

TDDD55 Lesson 2: GRAMMARS AND FORMAL LANGUAGES

Assignments

- Given the alphabet $A = \{ 1, 2, 3 \}$ and the strings $x = 2, y = 13, z = 323$:
 - What are the strings xz, zyx, z^2, x^7 , and what are their lengths?
 - What are A^1, A^2, A^0
 - Describe A^* and A^+
- Given the following grammar for arithmetic expressions $G(\langle \text{exp} \rangle)$:
$$\begin{aligned} \langle \text{exp} \rangle &::= \langle \text{term} \rangle \mid \langle \text{exp} \rangle + \langle \text{term} \rangle \mid \langle \text{exp} \rangle - \langle \text{term} \rangle \\ \langle \text{term} \rangle &::= \langle \text{factor} \rangle \mid \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \langle \text{term} \rangle / \langle \text{factor} \rangle \\ \langle \text{factor} \rangle &::= (\langle \text{exp} \rangle) \mid \langle \text{ident} \rangle \\ \langle \text{ident} \rangle &::= A \mid B \mid C \dots \mid Z \end{aligned}$$
 - Find derivations and draw a parse tree for the statements:
 $A*B-C, A*(B-C), A/B/C,$ and $-A*B$
 - State the handle in statement form $\langle \text{term} \rangle * \langle \text{factor} \rangle + B/C$
 - State a canonic derivation of one of the statements, in example 2a.
 - Why is $A * \langle \text{exp} \rangle * D$ not in statement form?
 - What are \mathbf{V} (Vocabulary), $\mathbf{\Sigma}$ (Alphabet), and \mathbf{N} (Non-terminals) in this grammar?
 - Describe Σ^+ and $L(G)$. State some string in Σ^+ which is not in $L(G)$.
- Using the grammar in exercise 2, draw the parse tree for the statement
$$A - \langle \text{term} \rangle * B + (\langle \text{term} \rangle)$$
Argue why there is no canonic derivation of the statement.
- Consider the grammar in exercise 2 again.
 - Why can't the grammar be parsed using a topdown LL-parser? What options do we have?
 - Rewrite the grammar so that a leftmost derivation is possible.
 - Derive $A*B-C$ using leftmost derivation and provide the corresponding parse-tree
- Construct a context-free grammar for even integers, which may not begin with zeros (this also applies to a single zero).

6. Given the alphabet $A = \{ a, b, c, d, e, f, g, h, i \}$:
- Construct a context-free grammar for words of one syllable (i.e., words containing exactly one vowel).
 - Construct a context-free grammar for multi-syllable words.
7. Given the alphabet $A = \{ a, b, c \}$: Write regular expressions that describe
- all strings starting with a sequence of zero or several a's followed by an arbitrary number of b's and c's mixed together. The strings finish with another sequence of a's. (Example: aaabbcba, bbca, aa).
 - $a^n b^n c^n$, can this expression be described using a regular expression? If so, write down the regular expression. If not, motivate why.
8. Describe the languages (sets) that the following grammars generate: $\langle S \rangle$ is the start symbol.

a.

$$\begin{aligned} \langle S \rangle & ::= \langle A \rangle \langle A \rangle \\ \langle A \rangle & ::= 1 \langle A \rangle 0 \mid 10 \end{aligned}$$

b.

$$\begin{aligned} \langle S \rangle & ::= 1 \langle S \rangle 0 \mid \langle B \rangle \\ \langle B \rangle & ::= 0 \langle B \rangle 1 \mid \varepsilon \end{aligned}$$

c.

$$\begin{aligned} \langle S \rangle & ::= 1 \langle A \rangle \mid \langle B \rangle 0 \\ \langle A \rangle & ::= 1 \langle A \rangle \mid \langle C \rangle \\ \langle B \rangle & ::= \langle B \rangle 0 \mid \langle C \rangle \langle C \rangle \\ & ::= 1 \langle C \rangle 0 \mid \varepsilon \end{aligned}$$