

On logic programming and locating errors in programs

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Outline

Logic Programming (LP) is **declarative**

We can do declarative programming in Prolog

Debugging should be declarative too

Methods exist:

Declarative Diagnosis (DD), a.k.a. algorithmic debugging
[Shapiro'83, Pereira'86, Naish,...]

Tools do not ☹

We discuss the (possibly) main reason for non-acceptance of DD

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Outline

- ▶ Introduction to Logic Programming (LP)
- ▶ On proving program correctness (and completeness),
i.e. how to reason about our programs
- ▶ Approximate specifications
- ▶ Declarative Diagnosis (DD)
Why abandoned; a cure
Inadequacy of Prolog debuggers
- ▶ Summary

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Declarative programming

WHAT to compute

Program – a **description of the problem**

not a description of computer actions

Logic Programming

<p>Program – a set of axioms Results – its logical consequences Computation – proof construction</p>
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Main programming language – Prolog

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LP. Two levels of reading a program

declarative – a set of axioms,
operational – a description of computations.

ALGORITHM = LOGIC + CONTROL

[Robert Kowalski, 1974]

Operational level (prog. lang. Prolog): control information
 (the ordering within the program, some special constructs).

Important:, often **neglected**:

The two levels can be considered separately.

👉 Program correctness is a property of the declarative level.

We do not need to reason in terms of von Neumann machine.
 J.Backus, *Can programming be liberated from the von Neumann style?* CACM, 1978

(One may also program operationally, neglecting the 1st level.)

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Program correctness

How to reason about program results ?

Imperative
 programming:

partial correctness + termination

LP :

correctness completeness
 ↙ ↘
 full correctness (?)

Correctness –

the program answers compatible with the specification

Completeness – all the required answers will be produced
 (by the specification)

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Reasoning about program correctness

Specification – a set S of ground atoms (a Herbrand interpretation)

Correctness (of P) – each ground answer (of P) $\in S$: $\boxed{\mathbf{M}_P \subseteq S}$

Correctness proving method:

$S \models P \Rightarrow P \text{ correct w.r.t. } S.$

↑

For each ground instance $H \leftarrow B_1, \dots, B_n$ of a clause from P ,
 if $B_1, \dots, B_n \in S$ then $H \in S$.

(Out of atoms $\in S$, the rules of P produce only atoms $\in S$)

The method has been already informally applied at this presentation.

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Reasoning about program completeness

Completeness (of P w.r.t. S) – each atom $\in S$ is an answer of P

$\boxed{S \subseteq \mathbf{M}_P}$

Completeness proving method

Main part of the sufficient condition – reverse of that for correctness

If $H \in S$ then

(*) there exists a ground instance $H \leftarrow B_1, \dots, B_n$ of a clause from P
 s.that $B_1, \dots, B_n \in S$.

(Each atom of S can be produced by a rule of P from atoms of S .)

The two methods much simpler than those for proving
 correctness of imperative programs !

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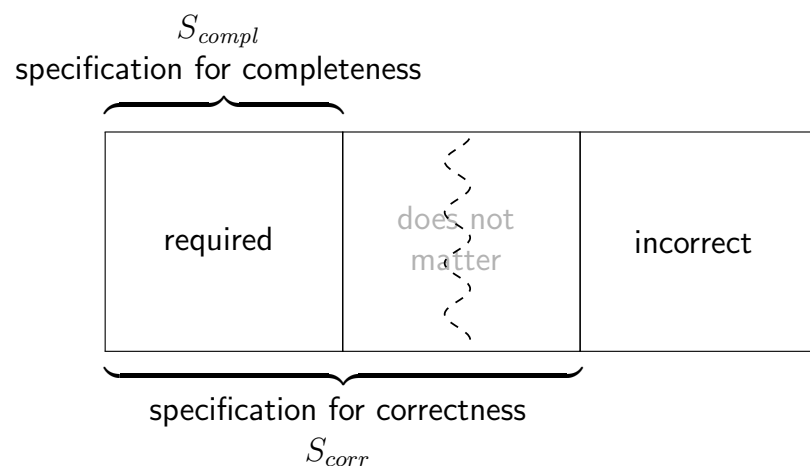
Important feature

Exact specification – often not known. E.g.

- ▶ $\text{member}(e, t)$ for a non-list t ,
- ▶ $\text{append}(l, t, t')$ for non-lists t, t' ,
- ▶ $\text{insert}(e, l, y)$ in insertion sort, for unsorted l ,
- ▶ a predicate may have **distinct** semantics in distinct versions of a program under development!
(see Howe&King SAT solver in [D...,TPLP2018])

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Approximate specifications



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Approximate specifications, example

Ex.: specification for $\text{member}/2$:

$$S_{corr} = S_{compl} \cup \{\text{member}(e, t) \mid t \text{ not a list}\},$$

S_{compl} – the list membership relation, i.e.

$$S_{compl} = \{\text{member}(t_i, [t_1, \dots, t_n]) \mid 1 \leq i \leq n\}.$$

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Declarative diagnosis (DD) a.k.a. algorithmic debugging

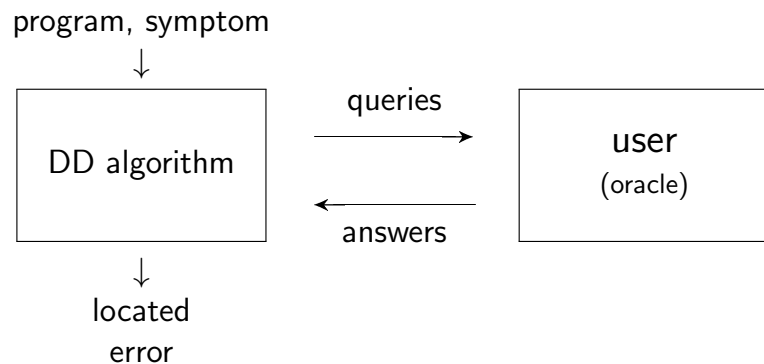
Methods of locating errors in programs,
based solely on the declarative semantics.

[Shapiro'83, Pereira'86, Naish,...]
[S.Nadjm-Tehrani, W.Drabent, J.Małuszyński,
H.Nilsson, N.Shahmehri, M.Kamkar, P.Fritzson,
R.Westman, P.Bunus, M.Sjölund]

The methods exist, but are abandoned.

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DD (Declarative Diagnosis)



Queries – about the intended declarative semantics of the program

User can locate the error **without looking at the program**
solely in terms of declarative semantics

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Examples – DD of incorrectness

Diagnosis sessions, to be shown after the first two items of the next slide

* A buggy insertion sort program [Shapiro'83]

* An actual bug in a rather big student program (from TDDD08, lab)

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Reasons for DD being neglected

- ▶ No freedom: Fixed order or queries to answer
- ▶ The user cannot change her mind
- ▶ ...
- ▶ **Exact** specification (*intended model*) required from the user But often she does not know it (and it does not matter)
 - ▶ `member(e, t)` for a non-list t ,
 - ▶ `append(l, t, t')` for non-lists t, t' ,
 - ▶ `insert(e, l, y)` in insertion sort, for unsorted l ,
 - ▶ a predicate may have **distinct** semantics in distinct versions of a program under development!

(see Howe&King SAT solver in [D...,TPLP2018])

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Instead of “the intended model” the user knows

- ▶ its certain superset S_{corr} – what may be computed
- ▶ and a subset S_{compl} – what must be computed

i.e. an **approximate specification**

The program should be **correct** w.r.t. S_{corr} and **complete** w.r.t. S_{compl} :

$$S_{compl} \subseteq \mathbf{M}_P \subseteq S_{corr}$$

The standard Declarative Diagnosis works!

when instead of the intended model we use

- ▶ S_{corr} for incorrectness diagnosis
- ▶ S_{compl} for incompleteness diagnosis

Apparently, this simple fact has been unnoticed

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Prolog debuggers

Prolog debugging tools – based solely on operational semantics

Worse, they are “declarative-programmer-unfriendly” ☹️

Difficult to obtain info about e.g.

Which answers to a query A have been obtained?

What is the proof tree for a given obtained answer?

(i.e. which “local” answers contributed to a given “top level” answer?)

We **need** tools for DD for Prolog.

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A basic tool for DD of incorrectness

Not an implementation of a DD algorithm,
but a proof tree browser.

A simple prototype.

(Used in the example diagnosis sessions.)

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Summary. This work dealt with some basic issues of LP

- ▶ Simple method for proving correctness (old [Clark'79], but neglected)
- ▶ Proving completeness. (Hardly anybody has dealt with this previously)
- ▶ The usefulness of approximate specifications
- ▶ Explaining & solving the main (?) problem with DD
- ▶ A study when least Herbrand models exactly characterize programs, a sufficient and necessary condition.

* W. Drabent. “Logic + control: On program construction and verification.” TPLP, 2018

* W. Drabent. “Correctness and Completeness of Logic Programs.” ACM TOCL, 2016

* W. Drabent. “On definite program answers and least Herbrand models.” TPLP, 2016

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Conclusions

Declarative programming in Prolog possible;

reasoning about correctness / completeness
error diagnosis

can be dealt with declaratively (abstracting from operational semantics)

Proof methods for correctness/completeness can be used
more or less formally by programmers

At the informal end

they show how to reason about our programs
in a systematic / orderly way.

To be applied in everyday programming

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