	13	224	86	TAP	TAP
	14	224	86	TG <sub>0</sub>	TRA <sub>0</sub>
TXC	15	364	140	TAP	TAP
	16	364	140	TG <sub>0</sub>	TRA <sub>0</sub>
CPM <sub><math>i</math></sub>	$17 + i$	239	80	TG <sub>1</sub>	TRA <sub>1</sub>
CDM <sub><math>j</math></sub>	$25 + j$	369	64	TG <sub>1</sub>	TRA <sub>1</sub>
DSP <sub><math>n</math></sub>					
LPM	$35 + 17 \times n$	46	16	TG <sub><math>n,0</math></sub>	TRA <sub><math>n,0</math></sub>
LDM <sub><math>l</math></sub>	$36 + 17 \times n + 1$	92	8	TG <sub><math>n,0</math></sub>	TRA <sub><math>n,0</math></sub>
LZM <sub><math>m</math></sub>	$40 + 17 \times n + m$	23	2	TG <sub><math>n,0</math></sub>	TRA <sub><math>n,0</math></sub>
Logic <sub>0</sub>	$17 \times n + 42$	4435	152	TAP	TAP
	$17 \times n + 43$	4435	152	TG <sub><math>n,1</math></sub>	TRA <sub><math>n,1</math></sub>
Logic <sub>1</sub>	$17 \times n + 44$	4435	152	TAP	TAP
	$17 \times n + 45$	4435	152	TG <sub><math>n,1</math></sub>	TRA <sub><math>n,1</math></sub>
Logic <sub>2</sub>	$17 \times n + 46$	7009	230	TAP	TAP
	$17 \times n + 47$	7009	230	TG <sub><math>n,1</math></sub>	TRA <sub><math>n,1</math></sub>
Logic <sub>3</sub>	$17 \times n + 48$	7224	250	TAP	TAP
	$17 \times n + 49$	7224	250	TG <sub><math>n,1</math></sub>	TRA <sub><math>n,1</math></sub>
Logic <sub>4</sub>	$17 \times n + 50$	7796	270	TAP	TAP
	$17 \times n + 51$	7796	270	TG <sub><math>n,1</math></sub>	TRA <sub><math>n,1</math></sub>

the same assumptions as Chou et al. and the results are in Table 4. Our approaches (*our1*, *our2*, and *our3*) results, in all cases, in a test schedule with three test sessions ( $ts$ ) at a test time of 300 time units, which is 23% better than Zorian's approach and 9% better than the approach by Chou et al.

In System S, no power constraints are given and therefore only *our2* can be used. Our approach finds using partitioned testing with run to completion after 1 second the optimal solution; see Table 5 (first group).

Table 4. ASIC Z test scheduling.

ts	Zorian		Chou et al.		Our1, Our2, Our3	
	Cores	Time	Cores	Time	Cores	Time
1	RAM1, RAM4, RF	69	RAM1, RAM3, RAM4, RF	69	RL2, RL1, RAM2	160
2	RL1, RL2	160	RL1, RL2	160	RAM1, ROM1, ROM2	102
3	RAM2, RAM3	61	ROM1, ROM2, RAM2	102	RAM3, RAM4, RF	38
4	ROM1, ROM2	102				
Test time		392		331		300

The results on the industrial design are in Table 5 (second group) where the industrial designer's solution is 1592 time units while our test scheduling achieve a test time of 1077 time units, the optimum, in all cases

Table 5. Test scheduling results.

Design	Approach	Test time	Difference to SA/optimum (%)	CPU (sec)
System S [4]	Optimal solution	1152180	-	-
	Chakrabarty	1204630	4.5	
	Our2 ( $t$ )	1152180	0	1
Industrial design	Optimal solution	1077	-	-
	Designer	1592	47.8	-
	Our1 ( $p$ )	1077	0	1
	Our2 ( $t$ )	1077	0	1
	Our3 ( $p \times t$ )	1077	0	1
Muresan [23]	SA	25	-	90
	Muresan [23]	29	16	-
	Our1 ( $p$ ) [18]	28	12	1
	Our2 ( $t$ ) [18]	28	12	1
	Our3 ( $p \times t$ ) [18]	26	4	1
ASIC Z (1)	SA	262	-	74
	Our1 ( $p$ )	262	0	1
	Our2 ( $t$ )	262	0	1
	Our3 ( $p \times t$ )	262	0	1
ASIC Z (2)	SA	274	-	223
	Our1 ( $p$ ) [18]	300	10	1
	Our2 ( $t$ ) [18]	290	6	1
	Our3 ( $p \times t$ ) [18]	290	6	1
Extended ASIC Z (3)	SA	264	-	132
	Our1 ( $p$ )	313	18	1
	Our2 ( $t$ )	287	9	1
	Our3 ( $p \times t$ )	287	9	1
Ericsson	SA	30899	-	3260
	Our1 ( $p$ )	37336	20	3
	Our2 ( $t$ )	34762	12	3
	Our3 ( $p \times t$ )	34762	12	3

(our1, our2, and our3), which is 32.3% better than the designer's solution.

The results on design Muresan are in the third group of Table 5. The test time using the approach by Muresan et al. is 29 time units and the results using our approaches our1, our2, and our3 are 28, 28 and 26, respectively, all produced within 1 sec. Our SA (TI=400, TL=400,  $\alpha=0.97$ ) improves to 25 time units using 90 seconds.

When not considering idle power on ASIC Z, the test schedules using our1, our2, and our3 (fourth group in Table 5) all result in a test time of 262. The SA (TI=400, TL=400 and  $\alpha=0.97$ ) did not find a better solution.

In the experiments considering idle power (fifth group of Table 5), our heuristic approaches our1, our2, and our3 resulted in a solution of 300, 290 and 290, respectively, each produced within 1 second. The SA (TI=400, TL=400 and  $\alpha=0.99$ ) produced a solution of 274 requiring 223 sec., i.e. a cost improvement in the range of 6% to 10%.

The results on Extended ASIC Z when not considering idle power are 313 (our1), 287 (our2) and 287 (our3) (sixth group in Table 5), which were produced by our heuristic after 1 second. The SA optimization (TI=TL=400,  $\alpha=0.97$ ) produced a solution at a cost of 264 running for 132 seconds, i.e. a cost improvement in the range of 9% to 18%.

The results on the Ericsson design (seventh group of Table 5) are 37226, 34762, 34762 produced by our heuristic our1, our2, and our3 (within 3 sec.). The SA algorithm (TI=200, TL=200,  $\alpha=0.95$ ) produced a solution at 30899 after 3260 seconds.

### 7.3. Test Resource Placement

In the ASIC Z design all cores have their own dedicated BIST structure. Let us assume that all ROM cores

share one BIST structure and all RAM memories share another BIST structure; the rest of the cores have their own dedicated BIST structure. Using our placement strategy the test resources in ASIC Z will be placed as in Fig. 18.

#### 7.4. Test Access Mechanism Design

Assume for ASIC Z (Fig. 18) that all tests are scan-based (1 scan-chain per core) applied with an external tester allowing a maximum of 8 scan chains to operate concurrently. The results using our1, our2, and our3 considering idle power are collected in Table 6. The test schedule and the TAM schedule achieved with heuristic our3 are in Fig. 20. The total length of the test access mechanism is 360 units and it is routed as in Fig. 21. All solutions were produced within 1 second.

Table 6. Results on ASIC Z.

Approach	Test time	TAM cost
Our1 ( $p$ )	300	360
Our2 ( $t$ )	290	360
Our3 ( $p \times t$ )	290	360

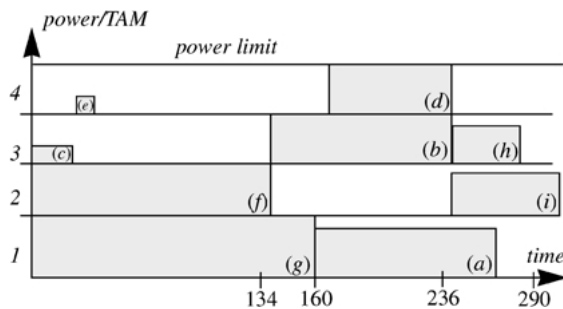


Fig. 20. Test schedule for ASIC Z.

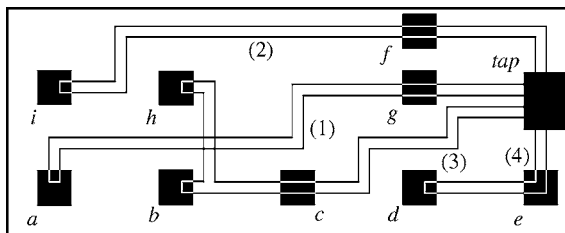


Fig. 21. ASIC Z with test data access mechanism.

Table 7. TAM design and test scheduling.

Approach	System S			ASIC Z		
	Time	TAM	Total	Time	TAM	Total
Naive 1	1541394	100	1641	699	110	809
Naive 2	996194	360	1356	300	500	800
Our1 ( $p$ )	–	–	–	300	360	660
Our2 ( $t$ )	996194	320	1316	290	360	650
Our3 ( $p \times t$ )	–	–	–	290	360	650
SA	996194	160	1156	334	180	514

#### 7.5. Test Scheduling and TAM Design

We have made experiments using System S and ASIC Z to demonstrate the importance of integrating test scheduling and TAM design. The ASIC Z is fully BISTed; however, in this experiment we assume all tests are applied using an external tester able of supporting several tests concurrently. We have used two naive approaches, Naive1 and Naive2. Naive1 uses a minimal TAM design connecting all cores in a ring and Naive 2 uses an extensive TAM where each core gets its own dedicated TAM.

For the cost function, we have for ASIC Z used  $\beta_1 = \beta_2 = 1$  and for System S  $\beta_1 = 1/1000$  and  $\beta_2 = 1$  and the results are collected in Table 7. Naive 1 produces a low cost TAM design but the test time is long leading to high total cost due to that all tests have to be scheduled in a sequence. The total cost of using the approach Naive 2 is also high due to the extensive TAM design. Such extensive TAM gives more flexibility, however, other constraints in the design limits its use. Our approaches (our1, our2, and our3) produces better results indicating the importance of considering TAM design and test scheduling in an integrated manner. The TAM design (Fig. 13) and the test schedule (Fig. 14) achieved using our heuristic for System S (Table 1) have a test time of 996194 and a TAM length of 320 computed within 1 second. The SA (TI = TL = 100,  $\alpha = 0.99$ ) was running for 1004 seconds producing a test schedule (Fig. 16) and a TAM design (Fig. 17) with a test time of 996194 and a TAM length of 160, a TAM improvement of 50%. For ASIC Z, the SA (TI = TL = 300,  $\alpha = 0.97$ ) produced after 855 seconds a solution with a cost of 514 (334 for test time and 180 for TAM).

The results comparing our heuristic with SA are collected in Table 8 where, for instance, our heuristic our1 produced a solution for ASIC Z with a total cost of 660 (a test time of 290 and a TAM cost of 360)

Table 8. TAM and scheduling results.

Approach	SA	Our1	Our2	Our3
<b>ASIC Z</b>				
Test time	334	300	290	290
Diff to SA	–	–10%	–13%	–13%
TAM cost	180	360	360	360
Diff to SA	–	100%	100%	100%
Total cost	514	660	650	650
Diff to SA	–	28%	21%	21%
Comp. cost	855 sec.	1 sec.	1 sec.	1 sec.
Diff to SA	–	–85400%	–85400%	–85400%
<b>Extended ASIC Z</b>				
Test time	270	313	287	287
Diff to SA	–	16%	6%	6%
TAM cost	560	720	660	660
Diff to SA	–	29%	18%	18%
Total cost	830	1033	947	947
Diff to SA	–	24%	14%	14%
Comp. cost	4549 sec.	1 sec.	1 sec.	1 sec.
Diff to SA	–	–454800%	–454800%	–454800%
<b>Ericsson</b>				
Test time	33082	37336	34762	34762
Diff to SA	–	11%	5%	5%
TAM	6910	8245	9350	8520
Diff to SA	–	19%	35%	23%
Total cost	46902	53826	53462	51802
Diff to SA	–	15%	14%	10%
Comp. cost	15 h	81 sec.	79 sec.	62 sec.
Diff to SA	–	–66567%	–68254%	–86996%

after 1 second. The test time results are in the range of 10% to 13% better using our fast heuristic (in all cases) compared to the SA optimization. However, the TAM results are much worse using our heuristics and the total cost improvements by the SA are in the range from 21% to 28%.

The results from experiments on Extended ASIC Z are in Table 8 (second group). Our heuristic our1 produced a solution after 1 second with a test time of 313 and a TAM cost of 720, resulting in a total cost of 1033. The solution produced after 4549 seconds by our SA ( $TI = TL = 200$ ,  $\alpha = 0.97$ ) optimization has a test time of 270 and a TAM cost of 560. In this experiment, SA produced a better total cost (range 14% to 24%) as well as better cost regarding test time (range 6% to 16%) and TAM cost (range 18% to 29%). The

results on the Ericsson design are collected in Table 8 (third group). For instance, our heuristic our1 results in a solution with a test time of 37336 and a TAM cost of 8245, which took 81 seconds to produce. The total cost is 53826 when using  $\beta_1 = 1$  and  $\beta_2 = 2$ . The SA ( $TI = TL = 200$ ,  $\alpha = 0.95$ ) optimization produced a solution with a test time of 33082 and a TAM cost of 6910 after 15 hours. In all cases, the SA produces better results. Regarding test time the SA improvement is in the range from 5% to 11%, for the TAM cost in the range from 19% to 35% and the total cost in the range from 10% to 15%.

For all experiments with the SA, the computational cost is extremely higher compared to our heuristics. A finer tuning of the SA parameters could reduce it, however, the extensive optimization is only used for the final design and therefore a high computational cost can be accepted.

## 8. Conclusions

For complex systems such as SOCs, it is a difficult problem for the test designer to develop an efficient test solution due to the large number of factors involved. The work-flow consists of two consecutive parts: an early design space exploration and an extensive optimization for the final solution. In this paper we have proposed a framework suitable for these two parts where test scheduling, test access mechanism design, test set selection and test resource placement are considered in an integrated manner minimizing the test time and the size of the test access mechanism while satisfying test conflicts and test power constraint. For the early design space exploration, we have implemented an algorithm running at a low computational cost, which is suitable to be used iteratively many times. For the final solution, a more extensive optimization can be justified and we have proposed and implemented a technique based on Simulated Annealing for test scheduling and test access mechanism design.

We have performed several experiments on benchmarks and industrial designs to show the efficiency and usefulness of our approach.

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