Meta-Programming with Modelica

for Meta-Modeling and Model Transformations

Peter Fritzson, Adrian Pop
OpenModelica Course, 2007 02 05

Extensibility and Modularity of Modeling Tools

- Modeling and simulation tools are too monolithic
- Models and tools need to be extensible and modular
- Creation, query, manipulation, composition and management of models
- Need for modeling of operations on models

Some Semantics Modeling Approaches

- Extensibility - allow models to also model language properties
- Ontologies to classify application domains
  - For example, semantic web
- Equation-based approaches
  - Modelica – hybrid differential algebraic equations
  - Single-assignment equations – functional languages, SOS/Natural semantics
  - Unification equations: logic programming and functional languages, SOS/Natural semantics
  - Can usually be efficiently executed
- Logic approaches
  - First-order logic
  - Often computationally intractable for realistic applications in its general form

Meta-Level Operations on Models

- Model Operations
  - Creation
  - Query
  - Manipulation,
  - Composition
  - management
- Manipulation of model equations for
  - Optimization purposes
  - Parallelization
  - Model checking
  - Simulation with different solvers
- Modularity
  - Allow model packages for tool extensions
  - Example: Automatic PDE discretization schemes

Meta-Level Operations on Models, Cont.

- Model configuration for simulation purposes
  - Initial state
  - Initialization via xml data files or databases
- Simulation features
  - Running a simulation and display a result
  - Running more simulations in parallel
  - Handle simulation failures and continue the simulation in a different way
  - Possibility to generate ONLY specific data from a simulation
  - Possibility to manipulate simulation data for export to another tool

Meta-Modelica Compiler (MMC) and Language

- Supports extended *subset* of Modelica
- Used for development of OMC
- Some MetaModelica Language properties:
  - Modelica syntax and base semantics
  - Pattern matching (named/positional)
  - Local equations (local within expression)
  - Recursive tree data structures
  - Lists and tuples
  - Garbage collection of heap-allocated data
  - Arrays (with local update as in standard Modelica)
  - Polymorphic functions
  - Function formal parameters to functions
  - Simple builtin exception (failure) handling mechanism

A Simple match-Expression Example

- Example, returning a number, given a string

```
  String s;
  Real   x;
algorithm
  x :=
    matchcontinue s
      case "one"   then 1;
      case "two"   then 2;
      case "three" then 3;
      else              0;
    end matchcontinue;
```


Tree Types – uniontype Declaration Example

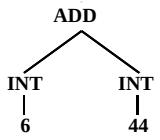
- Union types specifies a *union* of one or more record types
- Union types can be *recursive* - can reference themselves

MetaModelica tree type declaration:

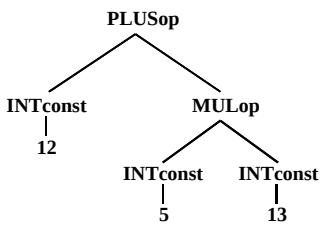
```
uniontype Exp
  record INT  Integer x1;      end INT;
  record NEG  Exp x1;          end NEG;
  record ADD  Exp x1; Exp x2;  end ADD;
end Exp;
```

- The Exp type is a union type of three record types
- Record constructors INT, NEG and ADD
- Common usage is abstract syntax trees.

ADD(INT(6),INT(44))



Another uniontype Declaration of Exp Expressions



Abstract syntax tree data type declaration of Exp:

```
uniontype Exp
  record INTconst Integer x1;  end INTconst;
  record PLUSop  Exp x1; Exp x2; end PLUSop;
  record SUBop   Exp x1; Exp x2; end SUBop;
  record MULop   Exp x1; Exp x2; end MULop;
  record DIVop   Exp x1; Exp x2; end DIVop;
  record NEGop   Exp x1;         end NEGop;
end Exp;
```

```
12+5*13

PLUSop(INTconst(12),
       MULop(INTconst(5),INTconst(13)))
```


Simple Expression Interpreter – with equation keyword, match, case

```
function eval "Evaluates integer expression trees"
  input  Exp     exp;
  output Integer intval;
algorithm
 intval :=
  matchcontinue exp
    local Integer v1,v2; Exp e1,e2;
    case INTconst(v1) then v1;
    case PLUSop(e1,e2) equation
      v1 = eval(e1);  v2 = eval(e2); then v1+v2;
    case SUBop(e1,e2) equation
      v1 = eval(e1);  v2 = eval(e2); then v1-v2;
    case MULop(e1,e2) equation
      v1 = eval(e1);  v2 = eval(e2); then v1*v2;
    case DIVop(e1,e2) equation
      v1 = eval(e1);  v2 = eval(e2); then v1/v2;
    case NEGop(e1) equation
      eval(e1) = v1; then  -v1;
  end matchcontinue;
end eval;
```

Local variables with scope inside case expression

Pattern binding local pattern variables e1, e2

Local equations with local unknowns v1, v2

A returned value

Example: Simple Symbolic Differentiator

```
function difft "Symbolic differentiation
    of expression with respect to time"
  input  Exp expr;
  input  list<IDENT> timevars;
  output Exp diffexpr;
algorithm
 diffexpr :=
  matchcontinue (expr, timevars)
    local Exp e1prim,e2prim,tvars;
          Exp e1,e2,id;
// der of constant
    case(RCONST(_), _) then RCONST(0.0);
// der of time variable
    case(IDENT("time"), _) then
      RCONST(1.0);
// der of any variable id
    case (id as IDENT(_),tvars) then
      if listMember(id,tvars) then
        CALL(IDENT("der"),list(id))
      else
        RCONST(0.0);
 ...
```

```
// (e1+e2)' => e1'+e2'
    case (ADD(e1,e2),tvars) equation
      e1prim = difft(e1,tvars);
      e2prim = difft(e2,tvars);
      then ADD(e1prim,e2prim);
 // (e1-e2)' => e1'-e2'
    case (SUB(e1,e2),tvars) equation
      e1prim = difft(e1,tvars);
      e2prim = difft(e2,tvars);
      then SUB(e1prim,e2prim);
// (e1*e2)' => e1'*e2 + e1*e2'
    case (MUL(e1,e2),tvars) equation
      e1prim = difft(e1,tvars);
      e2prim = difft(e2,tvars);
      then PLUS(MUL(e1prim,e2),
              MUL(e1,e2prim));
...
```


General Syntactic Structure of match-expressions

```
matchcontinue <expr>  <opt-local-decl>

  case <pat-expr> <opt-local-decl>
    <opt-equations>
    then <expr>;
  case <pat-expr> <opt-local-decl>
    <opt-equations>
    then <expr>;
  ...
  else <opt-local-decl>
    <opt-equations>
    then <expr>;

end matchcontinue;
```

Semantics of Local Equations in match-Expressions

- Only algebraic equations are allowed, no differential equations
- Only locally declared variables (local unknowns) declared by local declarations within the case expression are solved for
- Equations are solved in the order they are declared. (This restriction may be removed in the future).
- If an equation or an expression in a `case`-branch of a matchcontinue-expression fails, all local variables become unbound, and matching continues with the next branch.

Semantics of Local Equations cont...

- Certain equations in match-expressions do not solve for any variables – they may be called "constraints"
  - All variables are already bound in these equations
  - The equation may either be fulfilled (succeed) or not (fail)
  - Example:

```
local
  Real x=5; Integer y = 10;
equation
  true = x>4;    // Succeeds!
  true = y<10;   // Fails!!
```

- Thus, there can locally be more equations than unbound variables, if including the constraints

List Data Structures

- **`list`** – **`list`**<type-expr> is a list type constructor
  - Example: **`type`** `RealList =` **`list`**`<Real>;` type is a list of reals
  - Example: **`list`**`<Real> rlist;` variable that is a list of reals
- `list` – `list`(el1,el2,el3, ...) is a list data constructor that creates a list of elements of identical type.
  - `{}` or `list`() empty list
  - `{2,3,4}` or `list`(2,3,4) list of integers
- Allow {el1,el2,el3, ...} overloaded array or list constructor, interpreted as array(...) or list(...) depending on type context.
- **`{} or`** `list()` denotes an empty reference to a list or tree. `cons` – `cons`(*element*, *lst*) adds an element in front of the list *lst* and returns the resulting list.
- Also as `::` operator – *element*`::`*lst*

Predefined Polymorphic List Operations

```
function listAppend
  input list<Eltype> lst1;
  input list<Eltype> lst2;
  output list<Eltype> lst3;
 replaceable type Eltype subtypeof Any;
end listAppend;

function listReverse
  input list<Eltype> lst1;
  output list<Eltype> lst3;
 replaceable type Eltype subtypeof Any;
end listReverse;

function listLength
  input list<Eltype> lst1;
  output Integer len;
 replaceable type Eltype subtypeof Any;
end listLength;
```

```
function listMember
  input Eltype elem;
  input list<Eltype> lst2;
  output Boolean result;
replaceable type Eltype subtypeof Any;
end listMember;

function listNth
  input list<Eltype> lst1;
  input Integer elindex;
  output Eltype elem;
replaceable type Eltype subtypeof Any;
end listNth;

function listDelete
  input ListType lst1;
  input Integer  elindex;
  output ListType lst3;
replaceable type Eltype subtypeof Any;
 type ListType = list<Eltype>;
end listDelete;
```

Function Formal Parameters

- Functions can be passed as actual arguments at function calls.
- Type checking done on the function formal parameter type signature, not including the actual names of inputs and outputs to the passed function.

```
function intListMap   "Map over a list of integers"
  input  Functype func;
  input  list<Integer> inlst;
  output list<Integer> outlst;
public
  partial function Functype input Integer x1; output Integer x2; end Functype;
algorithm  ...
end intListMap;
```

```
function listMap    "Map over a list of elements of Type_a, a type parameter"
  input  Functype func;
  input  list<Type_a> inlst;
  output list<Type_a> outlst;
public
  replaceable type Type_a;
  partial function Functype  input Type_a x1; output Type_a x2; end Functype;
algorithm  ...
end listMap;
```


Calling Functions with Function Formal Parameters and/or Parameterized Types

- Call with passed function arguments: `int_list_map(add1,intlst1)`
  Declared using type Int
- Compiler uses type inference to derive type of replaceable type parameter `Type_a = Integer`
  from input list type `list<Integer>` in `listMap(add1, intlst1);`

```
// call function intListMap   "Map over a list of integers"
list<Integer> intlst1 := {1,3,5,9};
list<Integer> intlst2;

intlst2 := intListMap(add1, intlst1);
```

```
// call function listMap   "Map over a list of Type_a - a type parameter"
list<Integer> intlst1 := {1,3,5,9};
list<Integer> intlst2;

intlst2 := listMap(add1, intlst1);  // The type parameter is
```

Tuple Data Structures

- Tuples are anonymous records without field names
- **tuple**<...> – tuple type constructor (keyword not needed)
  - Example: `type VarBND = tuple<Ident, Integer>;`
  - Example: `tuple<Real,Integer> realintpair;`
- (..., ..., ...) – tuple data constructor
  - Example: `(3.14, "this is a string")`
- Modelica functions with multiple results return tuples
  - Example: `(a,b,c) := foo(x, 2, 3, 5);`

Option Type Constructor

- The **`Option`** type constructor, parameterized by some type (e.g.,`Type_a`) creates a kind of uniontype with the predefined constructors `NONE()` and `SOME(...)`:

```
replaceable type Type_a subtypeof Any;
type Option_a = Option<Type_a>;
```

- The constant `NONE()` with no arguments automatically belongs to any option type. A constructor call such as `SOME(x1)` where `x1` has the type `Type_a`, has the type `Option<Type_a>`.
- Roughly equivalent to:

```
uniontype Option
  record NONE  end NONE;
  record SOME  Type_a x1;  end SOME;
 replaceable type Type_a subtypeof Any;
end Option;
```

Testing for Failure

- A local equation may fail or succeed.
- A builtin equation operator `failure`(arg) succeeds if *arg* fails, where *arg* is a local equation

Example, testing for failure in Modelica:

```
case ((id2,_) :: rest, id)
  equation
    failure(true =  id ==& id2);  value = lookup(rest,id);
  then value;
```


Generating a fail "Exception"

- A call to `fail()` will fail the current case-branch in the match-expression and continue with the next branch.
- If there are no more case-branches, the enclosing function will fail.
- An expression or equation may fail for other reasons, e.g. division by zero, no match, unsolvable equation, etc.

as-expressions in Pattern Expressions

- An unbound local variable (declared `local`) can be set equal to an expression in a pattern expression through an as-expresson (`var` **`as`** `subexpr`)
- This is used to give another name to `subexpr`
- The same variable may only be associated with one expression
- The value of the expression equation (`var` **`as`** `subexpr`) is `subexpr`
- Example:
  - `(a` **`as`** `Absyn.IDENT("der"), expl,b,c)`

Summary of New MetaModelica Reserved Words

- _ Underscore is a reserved word used as a pattern placeholder, name placeholder in anonymous functions, types, classes, etc.
- (**`match`** is used in match-expressions).
- **`matchcontinue`** is used in matchcontinue-expressions.
- **`case`** is used in match/matchcontinue-expressions.
- **`local`** is used for local declarations in match expressions, etc.
- **`uniontype`** for union type declarations, e.g. tree data types.
- **`as`** for as-expressions

Summary of New Reserved Words Cont'

- **`list`** can be a reserved word, but this is not necessary since it is only used in list(...) expressions
- **`Option`** is a predefined parameterized union type

Summary of New Builtin Functions and Operators

- `list`<...> – list type constructor, in type context
- `tuple`<...> – tuple type constructor
- `list`(...) – list data constructor, in expression context
- `cons`(*element*, *lst*) – attach *element* at front of list *lst*
- `fail`() – Raise fail exception, having null value
- (..., ..., ...) or `tuple`(..., ..., ...) – tuple data constructor
- `::` – List `cons` operator

Conclusions

- Meta-modeling increasingly important, also for the Modelica language and its applications
- Meta-modeling/meta-programming extensions allow writing a Modelica compiler in Modelica
- Extensions are recursive union types (trees), lists, and match-expressions – standard constructs found in functional languages
- OpenModelica compiler implemented using MetaModelica extensions since March 2006.