## METRIC CLUSTER ANALYSIS OF MOLECULAR BIOLOGY DATA FOR SYSTEMS IDENTIFICATION OF GENE REGULATORY NETWORKS

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ABSTRACT. Our talk develops metrics for cluster analysis—with a view towards molecular systems-biology. We discuss negative type and other notions from "the sociology of metric spaces" (Gromov).

Cluster analysis uses dissimilarities, distances, and metrics. Metrics facilitate the analysis of clustering methods.

The mathematical theory of metric spaces has been used to characterize the applicability of statistical procedures. For example, least-squares methods rely on the geometric properties of inner-product spaces. In Banach spaces, the strong law of large numbers depends on Beck convexity. In metric spaces, the distance-covariance test of dependence relies on the negative type (Lyons 2013; Janson 2021); characterizing metric spaces that isometrically embed into Euclidean spaces, Schoenberg's negative type is used in computer science for the design & analysis of approximation algorithms (Deza & Laurent 1997).

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