# On logic programming and locating errors in programs

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## Outline

- Introduction to Logic Programming (LP)
- On proving program correctness (and completeness), i.e. how to reason about our programs
- Approximate specifications

Outline 2 LP Correctness DD Summary

- Declarative Diagnosis (DD)
   Why abandoned; a cure
   Inadequacy of Prolog debuggers
- Summary

### Outline

Logic Programming (LP) is declarative

We can do declarative programming in Prolog

Debugging should be declarative too

#### Methods exist:

Declarative Diagnosis (DD), a.k.a. algorithmic debugging [Shapiro'83,Pereira'86,Naish,...]

Tools do not  $\stackrel{\cdot\cdot}{\sim}$ 

We discuss the (possibly) main reason for non-acceptance of DD

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Outline 2 LP Correctness DD Summary Ex. ex.program Logic+control

## Declarative programming

#### WHAT to compute

Program – a description of the problem

not a description of computer actions

### **Logic Programming**

Program – a set of axioms Results – its logical consequences Computation – proof construction

Main programming language – Prolog

# Logic Programming (LP). The core part

Outline 2 LP Correctness DD Summary

Program – a set of axioms (of the form  $A_0 \leftarrow A_1, \ldots, A_n$  $A_i$  – atoms (atomic formulae)).

Computation – search for logical consequences of the program.

Query Q (of the form  $A_1, \ldots, A_n$ ). Answers  $Q\theta$  such that  $P \models Q\theta$  $(P - \text{the program, } \theta - \text{substitution}).$ 

Any answer Q' computed for P is a logical consequence of P,  $P \models Q'$ .

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And conversely

(if  $P \models Q\theta$  then  $Q\theta$  is an instance of a computed answer for Q).

Note: untyped logic

# LP, example, puzzle

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Build a sequence out of three 1's, three 2's, ..., three 9's, so that between each consecutive occurrences of i there are exactly i elements.

[1,9,1,2,1,8,2,4,6,2,7,9,4,5,8,6,3,4,7,5,3,9,6,8,3,5,7]

 $\begin{bmatrix} 1,8,1,9,1,5,2,6,7,2,8,5,2,9,6,4,7,5,3,8,4,6,3,9,7,4,3 \end{bmatrix} \\ \begin{bmatrix} 1,9,1,6,1,8,2,5,7,2,6,9,2,5,8,4,7,6,3,5,4,9,3,8,7,4,3 \end{bmatrix} \\ \begin{bmatrix} 3,4,7,8,3,9,4,5,3,6,7,4,8,5,2,9,6,2,7,5,2,8,1,6,1,9,1 \end{bmatrix} \\ \begin{bmatrix} 3,4,7,9,3,6,4,8,3,5,7,4,6,9,2,5,8,2,7,6,2,5,1,9,1,8,1 \end{bmatrix} \\ \begin{bmatrix} 7,5,3,8,6,9,3,5,7,4,3,6,8,5,4,9,7,2,6,4,2,8,1,2,1,9,1 \end{bmatrix}$ 

Variables in programs - begin with upper case

LP Correctness DD Summarv

\_ – anonymous variable (each occurrence of \_ – a distinct variable)

Ex. ex.program Logic+cont

 $[a_1,\ldots,a_n]$  – list, its elements  $a_1,\ldots,a_n$   $(n \ge 0)$ 

[] – empty list

[h|t] – the list with head h and tail t

 $[h_1,h_2|t]$  – the list with head  $h_1$  and tail  $[h_2|t]$ , i.e.  $[h_1|[h_2|t]]$ 

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Ex ex program Logic+co

YZ

# LP, example, puzzle

 $solution(S) \leftarrow$ XYZsequence 27(S),sublist([1, \_, 1, \_, 1], S), н sublist([2, \_, \_, 2, \_, \_, 2], S), Msublist([3, \_, \_, \_, 3, \_, \_, 3], S), sublist([4, -, -, -, -, 4, -, -, -, 4], S),sublist([5, -, -, -, -, 5, -, -, -, 5], S), sublist([7, -, -, -, -, -, -, 7, -, -, -, -, -, 7], S), sublist([8, -, -, -, -, -, -, 8, -, -, -, -, -, 8], S), sublist([9, ..., ..., ..., ..., ..., ..., 9, ..., ..., ..., ..., 9], S). $sublist(Y, XYZ) \leftarrow app(\_, YZ, XYZ), app(Y, \_, YZ).$ app([], L, L). $app([H|K], L, [H|M]) \leftarrow app(K, L, M).$ 

#### Outline 2 LP Correctness DD Summary Ex. ex.program Logic+control

### LP. Two levels of reading a program

declarative – a set of axioms, operational – a description of computations.

ALGORITHM = LOGIC + CONTROL

[Robert Kowalski, 1974]

Operational level (prog. lang. Prolog): control information (the ordering within the program, some special constructs).

#### Important:, often neglected:

The two levels can be considered separately.

Program correctness is a property of the declarative level.

We do not need to reason in terms of von Neumann machine. J.Backus, *Can programming be liberated from the von Neumann style*? CACM, 1978

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(One may also program operationally, neglecting the 1st level.)

### Reasoning about program correctness

Specification – a set S of ground atoms (a Herbrand interpretation)

Correctness (of P) – each ground answer (of P)  $\in S$ :  $|\mathbf{M}_P \subseteq S|$ 

Correctness proving method:

$$S \models P \implies P \text{ correct w.r.t. } S.$$

For each ground instance  $H \leftarrow B_1, \ldots, B_n$  of a clause from P, if  $B_1, \ldots, B_n \in S$  then  $H \in S$ .

(Out of atoms  $\in S$ , the rules of P produce only atoms  $\in S$ )

The method has been already informally applied at this presentation.

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method 1 method 2

# Program correctness



Outline 2 LP Correctness DD Summary

Imperative programming: partial correctness + termination LP: correctness completeness full correctness (?)

#### Correctness -

the program answers compatible with the specification

Completeness – all the required answers will be produced (by the specification)

# Reasoning about program completeness

Correctness DD

Completeness (of P w.r.t. S) – each atom  $\in S$  is an answer of P

 $S \subseteq \mathbf{M}_P$ 

#### Completeness proving method

Main part of the sufficient condition - reverse of that for correctness

If  $H \in S$  then

(\*) there exists a ground instance  $H \leftarrow B_1, \ldots, B_n$  of a clause from P s.that  $B_1, \ldots, B_n \in S$ .

(Each atom of S can be produced by a rule of P from atoms of S.)

The two methods much simpler than those for proving correctness of imperative programs !

#### Outline 2 LP Correctness DD Summary method 1 method 2 Approximate

## Approximate specifications, example

Exact specification – often not known. E.g.

- member(e, t) for a non-list t,
- append(l, t, t') for non-lists t, t',
- insert(e, l, y) in insertion sort, for unsorted l,
- a predicate may have distinct semantics in distinct versions of a program under development!

(see Howe&King SAT solver in [D...,TPLP2018])

- **Ex.**: specification for member/2:  $S_{corr} = S_{compl} \cup \{ \text{member}(e, t) \mid t \text{ not a list} \},$ 
  - $S_{compl}$  the list membership relation, i.e.  $S_{compl} = \{ \text{member}(t_i, [t_1, \dots, t_n]) \mid 1 \le i \le n \}.$



# Approximate specifications



Declarative diagnosis (DD) a.k.a. algorithmic debugging

Methods of locating errors in programs, based solely on the declarative semantics.

[Shapiro'83, Pereira'86, Naish,...] [S.Nadjm-Tehrani, W.Drabent, J.Małuszyński, H.Nilsson, N.Shahmehri, M.Kamkar, P.Fritzson, R.Westman, P.Bunus, M.Sjölund]

The methods exist, but are abandoned.

### DD (Declarative Diagnosis)

Outline 2 LP Correctness DD Summary



Queries - about the intended declarative semantics of the program

User can locate the error without looking at the program solely in terms of declarative semantics

#### Outline 2 LP Correctness DD Summary 🛛 🔿 🥥

# Reasons for DD being neglected

- ▶ No freedom: Fixed order or queries to answer
- The user cannot change her mind
- • •
- Exact specification (*intended model*) required from the user
   But often she does not know it (and it does not matter)
  - member(e, t) for a non-list t,
  - append(l, t, t') for non-lists t, t',
  - insert(e, l, y) in insertion sort, for unsorted l,
  - a predicate may have distinct semantics in distinct versions of a program under development!

(see Howe&King SAT solver in [D...,TPLP2018])

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Outline 2 LP Correctness DD Summary Prolog tool	Outline 2 LP Correctness DD Summary - Prolog tool
Examples – DD of incorrectness	Instead of "the intended model" the user knows
Diagnosis sessions, to be shown after the first two items of the next slide	• its certain superset $S_{corr}$ – what may be computed
	and a subset S <sub>compl</sub> – what must be computed
	i.e. an approximate specification
* A buggy insertion sort program [Shapiro'83]	The program should be correct w.r.t. $S_{corr}$ and complete w.r.t. $S_{compl}$ : $S_{compl} \subseteq \mathbf{M}_P \subseteq S_{corr}$
* An actual bug in a rather big student program (from TDDD08, lab)	The standard Declarative Diagnosis works!
	when instead of the intended model we use
	<ul> <li>S<sub>corr</sub> for incorrectness diagnosis</li> </ul>
	S <sub>compl</sub> for incompleteness diagnosis

Apparently, this simple fact has been unnoticed

# Prolog debuggers

Outline 2 LP Correctness DD Summary

Difficult to obtain info about e.g.

We need tools for DD for Prolog.

Prolog debugging tools - based solely on operational semantics

(i.e. which "local" answers contributed to a given "top level" answer?)

Worse, they are "declarative-programmer-unfriendly"

Which answers to a query A have been obtained?

What is the proof tree for a given obtained answer?

Prolog tool

...

### Summary. This work dealt with some basic issues of LP

- Simple method for proving correctness (old [Clark'79], but neglected)
- Proving completeness. (Hardly anybody has dealt with this previously)
- The usefulness of approximate specifications
- Explaining & solving the main (?) problem with DD
- A study when least Herbrand models exactly characterize programs, a sufficient and necessary condition.
  - \* W. Drabent. "Logic + control: On program construction and verification." TPLP, 2018
  - \* W. Drabent. "Correctness and Completeness of Logic Programs." ACM TOCL, 2016
  - \* W. Drabent. "On definite program answers and least Herbrand models." TPLP, 2016

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Outline 2 LP Correctness DD Summary 🔿 💛 Prolog tool	Outline 2 LP Correctness DD Summary
A basic tool for DD of incorrectness	Conclusions
Not an implementation of a DD algorithm, but a proof tree browser.	Declarative programming in Prolog possible;
	reasoning about correctness / completeness error diagnosis
	can be dealt with declaratively (abstracting from operational semantics)
A simple prototype.	Proof methods for correctness/completeness can be used
(Used in the example diagnosis sessions.)	more or less formally by programmers
	At the informal end they show how to reason about our programs in a systematic / orderly way.
	To be applied in everyday programming