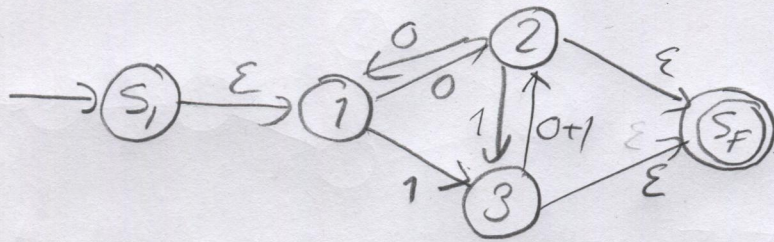


3.5a) Redraw and add new start and final state



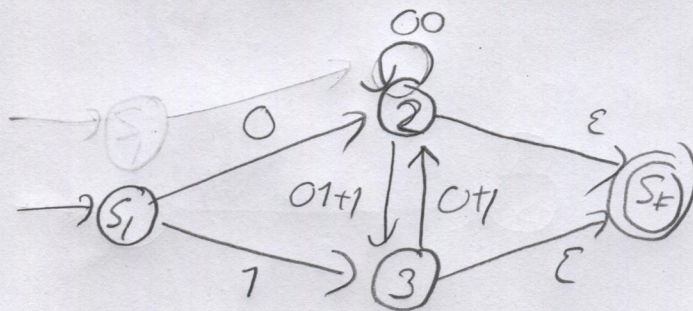
eliminate state 1. There are 4 paths through 1

$$S_1 \rightarrow 1 \rightarrow 2: \epsilon \emptyset^* 0 + \emptyset = 0$$

$$S_1 \rightarrow 1 \rightarrow 3: \epsilon \emptyset^* 1 + \emptyset = 1$$

$$S_2 \rightarrow 1 \rightarrow 2: 0 \emptyset^* 0 + \emptyset = 00$$

$$2 \rightarrow 1 \rightarrow 3: 0 \emptyset^* 1 + 1 = 01 + 1$$



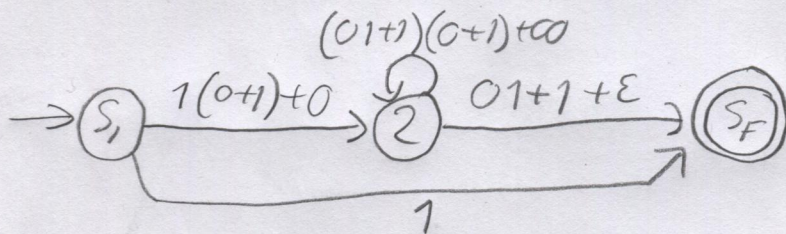
eliminate state 3. There are 4 paths through 3

$$S_1 \rightarrow 3 \rightarrow 2: 1 \emptyset^* (0+1) + 0 = 1(0+1) + 0 =$$

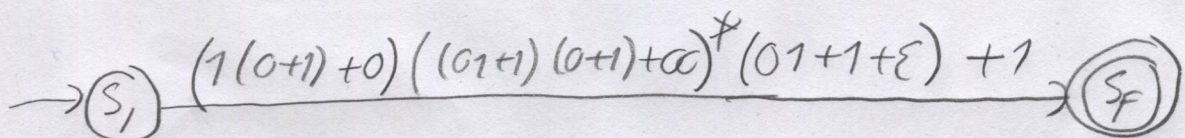
$$S_1 \rightarrow 3 \rightarrow S_F: 1 \emptyset^* \epsilon + \emptyset = 1$$

$$2 \rightarrow 3 \rightarrow 2: (01+1) \emptyset^* (0+1) + 00 = (01+1)(0+1) + 00$$

$$2 \rightarrow 3 \rightarrow S_F: (01+1) \emptyset^* \epsilon + \epsilon = (01+1) + \epsilon$$

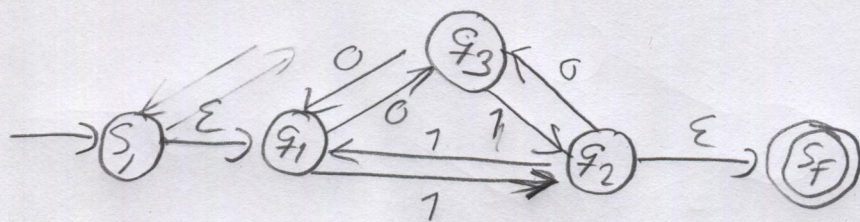


eliminate state 2: There is 1 path: $S_1 \rightarrow 2 \rightarrow S_F$



This reg. exp. describes the language of the original DFA.

3.5b) Redraw and add new start and final states



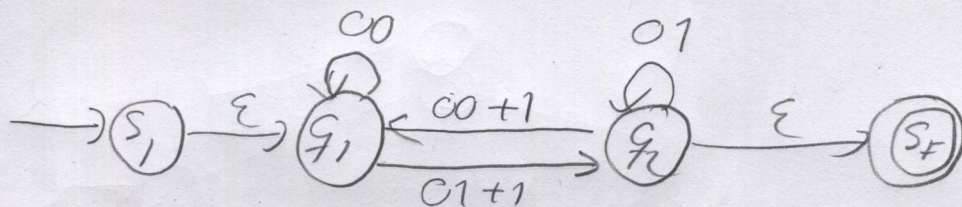
eliminate state Q_3 . There are 4 paths through Q_3 :

$$Q_1 \rightarrow Q_3 \rightarrow Q_1: 0\emptyset^*0 + \emptyset = 00$$

$$Q_1 \rightarrow Q_3 \rightarrow Q_2: 0\emptyset^*1 + 1 = 01 + 1$$

$$Q_2 \rightarrow Q_3 \rightarrow Q_1: 0\emptyset^*0 + 1 = 00 + 1$$

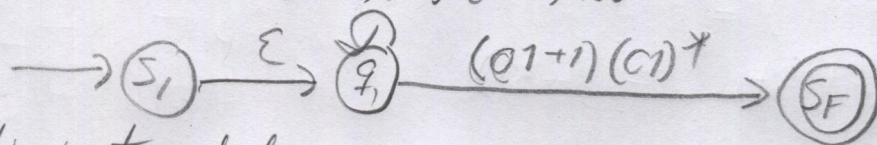
$$Q_2 \rightarrow Q_3 \rightarrow Q_2: 0\emptyset^*1 + \emptyset = 01$$



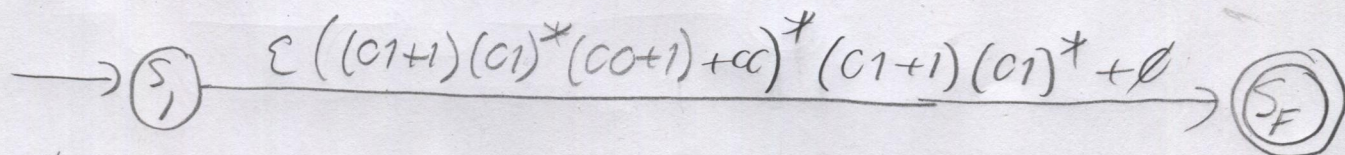
eliminate state Q_2 . There are 2 paths through Q_2 :

$$Q_1 \rightarrow Q_2 \rightarrow Q_1: (01+1)(01)^*(00+1) + 00$$

$$Q_1 \rightarrow Q_2 \rightarrow S_F: (01+1)(01)^*\epsilon + \emptyset = (01+1)(01)^*$$



eliminate state Q_1 . There is 1 path.



which simplifies to

$$((01+1)(01)^*(00+1)+00)^*(01+1)(01)^*$$